

Value Semantics

It ain't about the syntax!

John Lakos

Friday, May 16, 2014

Copyright Notice

© 2014 Bloomberg L.P. Permission is granted to copy, distribute, and display this material, and to make derivative works and commercial use of it. The information in this material is provided "AS IS", without warranty of any kind. Neither Bloomberg nor any employee guarantees the correctness or completeness of such information. Bloomberg, its employees, and its affiliated entities and persons shall not be liable, directly or indirectly, in any way, for any inaccuracies, errors or omissions in such information. Nothing herein should be interpreted as stating the opinions, policies, recommendations, or positions of Bloomberg.

Abstract

When people talk about a type as having **value** **semantics**, they are often thinking about its ability to be passed to (or returned from) a function by value. In order to do that, the C++ language requires that the type implement a copy constructor, and so people routinely implement copy constructors on their classes, which begs the question, "Should an object of that type be copyable at all?" If so, what should be true about the copy? Should it have the same state as the original object? Same behavior? What does copying an object mean?!

By **value** **type**, most people assume that the type is specifically intended to represent a member of some set (of values). A value-semantic type, however, is one that strives to approximate an abstract **mathematical** type (e.g., integer, character set, complex-number sequence), which comprises operations as well as values. When we copy an object of a value-semantic type, the new object might not have the same state, or even the same behavior as the original object; for proper value semantic types, however, the new object will have the same value.

In this talk, we begin by gaining an intuitive feel for what we mean by **value** by identifying **salient** **attributes**, i.e., those that contribute to value, and by contrasting types whose objects naturally represent values with those that don't. After quickly reviewing the syntactic properties common to typical value types, we dive into the much deeper issues that value semantics entail. In particular, we explore the subtle Essential Property of Value, which applies to every **salient** mutating operation on a value-semantic object, and then profitably apply this property to realize a correct design for each of a variety of increasingly interesting (value-semantic) classes.

Outline

1. Introduction and Background

Components, Physical Design, and Class Categories

2. Understanding Value Semantics (and Syntax)

Most importantly, the Essential Property of Value

3. Two Important, Instructional Case Studies

Specifically, *Regular Expressions* and *Priority Queues*

4. Conclusion

What must be remembered when designing value types

Outline

1. Introduction and Background

Components, Physical Design, and Class Categories

2. Understanding Value Semantics (and Syntax)

Most importantly, the *Essential Property of Value*

3. Two Important, Instructional Case Studies

Specifically, *Regular Expressions* and *Priority Queues*

4. Conclusion

What must be remembered when designing value types

1. Introduction and Background

What's the Problem?

1. Introduction and Background

What's the Problem?

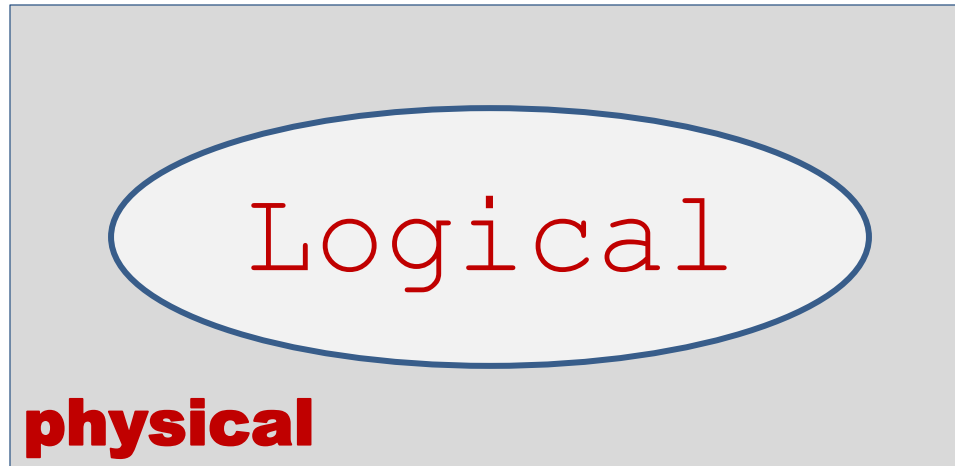
Large-Scale C++ Software Design:

- Involves many subtle logical and physical aspects.

1. Introduction and Background

Logical versus Physical Design

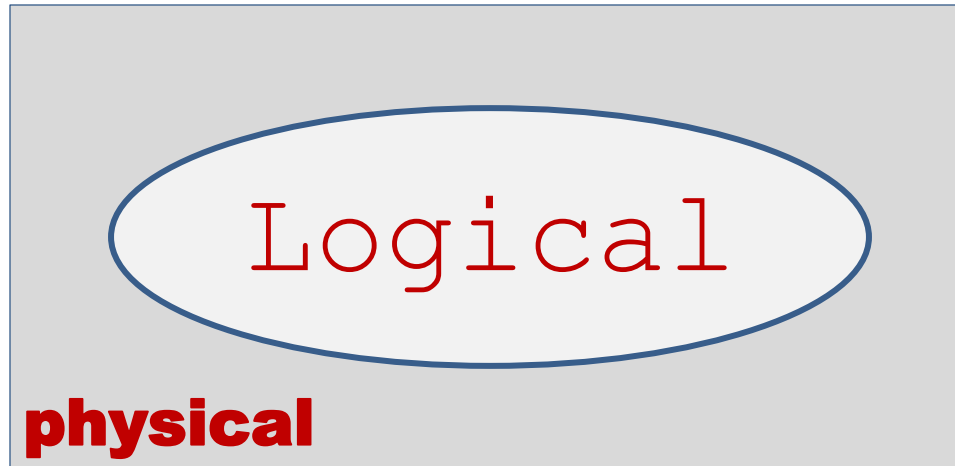
What distinguishes *Logical* from *Physical* Design?



1. Introduction and Background

Logical versus Physical Design

What distinguishes *Logical* from *Physical* Design?

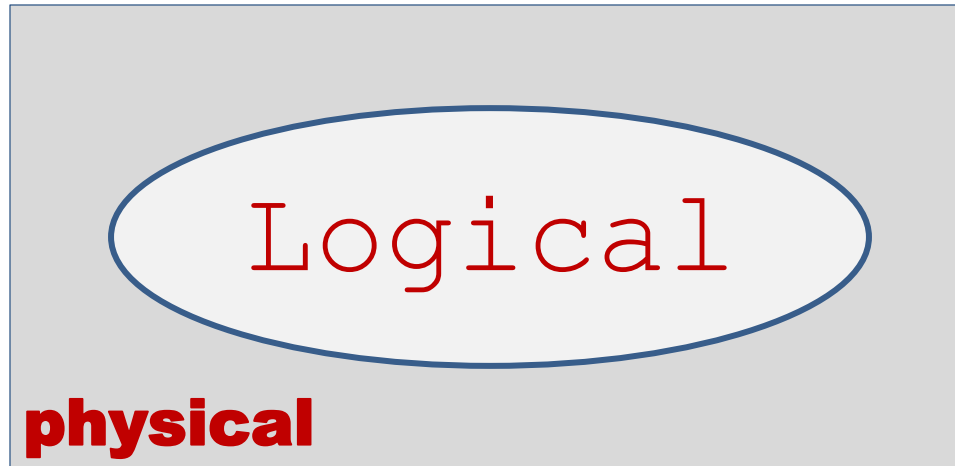


Logical: Classes and Functions

1. Introduction and Background

Logical versus Physical Design

What distinguishes *Logical* from *Physical* Design?



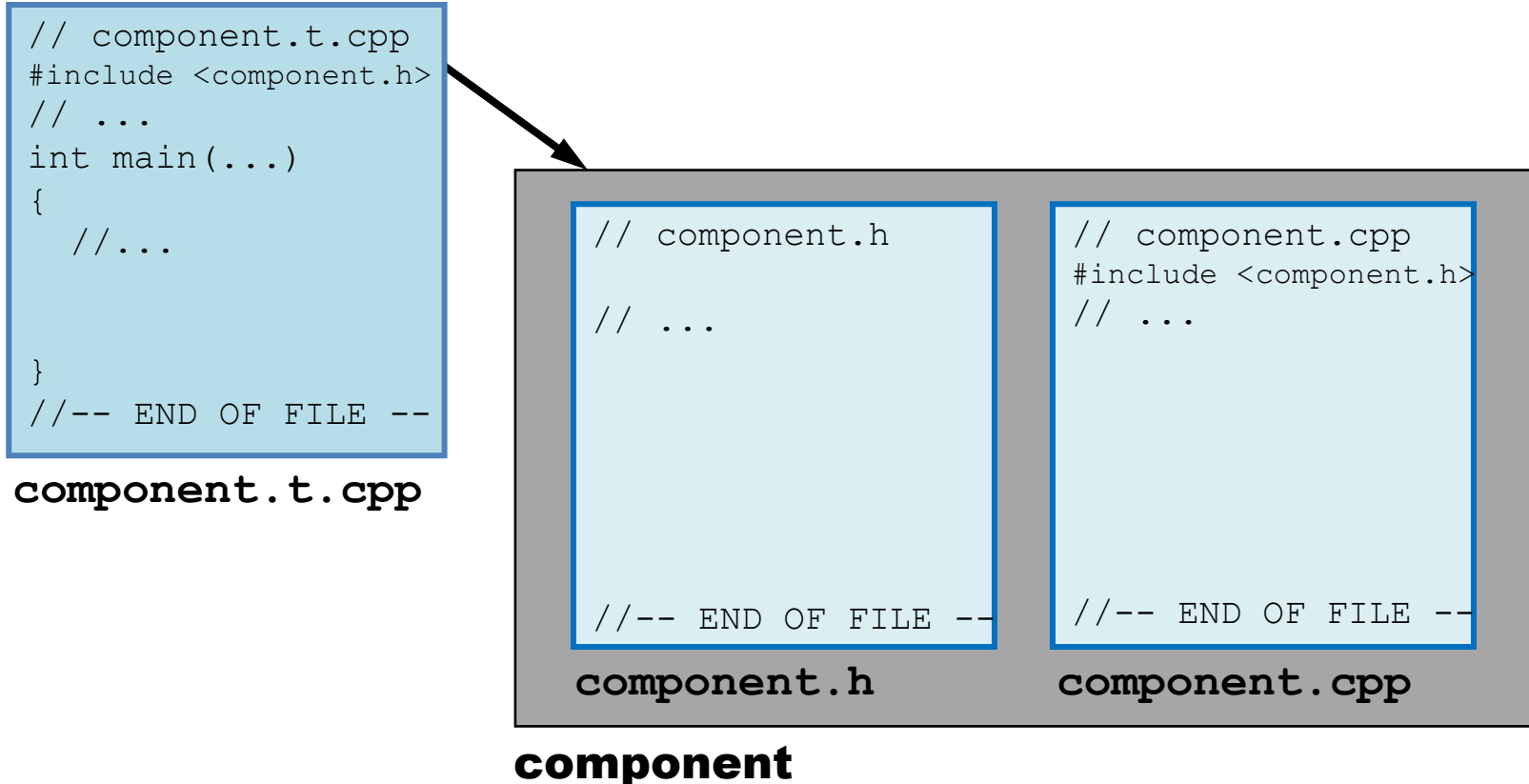
Logical: Classes and Functions

Physical: Files and Libraries

1. Introduction and Background

Component: Uniform Physical Structure

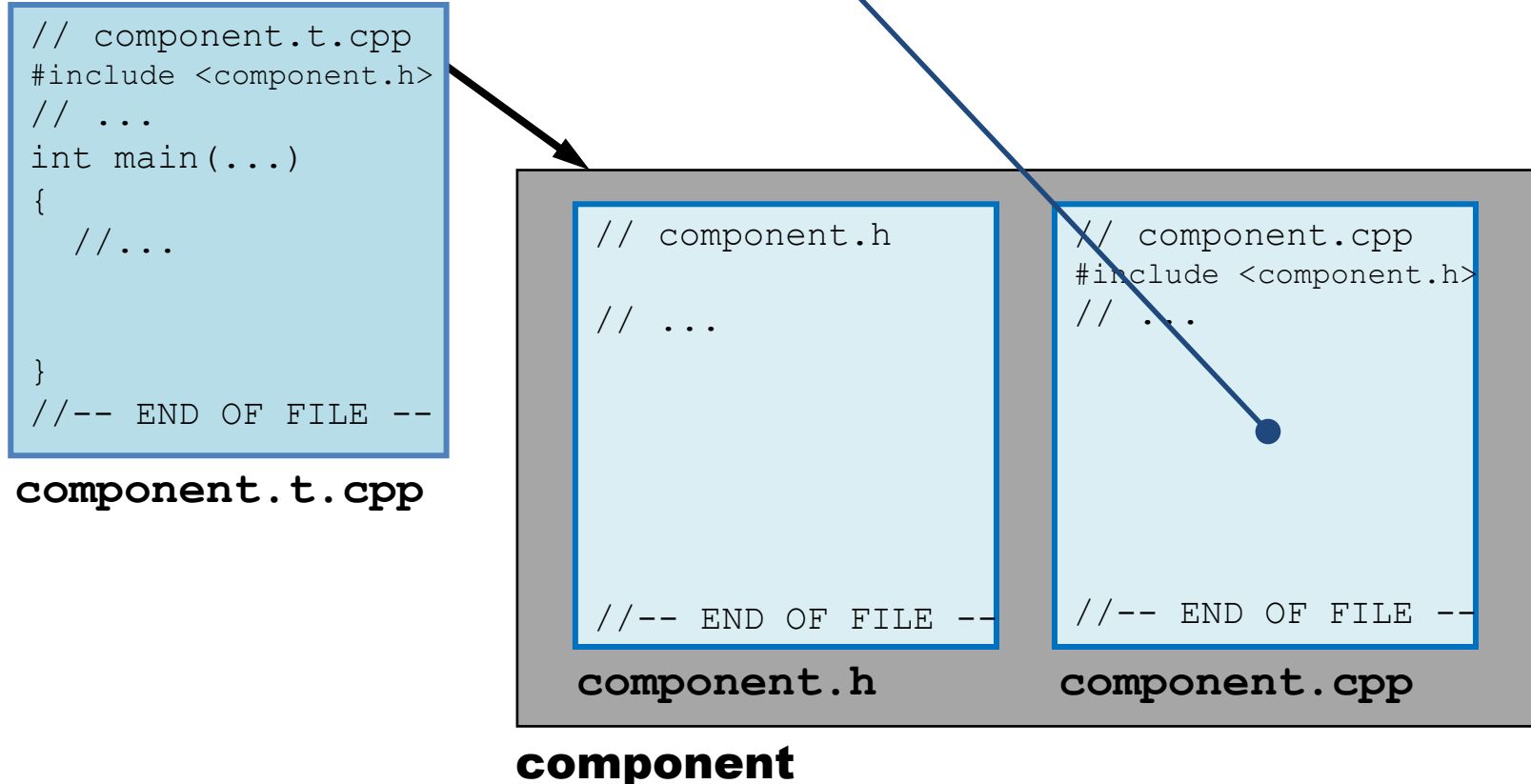
A Component Is Physical



1. Introduction and Background

Component: Uniform Physical Structure

Implementation



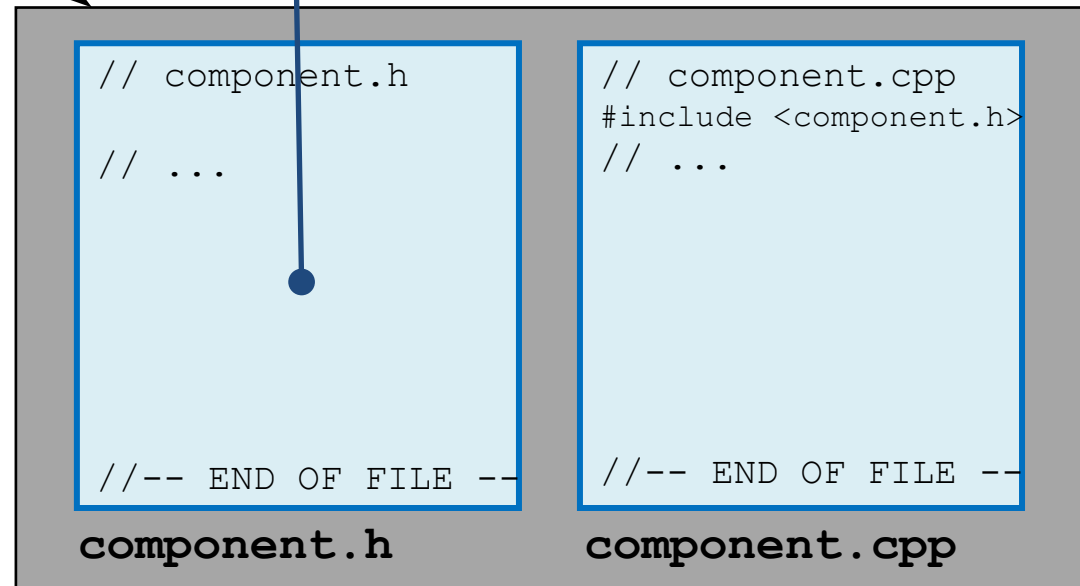
1. Introduction and Background

Component: Uniform Physical Structure

Header

```
// component.t.cpp
#include <component.h>
// ...
int main(...)
{
    //...
}
//-- END OF FILE --
```

component.t.cpp



component

1. Introduction and Background

Component: Uniform Physical Structure

Test Driver

```
// component.t.cpp
#include <component.h>
// ...
int main(...)
{
    //...
}
//-- END OF FILE --
```

component.t.cpp

```
// component.h
// ...
```

```
//-- END OF FILE --
```

component.h

```
// component.cpp
#include <component.h>
// ...
```

```
//-- END OF FILE --
```

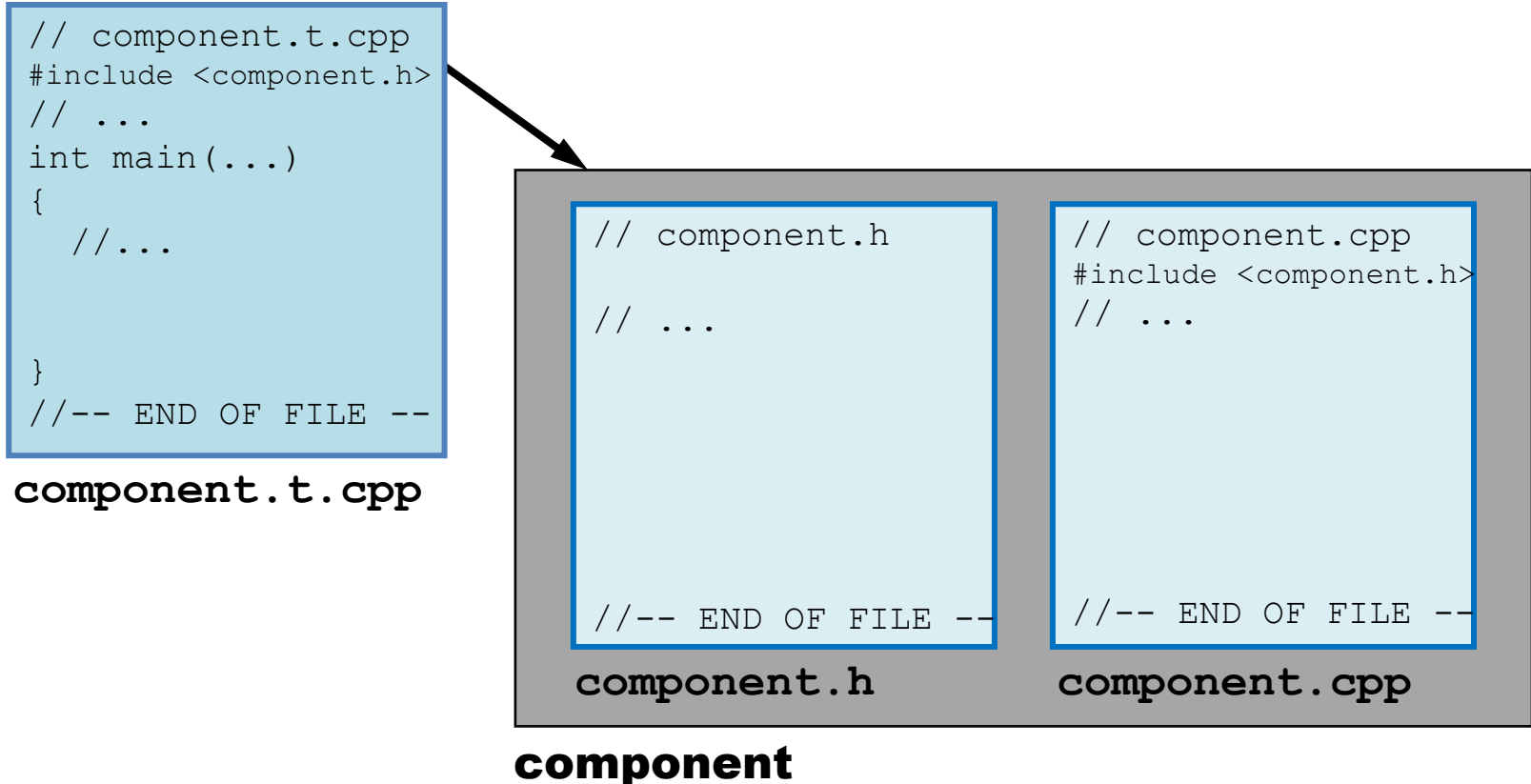
component.cpp

component

1. Introduction and Background

Component: Uniform Physical Structure

The Fundamental Unit of Design



1. Introduction and Background

What's the Problem?

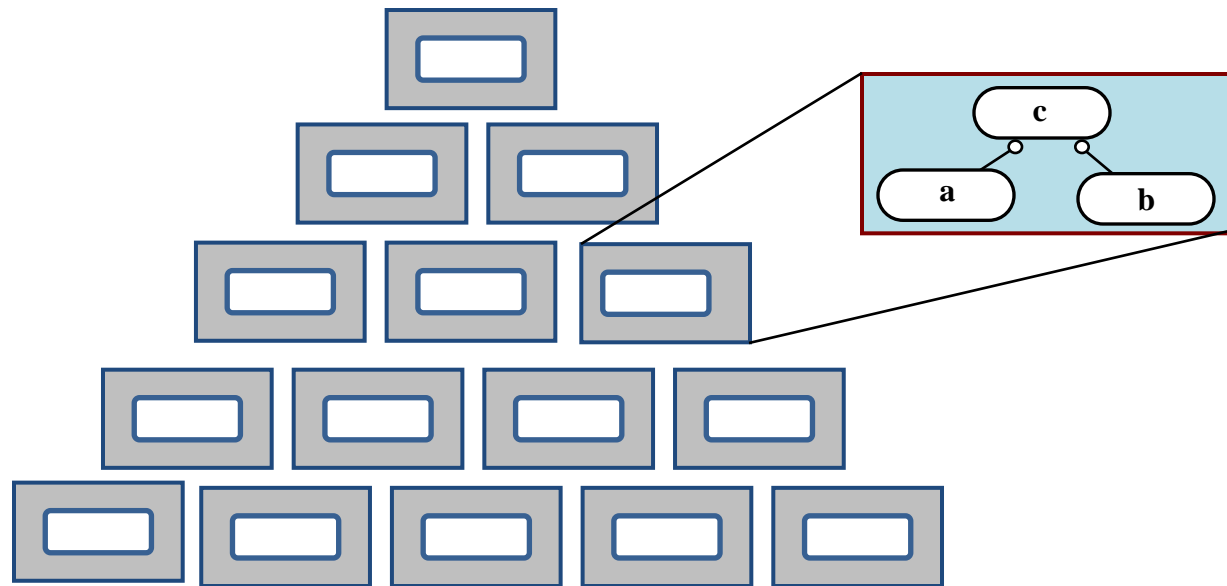
Large-Scale C++ Software Design:

- Involves many subtle logical and physical aspects.
- Requires an ability to isolate and modularize **logical functionality** within discrete, fine-grained **physical components**.

1. Introduction and Background

Logical versus Physical Design

Logical content aggregated into a
Physical hierarchy of **components**



1. Introduction and Background

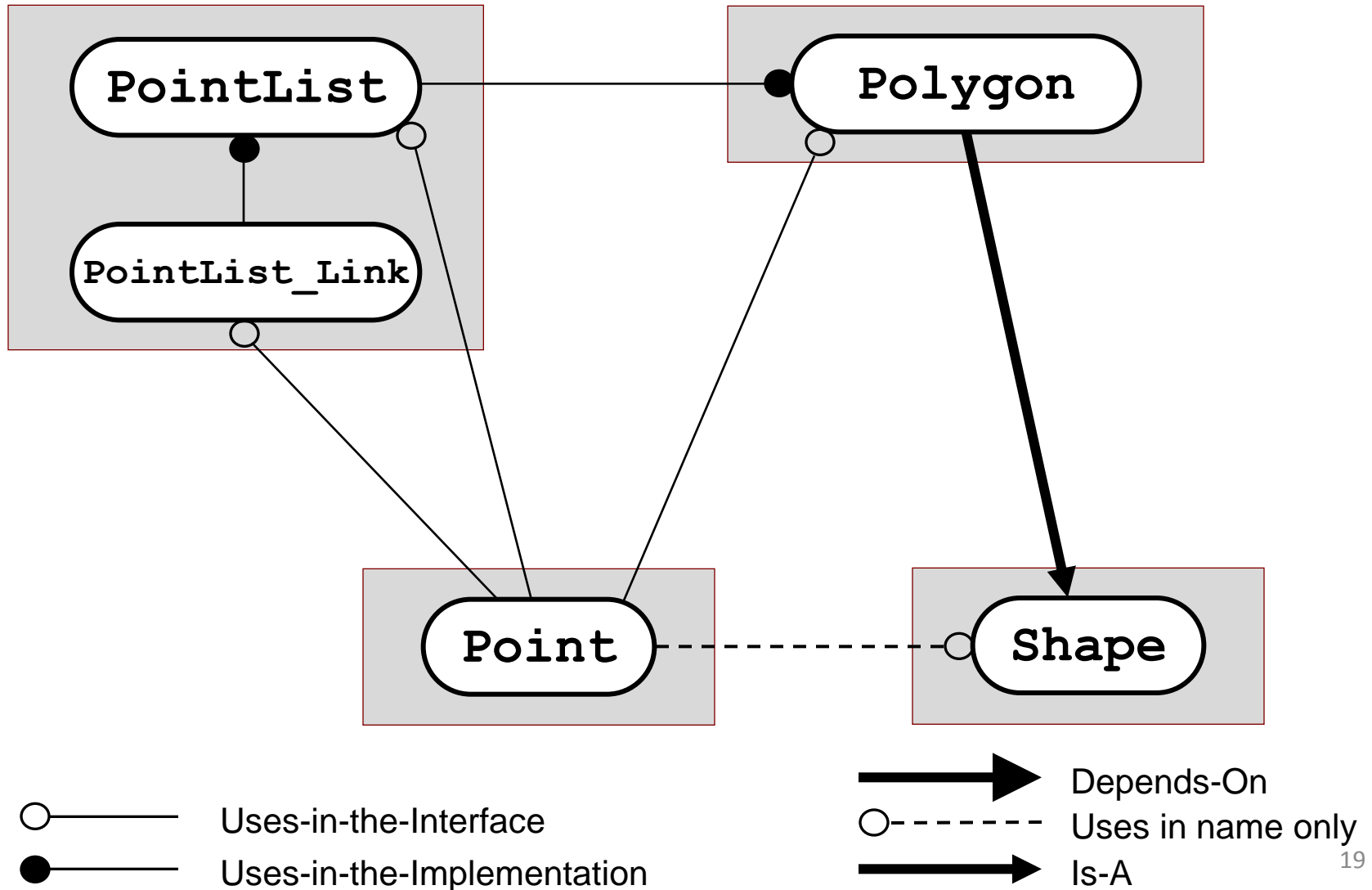
What's the Problem?

Large-Scale C++ Software Design:

- Involves many subtle logical and physical aspects.
- Requires an ability to isolate and modularize logical functionality within discrete, fine-grained physical components.
- Compels the designer to delineate **logical behavior** precisely, while managing the **physical dependencies** on other subordinate components.

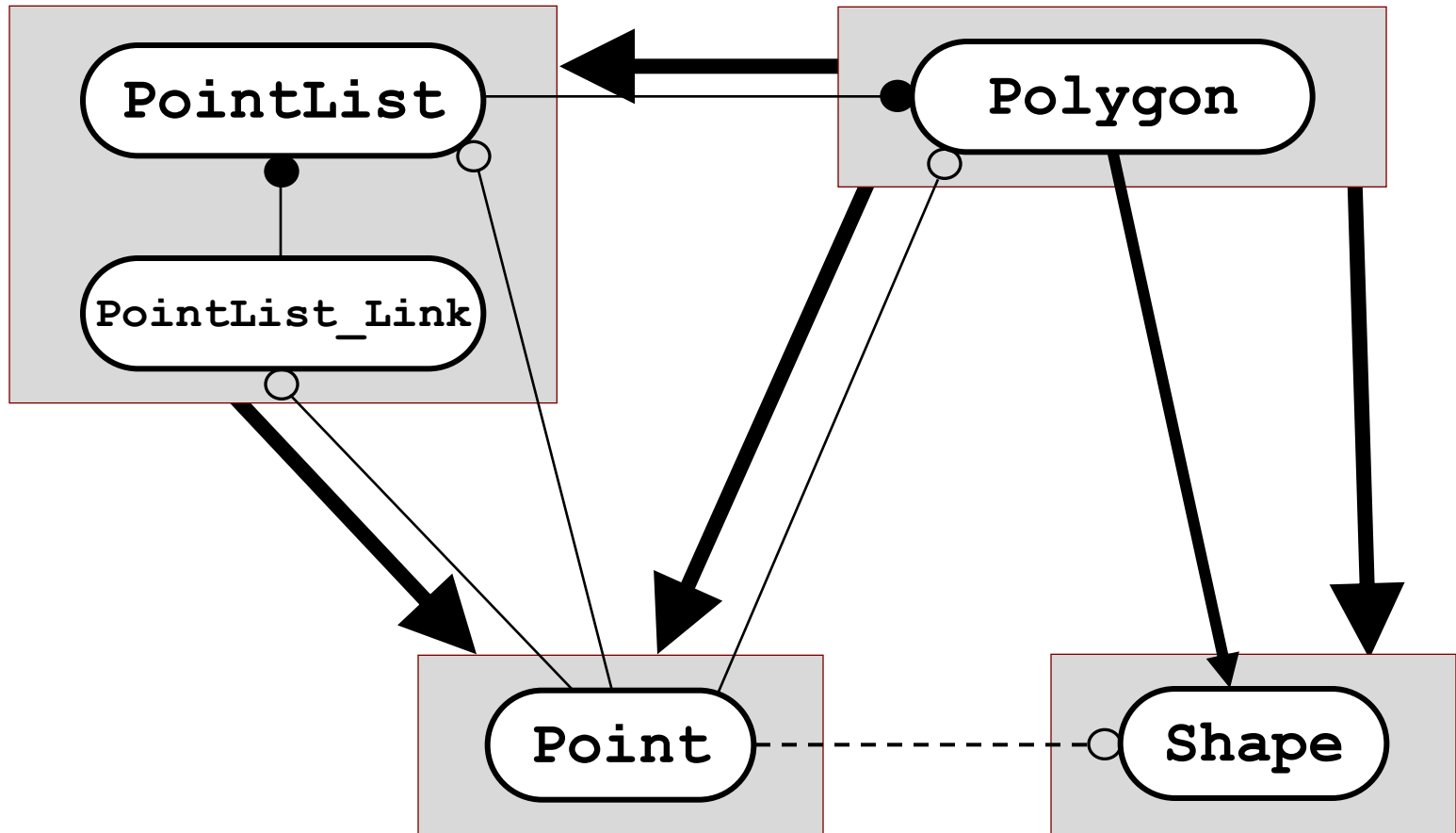
1. Introduction and Background

Implied Dependency



1. Introduction and Background

Implied Dependency



○ — Uses-in-the-Interface
● — Uses-in-the-Implementation

→ Depends-On
○ - - - Uses in name only
→ Is-A

1. Introduction and Background

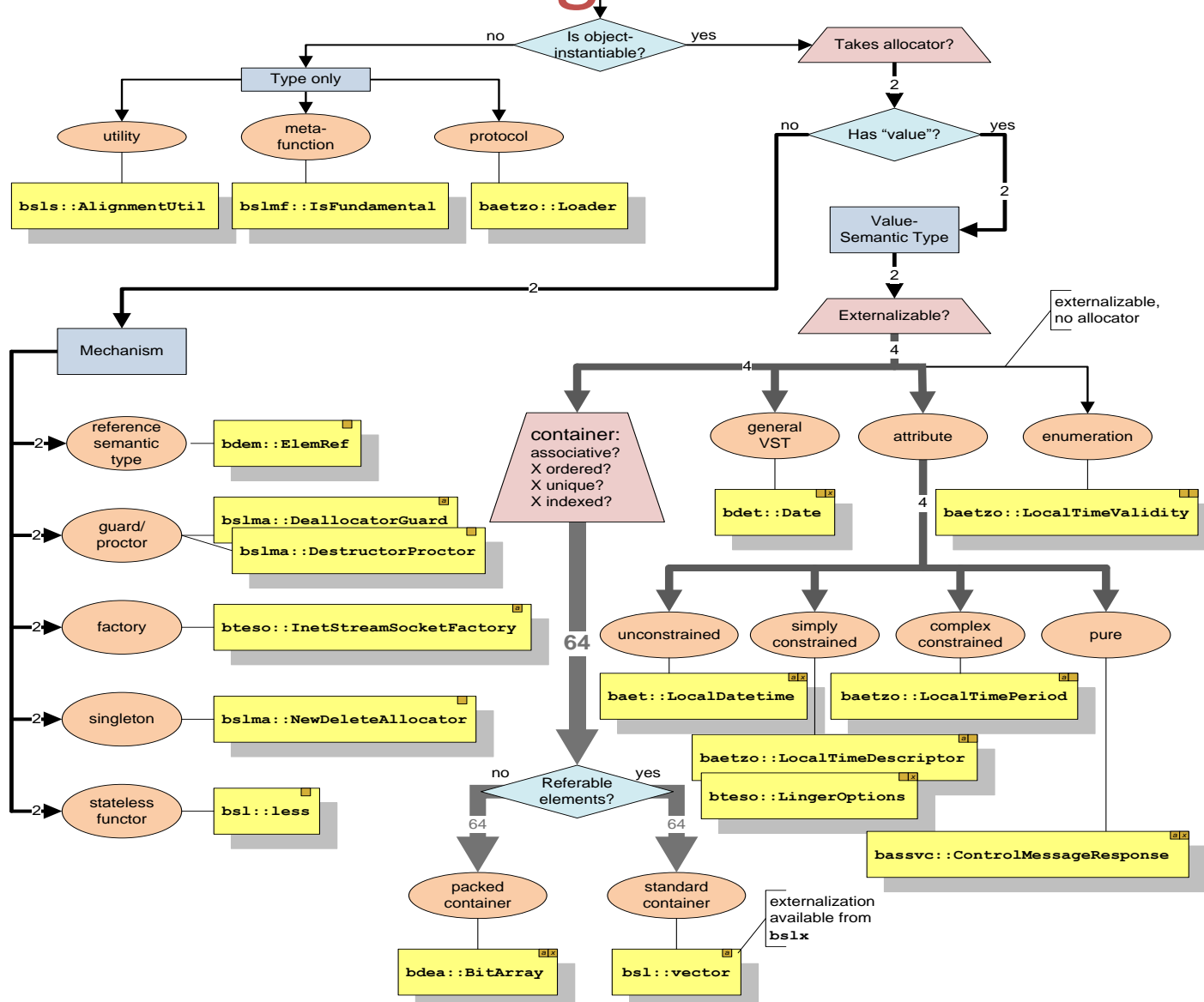
What's the Problem?

Large-Scale C++ Software Design:

- Involves many subtle logical and physical aspects.
- Requires an ability to isolate and modularize logical functionality within discrete, fine-grained physical components.
- Compels the designer to delineate logical behavior precisely, while managing the physical dependencies on other subordinate components.
- Demands a consistent, shared understanding of the properties of common class categories: **Value Types**.

1. Introduction and Background

The Big Picture



The Big Picture



Outline

1. Introduction and Background

Components, Physical Design, and Class Categories

2. Understanding Value Semantics (and Syntax)

Most importantly, the Essential Property of Value

3. Two Important, Instructional Case Studies

Specifically, *Regular Expressions* and *Priority Queues*

4. Conclusion

What must be remembered when designing value types

Outline

1. Introduction and Background

Components, Physical Design, and Class Categories

2. Understanding Value Semantics (and Syntax)

Most importantly, the Essential Property of Value

3. Two Important, Instructional Case Studies

Specifically, *Regular Expressions* and *Priority Queues*

4. Conclusion

What must be remembered when designing value types

2. Understanding Value Semantics

Purpose of this Talk

Answer some key questions about *value*:

- What do we mean by *value*?
- Why is the notion of value important?
- Which types should be considered value types?
- What do we expect *syntactically* of a value type?
- What *semantics* should its operations have?
- How do we design proper value-semantic types?
- When should value-related syntax be omitted?

2. Understanding Value Semantics

Value versus Non-Value Types

Getting Started:

2. Understanding Value Semantics

Value versus Non-Value Types

Getting Started:

- Not all useful C++ classes are value types.

2. Understanding Value Semantics

Value versus Non-Value Types

Getting Started:

- Not all useful C++ classes are value types.
- Still, value types form an important category.

2. Understanding Value Semantics

Value versus Non-Value Types

Getting Started:

- Not all useful C++ classes are value types.
- Still, value types form an important category.
- Let's begin with understanding some basic properties of value types.

2. Understanding Value Semantics

Value versus Non-Value Types

Getting Started:

- Not all useful C++ classes are value types.
- Still, value types form an important category.
- Let's begin with understanding some basic properties of value types.
- Then we'll contrast them with non-value types, to create a type-category hierarchy.

2. Understanding Value Semantics

Value versus Non-Value Types

Getting Started:

- Not all useful C++ classes are value types.
- Still, value types form an important category.
- Let's begin with understanding some basic properties of value types.
- Then we'll contrast them with non-value types, to create a type-category hierarchy.
- After that, we'll dig further into the details of value syntax and semantics.

2. Understanding Value Semantics

True Story

- Date: Friday Morning, October 5th, 2007
- Place: LWG, Kona, Hawaii
- Defect: issue #684: Wording of Working Paper

2. Understanding Value Semantics

True Story

- Date: Friday Morning, October 5th, 2007
- Place: LWG, Kona, Hawaii
- Defect: issue #684: Wording of Working Paper

What was meant by stating that two

`std::match_result`

objects (§28.10) were “the same” ?

2. Understanding Value Semantics

“The Same”

What do we mean by “the same”?

2. Understanding Value Semantics

“The Same”

What do we mean by “the same”?

- The two objects are *identical*?
 - same address, same process, same time?

2. Understanding Value Semantics

“The Same”

What do we mean by “the same”?

- The two objects are *identical*?
 - same address, same process, same time?
- The two objects are *distinct*, yet have certain *properties* in common.

2. Understanding Value Semantics

“The Same”

What do we mean by “the same”?

- The two objects are *identical*?
 - same address, same process, same time?
- The two objects are *distinct*, yet have certain *properties* in common.

(It turned out to be the latter.)

2. Understanding Value Semantics

“The Same”

What do we mean by “the same”?

- The two objects are *identical*?
 - same address, same process, same time?
- The two objects are *distinct*, yet have certain *properties* in common.

(It turned out to be the latter.)

So the meaning was clear...

2. Understanding Value Semantics

“The Same”

What do we mean by “the same”?

- The two objects are *identical*?
 - same address, same process, same time?
- The two objects are *distinct*, yet have certain *properties* in common.

(It turned out to be the latter.)

So the meaning was clear... *Or was it?*

2. Understanding Value Semantics

What exactly has to be “the Same”?

The discussion continued...

...some voiced suggestions:

2. Understanding Value Semantics

What exactly has to be “the Same”?

The discussion continued...

...some voiced suggestions:

- Whatever the copy constructor preserves.

2. Understanding Value Semantics

What exactly has to be “the Same”?

The discussion continued...

...some voiced suggestions:

- Whatever the copy constructor preserves.
- As long as the two are “equal”.

2. Understanding Value Semantics

What exactly has to be “the Same”?

The discussion continued...

...some voiced suggestions:

- Whatever the copy constructor preserves.
- As long as the two are “equal”.
- As long as they’re “equivalent”.

2. Understanding Value Semantics

What exactly has to be “the Same”?

The discussion continued...

...some voiced suggestions:

- Whatever the copy constructor preserves.
- As long as the two are “equal”.
- As long as they’re “equivalent”.
- “You know what I mean!!”

2. Understanding Value Semantics

What exactly has to be “the Same”?

The discussion continued...

...some voiced suggestions:

- Whatever the copy constructor preserves.
- As long as the two are “equal”.
- As long as they’re “equivalent”.
- “You know what I mean!!”

Since “purely wording” left solely to the editor!

2. Understanding Value Semantics

Not just an “Editorial Issue”?

2. Understanding Value Semantics

Not just an “Editorial Issue”?

What it means for two objects to be “the same” is an important, pervasive, and recurring concept in practical software design.

2. Understanding Value Semantics

Not just an “Editorial Issue”?

What it means for two objects to be “the same” is an important, pervasive, and recurring concept in practical software design.

Based on the notion of “*value*”.

What do we
mean by *value*?

2. Understanding Value Semantics

What does a *Copy Constructor* do?

2. Understanding Value Semantics

What does a *Copy Constructor* do?

After copy construction, the
resulting object is...

2. Understanding Value Semantics

What does a *Copy Constructor* do?

After copy construction, the resulting object is...

substitutable for the original one with respect to “some criteria”.

2. Understanding Value Semantics

What does a *Copy Constructor* do?

After copy construction, the resulting object is...

substitutable for the original one with respect to “some criteria”.

What Criteria?

2. Understanding Value Semantics

Same *Object*?

2. Understanding Value Semantics

Same *Object*?

```
std::vector<double> a, b(a);
```

```
assert(&a == &b);           // ??
```

2. Understanding Value Semantics

Same *Object*?

```
std::vector<double> a, b(a);
```

```
assert(&a == &b);           // ??
```

```
assert(0 == b.size());
```

```
a.push_back(5.0);
```

```
assert(1 == b.size());      // ??
```

2. Understanding Value Semantics

Same *Object*?

```
std::vector<double> a, b(a);
```

```
assert(&a == &b); // ??
```

```
assert(0 == b.size());
```

```
a.push_back(5.0);
```

```
assert(1 == b.size()); // ??
```

2. Understanding Value Semantics

Same *Object*?

```
std::vector<double> a, b(a);
```

```
assert(&a == &b); // ??
```

```
assert(0 == b.size());
```

```
a.push_back(5.0);
```

```
assert(1 == b.size()); // ??
```

Java?

2. Understanding Value Semantics

Same *Object*?

```
std::vector<double> a, b(a);
```

```
assert(&a == &b); // ??
```

```
assert(0 == b.size());
```

```
a.push_back(5.0);
```

```
assert(1 == b.size()); // ??
```


2. Understanding Value Semantics

Same *Object*?

```
std::vector<double> a, b(a);
```

```
assert(&a == &b); // ??
```

```
assert(0 == b.size());
```

```
a.push_back(5.0);
```

```
assert(1 == b.size()); // ??
```

2. Understanding Value Semantics

Same *State*?

2. Understanding Value Semantics

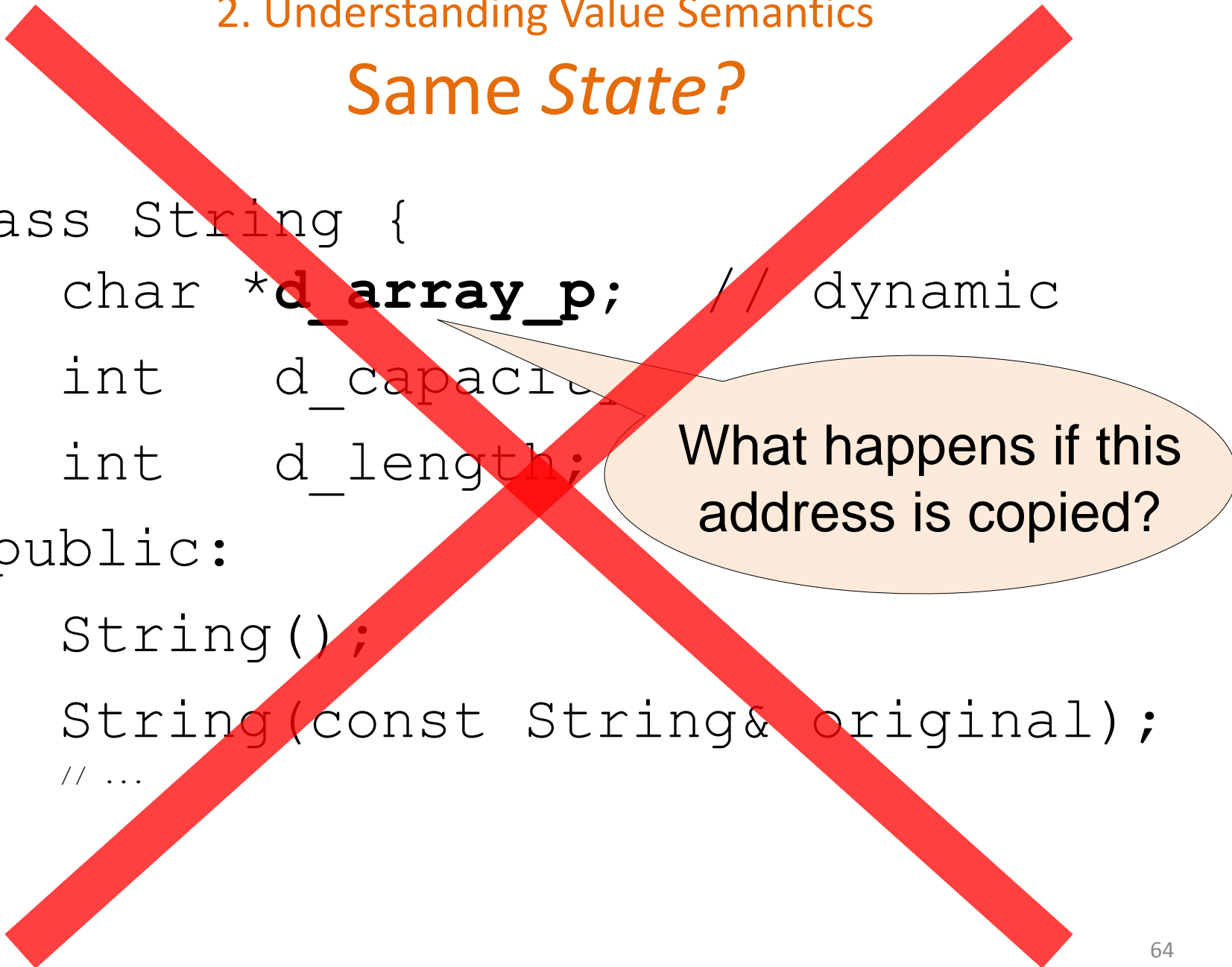
Same State?

```
class String {  
    char *d_array_p;    // dynamic  
    int    d_capacity;  
    int    d_length;  
public:  
    String();  
    String(const String& original);  
    // ...  
};
```

2. Understanding Value Semantics

Same *State*?

```
class String {  
    char *d_array_p; // dynamic  
    int    d_capacity;  
    int    d_length;  
public:  
    String();  
    String(const String& original);  
    // ...  
};
```



What happens if this address is copied?

2. Understanding Value Semantics

Same *Behavior*?

2. Understanding Value Semantics

Same *Behavior*?

If we apply *the same* sequence of operations to both objects, the observable behavior will be *the same*:

2. Understanding Value Semantics

Same *Behavior*?

If we apply *the same* sequence of operations to both objects, the observable behavior will be *the same*:

```
void f(bool x)
{
    std::vector<int> a;
    a.reserve(65536);           // is capacity copied?
    std::vector<int> b(a);      assert(a == b)
```

2. Understanding Value Semantics

Same *Behavior*?

If we apply *the same* sequence of operations to both objects, the observable behavior will be *the same*:

```
void f(bool x)
{
    std::vector<int> a;
    a.reserve(65536);           // is capacity copied?
    std::vector<int> b(a);      assert(a == b)

    a.reserve(65536);          // no reallocation!
    b.reserve(65536);          // memory allocation?
```


2. Understanding Value Semantics

Same Behavior?

If we apply *the same* sequence of operations to both objects, the observable behavior will be *the same*:

```
void f(bool x)
{
    std::vector<int> a;
    a.reserve(65536);           // is capacity copied?
    std::vector<int> b(a);      assert(a == b)

    a.reserve(65536);           // no reallocation!
    b.reserve(65536);           // memory allocation?

    a.push_back(5);  b.push_back(5); // so not empty

    std::vector<int>& r = x ? a : b;
    if (&r[0] == &a[0]) { std::cout << "Hello"; }
    else                { std::cout << "Goodbye"; }
}
```

2. Understanding Value Semantics

Same *What?*

2. Understanding Value Semantics

Same *What?*

What should be “the same”
after copy construction?

2. Understanding Value Semantics

Same *What?*

What should be “the same”
after copy construction?

(It better be easy to understand.)

2. Understanding Value Semantics

Same *What?*

What should be “the same”
after copy construction?

(It better be easy to understand.)

The two objects should
represent the same *value!*

2. Understanding Value Semantics

What do we mean by “value”?

2. Understanding Value Semantics

What do we mean by “value”?



2. Understanding Value Semantics

Mathematical Types

2. Understanding Value Semantics

Mathematical Types

A mathematical type consists of



- A set of globally **unique** *values*
 - Each one describable independently of any particular representation.

2. Understanding Value Semantics

Mathematical Types

A mathematical type consists of



- A set of globally **unique values**
 - Each one describable independently of any particular representation.
 - For example, the decimal integer 5:

5, 5, , 101 (binary), five, 

2. Understanding Value Semantics

Mathematical Types

A mathematical type consists of



- A set of globally **unique values**
 - Each one describable independently of any particular representation.
 - For example, the decimal integer 5:
 5 , 5 , , 101 (binary), $five$, 
- A set of *operations* on those values
 - For example: $+$, $-$, \times $(3 + 2)$

2. Understanding Value Semantics

Mathematical Types


A mathematical type consists of

- A set of globally **unique values**
 - Each one describable independently of any particular representation.
 - For example, the decimal integer 5:

5, 5, , 101 (binary), five, 

- A set of *operations* on those values

– For example: +, -, x (3 + 2)



Operations
will
become
important
shortly!

2. Understanding Value Semantics

C++ Type

2. Understanding Value Semantics

C++ Type

- A C++ type **may** represent (an approximation to) an abstract mathematical type:

2. Understanding Value Semantics

C++ Type

- A C++ type *may* represent (an approximation to) an abstract mathematical type:
 - For example: The C++ type `int` represents (an approximation to) the mathematical type *integer*.

2. Understanding Value Semantics

C++ Type

- A C++ type **may** represent (an approximation to) an abstract mathematical type:
 - For example: The C++ type `int` represents (an approximation to) the mathematical type *integer*.
- An object of such a C++ type represents one of (a subset of) the ***globally unique*** values in the set of that abstract *mathematical* type.

2. Understanding Value Semantics

C++ Type

- A C++ type **may** represent (an approximation to) an abstract mathematical type:
 - For example: The C++ type `int` represents (an approximation to) the mathematical type *integer*.
- An object of such a C++ type represents one of (a subset of) the ***globally unique*** values in the set of that abstract *mathematical* type.
- The C++ object is **just another representation** of that *globally unique*, abstract ***value***, e.g., 5.

2. Understanding Value Semantics

So, what do we mean by “value”?

```
class Date {  
    short d_year;  
    char  d_month;  
    char  d_day;  
public:  
    // ...  
    int year() ;  
    int month() ;  
    int day() ;  
};
```

2. Understanding Value Semantics

So, what do we mean by “value”?

```
class Date {  
    short d_year;  
    char  d_month;  
    char  d_day;  
public:  
    // ...  
    int year() ;  
    int month() ;  
    int day() ;  
};
```



2. Understanding Value Semantics

So, what do we mean by “value”?

```
class Date {  
    short d_year;  
    char  d_month;  
    char  d_day;  
public:  
    // ...  
    int year();  
    int month();  
    int day();  
};
```



2. Understanding Value Semantics

So, what do we mean by “value”?

```
class Date {  
    short d_year;  
    char  d_month;  
    char  d_day;  
public:  
    // ...  
    int year() const;  
    int month() const;  
    int day() const;  
};
```

2. Understanding Value Semantics

So, what do we mean by “value”?

```
class Date {  
    short d_year;  
    char  d_month;  
    char  d_day;  
public:  
    // ...  
    int year();  
    int month();  
    int day();  
};
```

```
class Date {  
    int d_serial;  
public:  
    // ...  
    int year();  
    int month();  
    int day();  
};
```

2. Understanding Value Semantics

So, what do we mean by “value”?

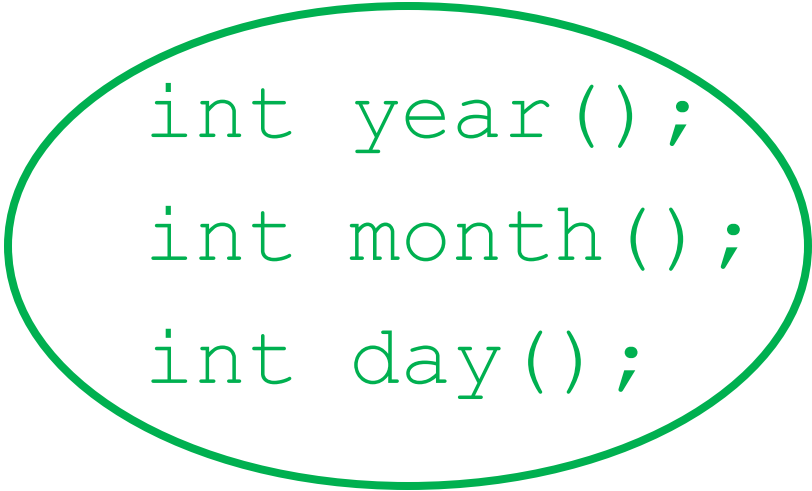
```
class Date {  
    short d_year;  
    char d_month;  
    char d_day;  
public:  
    //  
    int year();  
    int month();  
    int day();  
};
```

```
class Date {  
    int d_serial;  
public:  
    //  
    int year();  
    int month();  
    int day();  
};
```

2. Understanding Value Semantics

So, what do we mean by “value”?

Salient Attributes



```
int year();  
int month();  
int day();
```


2. Understanding Value Semantics

So, what do we mean by “value”?

Salient Attributes

The documented set of (observable) named attributes of a type \mathbb{T} that must respectively “have” (refer to) *the same* value in order for two instances of \mathbb{T} to “have” (refer to) *the same* value.

2. Understanding Value Semantics

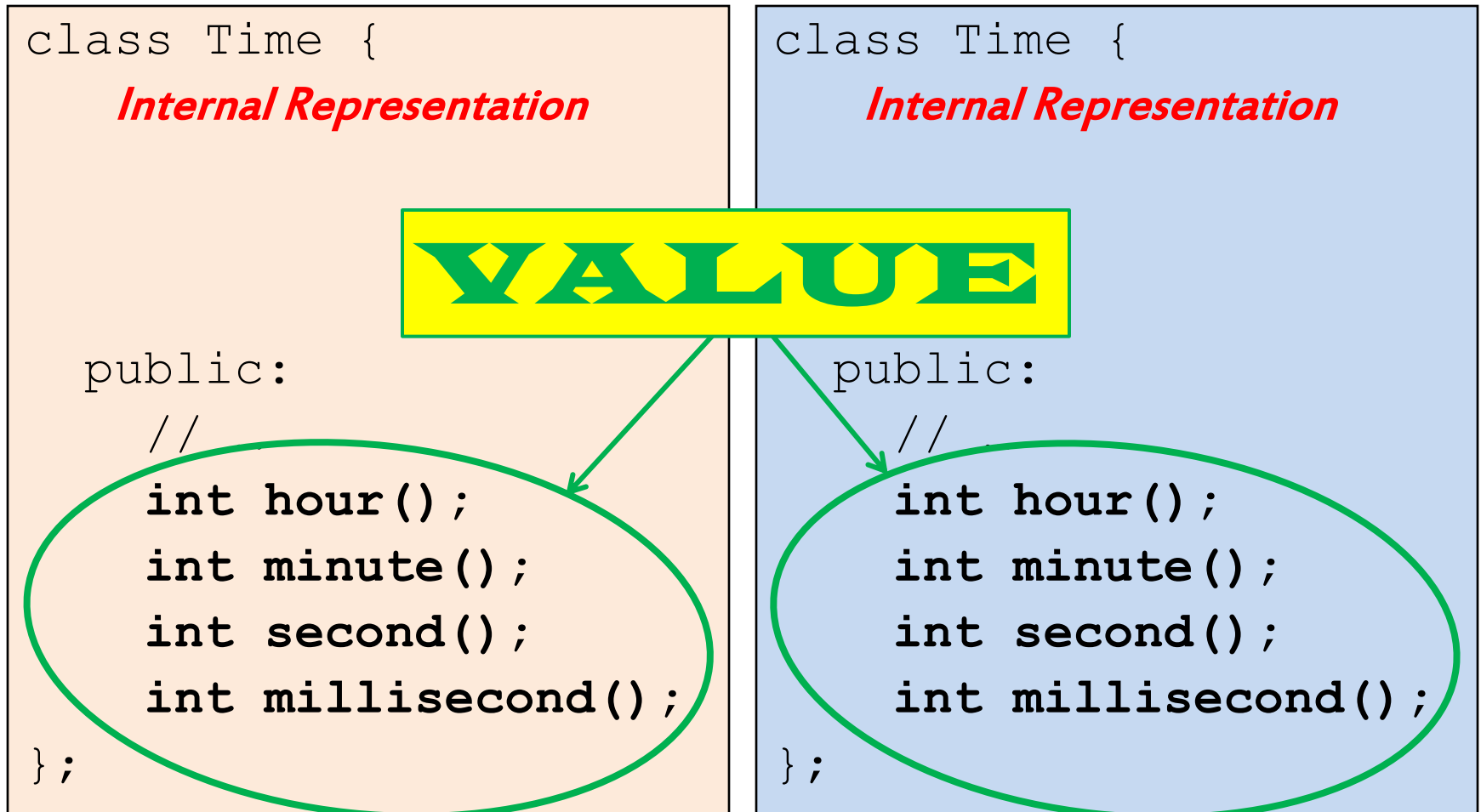
So, what do we mean by “value”?

```
class Time {  
    char    d_hour;  
    char    d_minute;  
    char    d_second;  
    short   d_millisecond;  
public:  
    // ...  
    int hour();  
    int minute();  
    int second();  
    int millisecond();  
};
```

```
class Time {  
    int d_mSeconds;  
  
public:  
    // ...  
    int hour();  
    int minute();  
    int second();  
    int millisecond();  
};
```

2. Understanding Value Semantics

So, what do we mean by “value”?



2. Understanding Value Semantics

So, what do we mean by “value”?

QUESTION:

What would be the simplest overarching mathematical type for which `std::string` and `(const char *)` are both approximations?

2. Understanding Value Semantics

So, what do we mean by “value”?

QUESTION:

So if they both represent the character sequence “Fred” do they represent the same value?

This is important!

2. Understanding Value Semantics

So, what do we mean by “value”?

QUESTION:

What about integers and
integers mod 5?

2. Understanding Value Semantics

So, what do we mean by “value”?

An “interpretation” of a subset of *instance* state.

2. Understanding Value Semantics

So, what do we mean by “value”?

An “interpretation” of a subset of *instance* state.

- The values of the **Salient Attributes**, and *not* the instance state used to represent them, comprise what we call the ***value*** of an object.

2. Understanding Value Semantics

So, what do we mean by “value”?

An “interpretation” of a subset of *instance* state.

- The values of the **Salient Attributes**, and *not* the instance state used to represent them, comprise what we call the **value** of an object.
- This definition may be **recursive** in that a documented **Salient Attribute** of a type T may itself be of type U having its own **Salient Attributes**.

2. Understanding Value Semantics

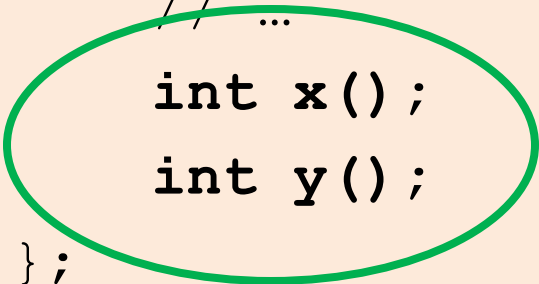
So, what do we mean by “value”?

```
class Point {  
    short int d_x;  
    short int d_y;  
public:  
    // ...  
    int x();  
    int y();  
};
```

2. Understanding Value Semantics

So, what do we mean by “value”?

```
class Point {  
    Internal Representation  
  
    public:  
        // ...  
        int x();  
        int y();  
};
```



2. Understanding Value Semantics

So, what do we mean by “value”?

```
class Point {  
    Internal Representation  
  
    public:  
        // ...  
        int x();  
        int y();  
};
```

```
class Box {  
    Point d_topLeft;  
    Point d_botRight;  
    public:  
        // ...  
        Point origin();  
        int length();  
        int width();  
  
};
```

2. Understanding Value Semantics

So, what do we mean by “value”?

```
class Point {
```

Internal Representation

```
public:
```

```
// ...
```

```
int x();
```

```
int y();
```

```
};
```

```
class Box {
```

Internal Representation

```
public:
```

```
// ...
```

```
Point origin();
```

```
int length();
```

```
int width();
```

```
};
```

2. Understanding Value Semantics

So, what do we mean by “value”?

```
class Point {  
    Internal Representation
```

```
public:
```

```
// ...
```

```
int x();
```

```
int y();
```

```
};
```

```
class Box {  
    Internal Representation
```

```
public:
```

```
// ...
```

```
Point origin();
```

```
int length();
```

```
int width();
```

```
};
```

Recursive

2. Understanding Value Semantics

What are “Salient Attributes”?

2. Understanding Value Semantics

What are “Salient Attributes”?

```
class vector {  
    T          *d_array_p;  
    size_type   d_capacity;  
    size_type   d_size;  
    // ...  
public:  
    vector();  
    vector(const vector<T>& orig);  
    // ...  
};
```


2. Understanding Value Semantics

What are “Salient Attributes”?

Consider `std::vector<int>`:

What are its *salient attributes*?

2. Understanding Value Semantics

What are “Salient Attributes”?

Consider `std::vector<int>`:

What are its *salient attributes*?

1. The number of elements: `size()`.

2. Understanding Value Semantics

What are “Salient Attributes”?

Consider `std::vector<int>`:

What are its *salient attributes*?

1. The number of elements: `size()`.
2. The *values* of the respective elements.

2. Understanding Value Semantics

What are “Salient Attributes”?

Consider `std::vector<int>`:

What are its *salient attributes*?

1. The number of elements: `size()`.
2. The *values* of the respective elements.
3. What about `capacity()`?

2. Understanding Value Semantics

What are “Salient Attributes”?

Consider `std::vector<int>`:

What are its *salient attributes*?

1. The number of elements: `size()`.
2. The *values* of the respective elements.
- ~~3. What about `capacity()`?~~

How is the client supposed to know for sure?

2. Understanding Value Semantics

What are “Salient Attributes”?

Salient Attributes:

2. Understanding Value Semantics

What are “Salient Attributes”?

Salient Attributes:

1. Are a part of logical design.

2. Understanding Value Semantics

What are “Salient Attributes”?

Salient Attributes:

1. Are a part of logical design.
2. *Should* be “natural” & “intuitive”.

2. Understanding Value Semantics

What are “Salient Attributes”?

Salient Attributes:

1. Are a part of logical design.
2. *Should* be “natural” & “intuitive”
3. Must be documented *explicitly*!

WHERE? HOW?
SOON!

Why is value
important?

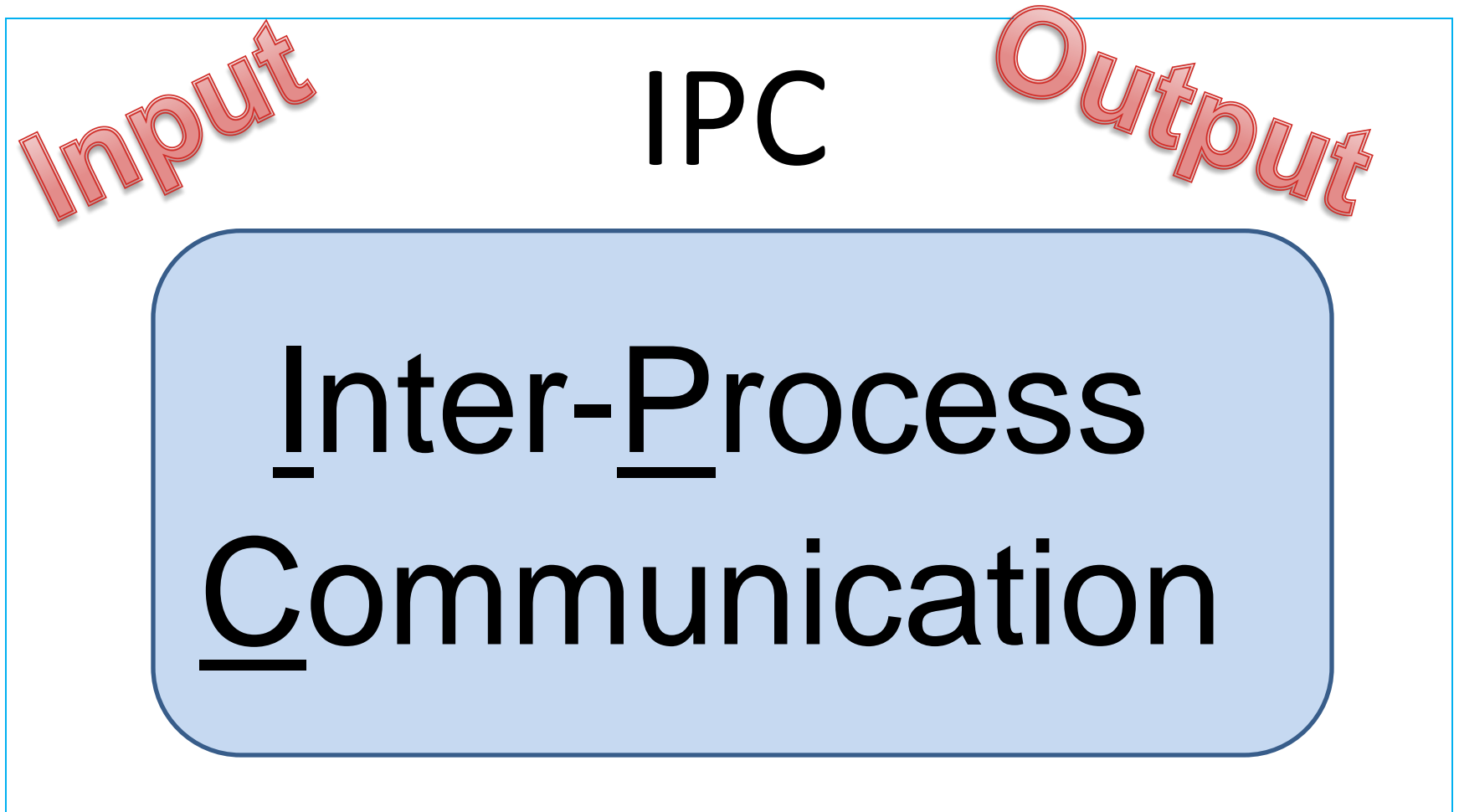
2. Understanding Value Semantics

Why are unique values important?



2. Understanding Value Semantics

Why are unique values important?



2. Understanding Value Semantics

Why are unique values important?

Abstract *date* Type

C++ Date Class

2. Understanding Value Semantics

Why are unique values important?

Abstract *date* Type

Has an infinite set of
valid *date* values.

C++ Date Class

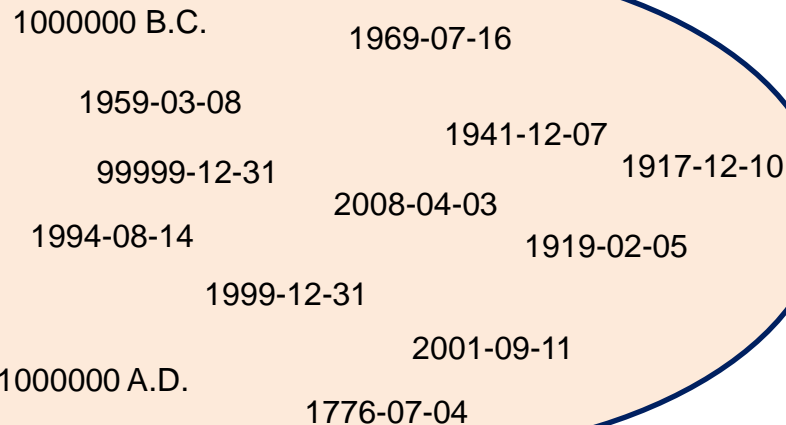
2. Understanding Value Semantics

Why are unique values important?

Abstract *date* Type

Has an infinite set of valid *date* values.

C++ Date Class



1000000 B.C. 1969-07-16
1959-03-08 1941-12-07
99999-12-31 1917-12-10
1994-08-14 2008-04-03
1999-12-31 1919-02-05
1000000 A.D. 2001-09-11
1776-07-04

Globally Unique Values

2. Understanding Value Semantics

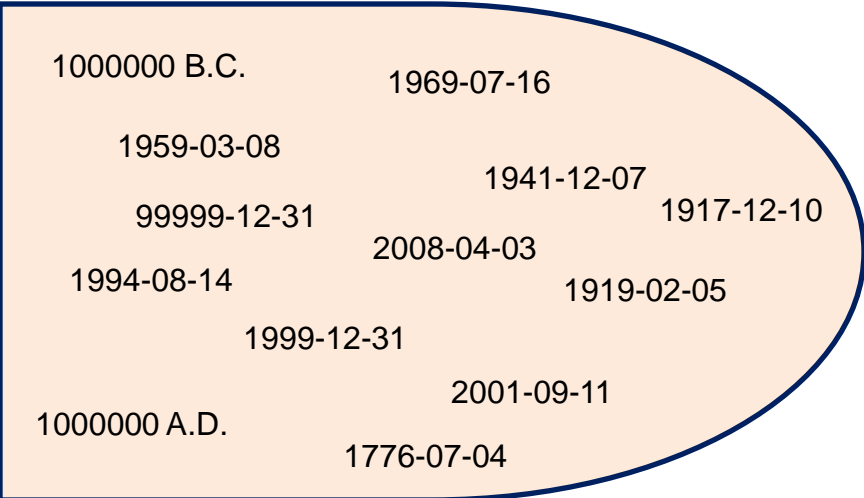
Why are unique values important?

Abstract *date* Type

Has an infinite set of valid *date* values.

C++ Date Class

Each instance refers to one of (a subset of) these abstract values.



1000000 B.C. 1969-07-16
1959-03-08 1941-12-07
99999-12-31 1917-12-10
1994-08-14 2008-04-03
1999-12-31 1919-02-05
1000000 A.D. 2001-09-11
1776-07-04

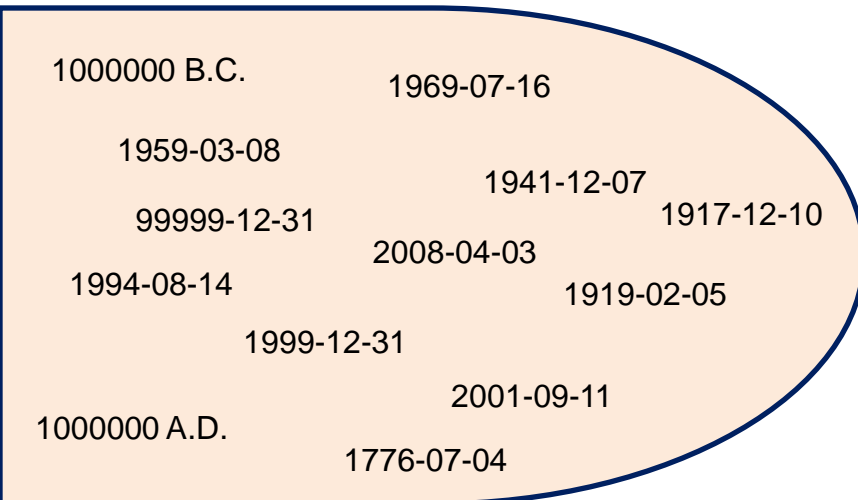
Globally Unique Values

2. Understanding Value Semantics

Why are unique values important?

Abstract *date* Type

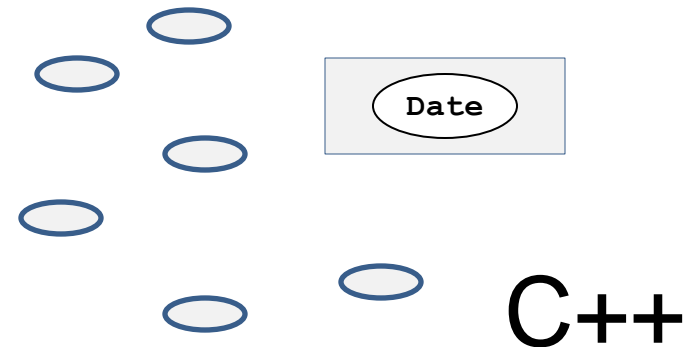
Has an infinite set of valid *date* values.



Globally Unique Values

C++ Date Class

Each instance refers to one of (a subset of) these abstract values.



2. Understanding Value Semantics

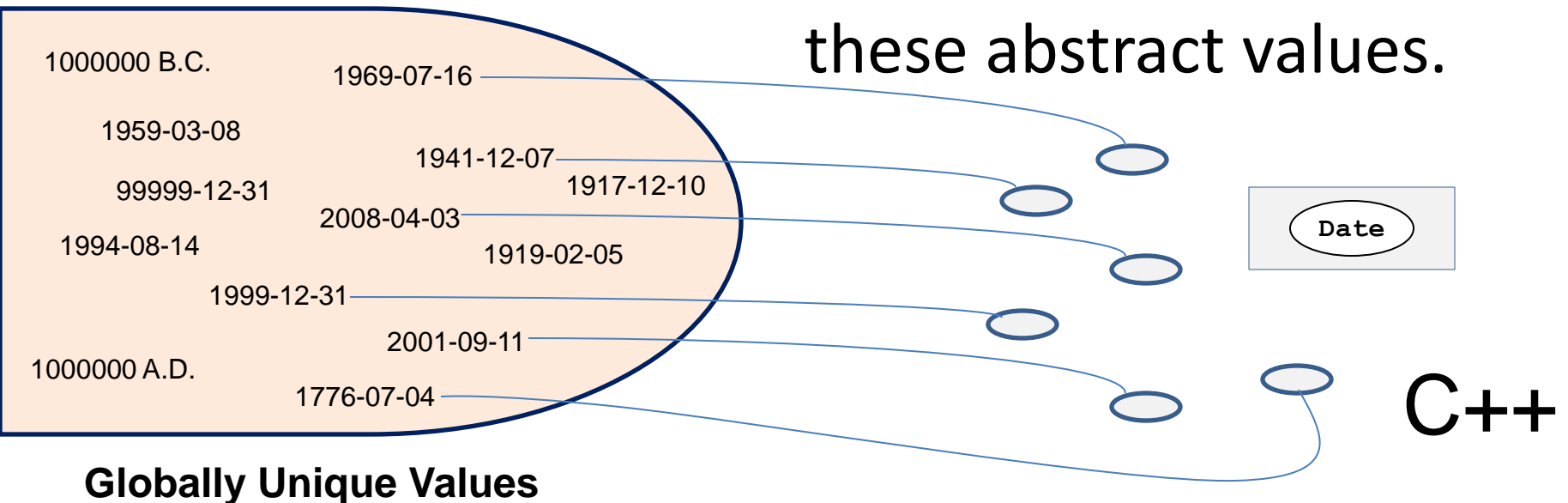
Why are unique values important?

Abstract *date* Type

Has an infinite set of valid *date* values.

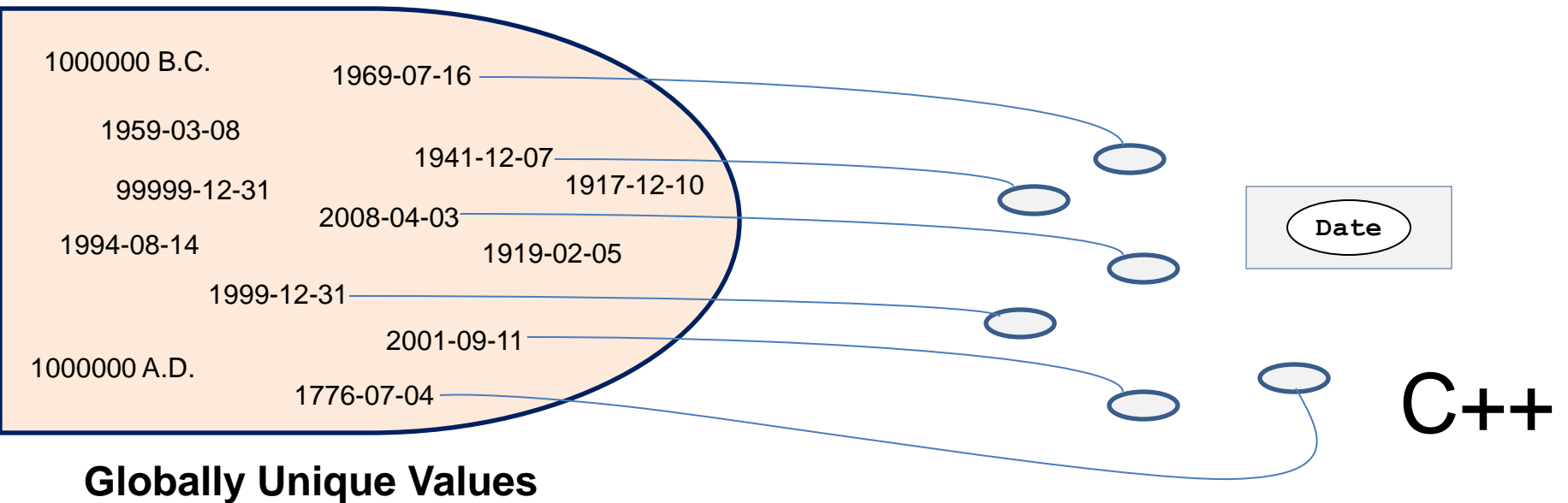
C++ Date Class

Each instance refers to one of (a subset of) these abstract values.



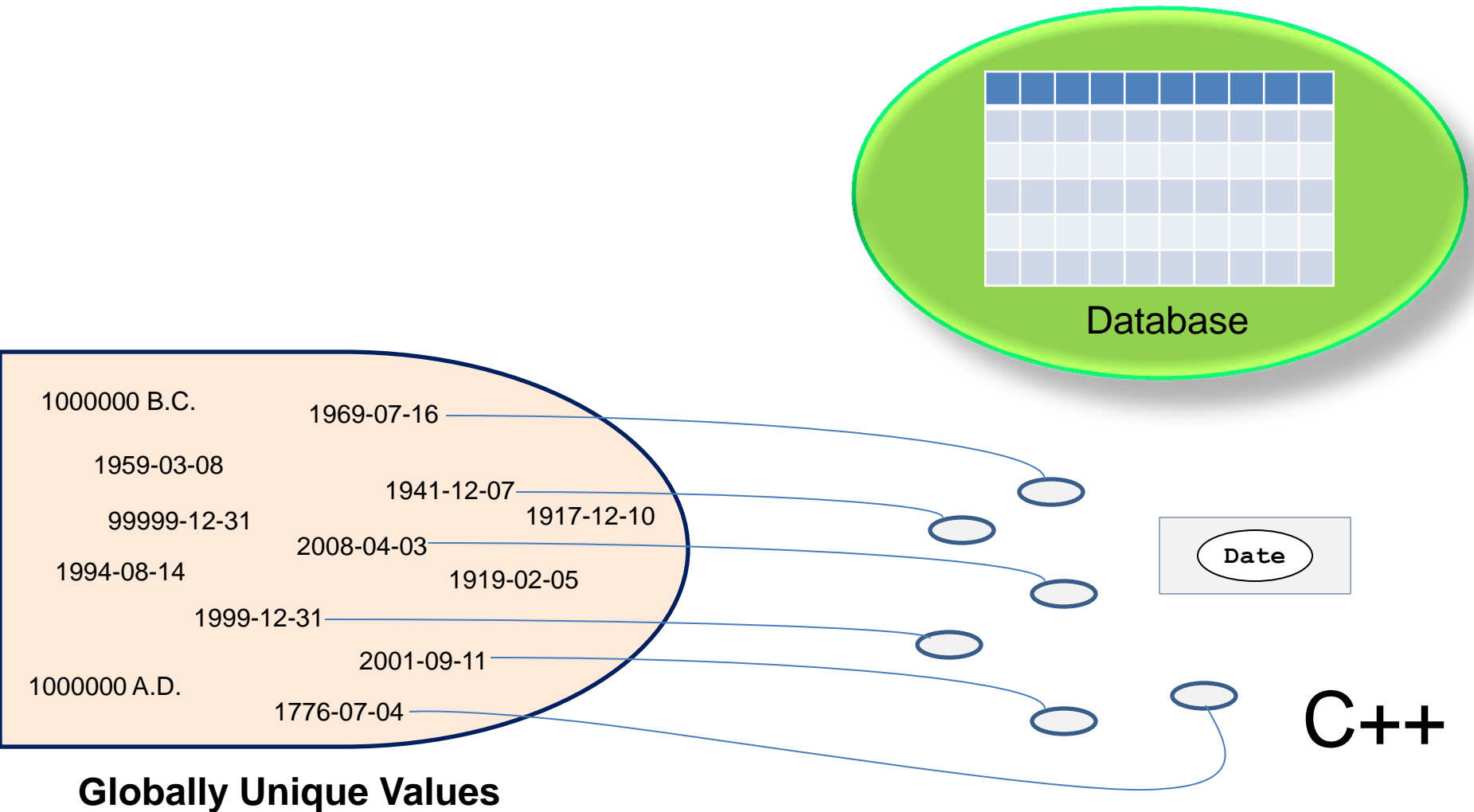
2. Understanding Value Semantics

Why are unique values important?



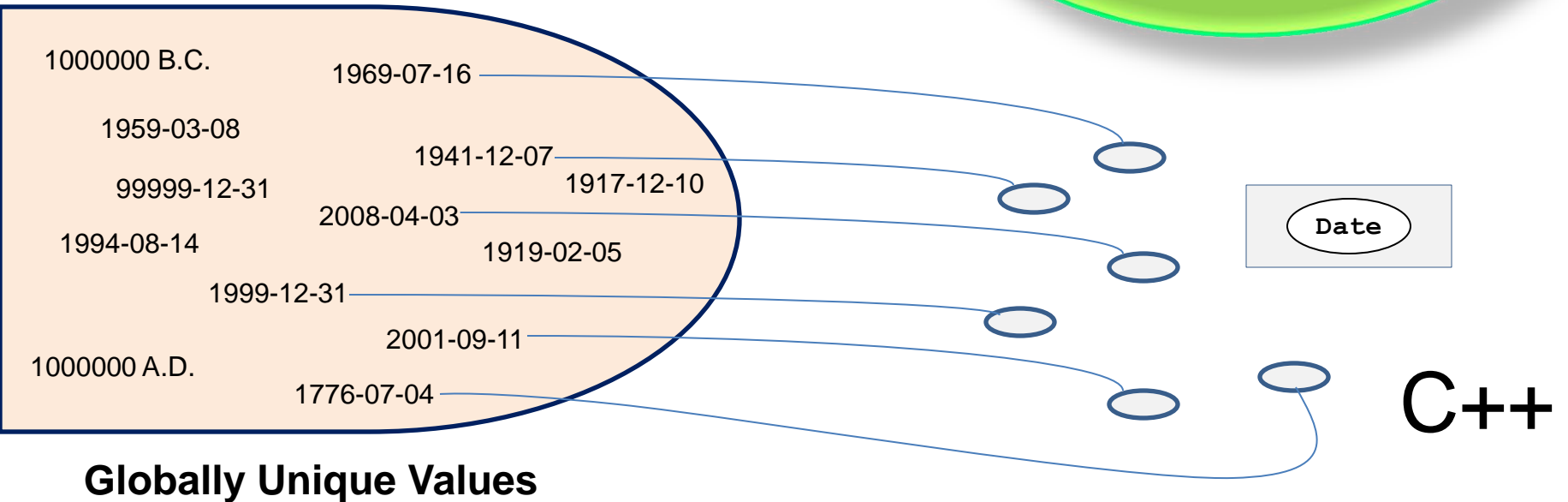
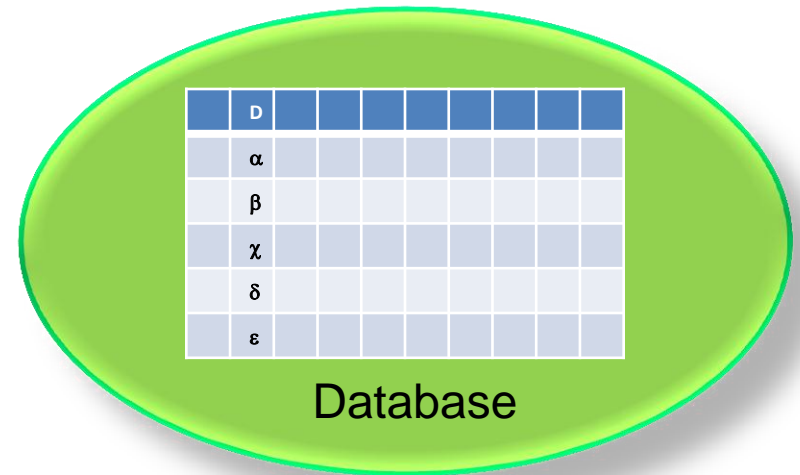
2. Understanding Value Semantics

Why are unique values important?



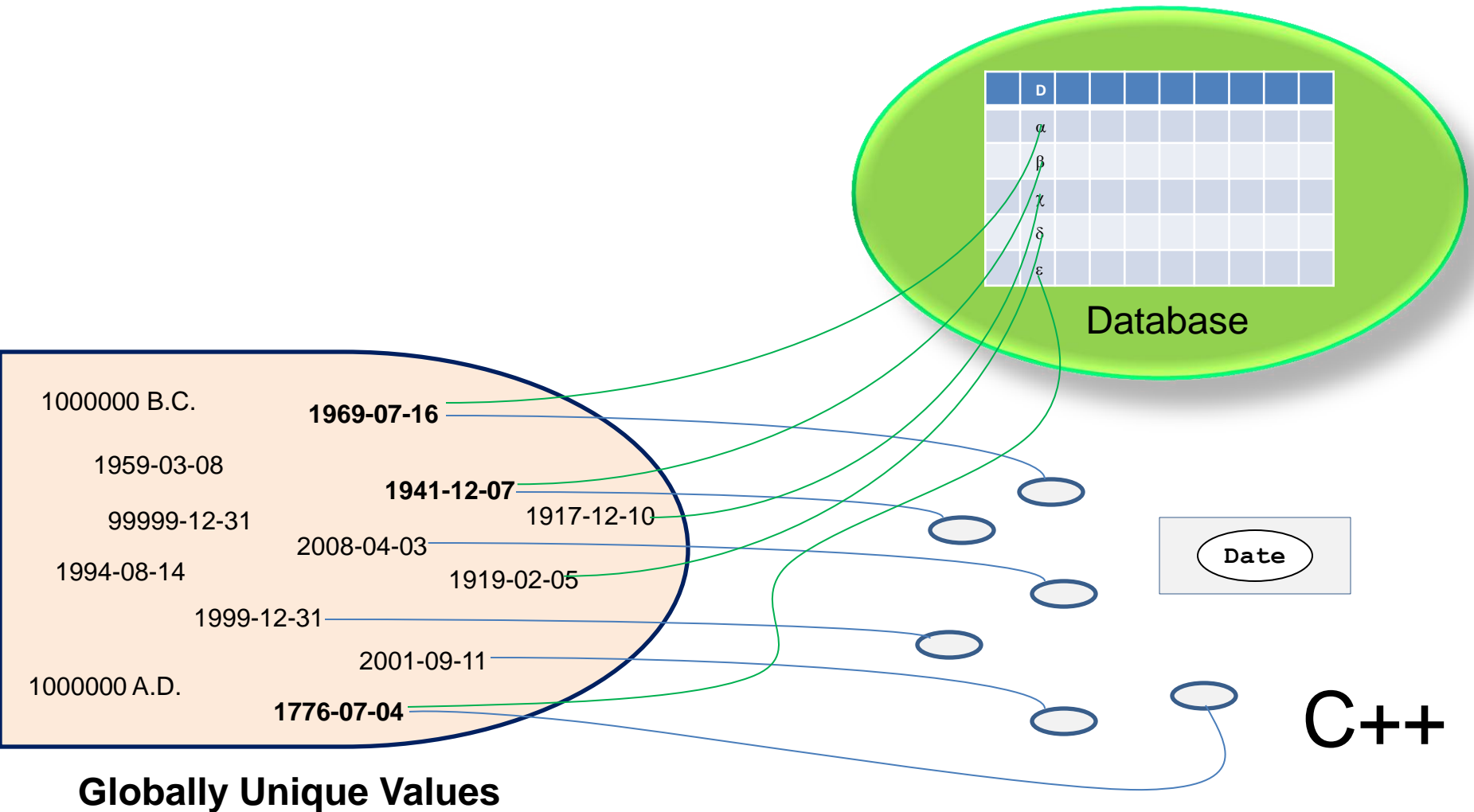
2. Understanding Value Semantics

Why are unique values important?



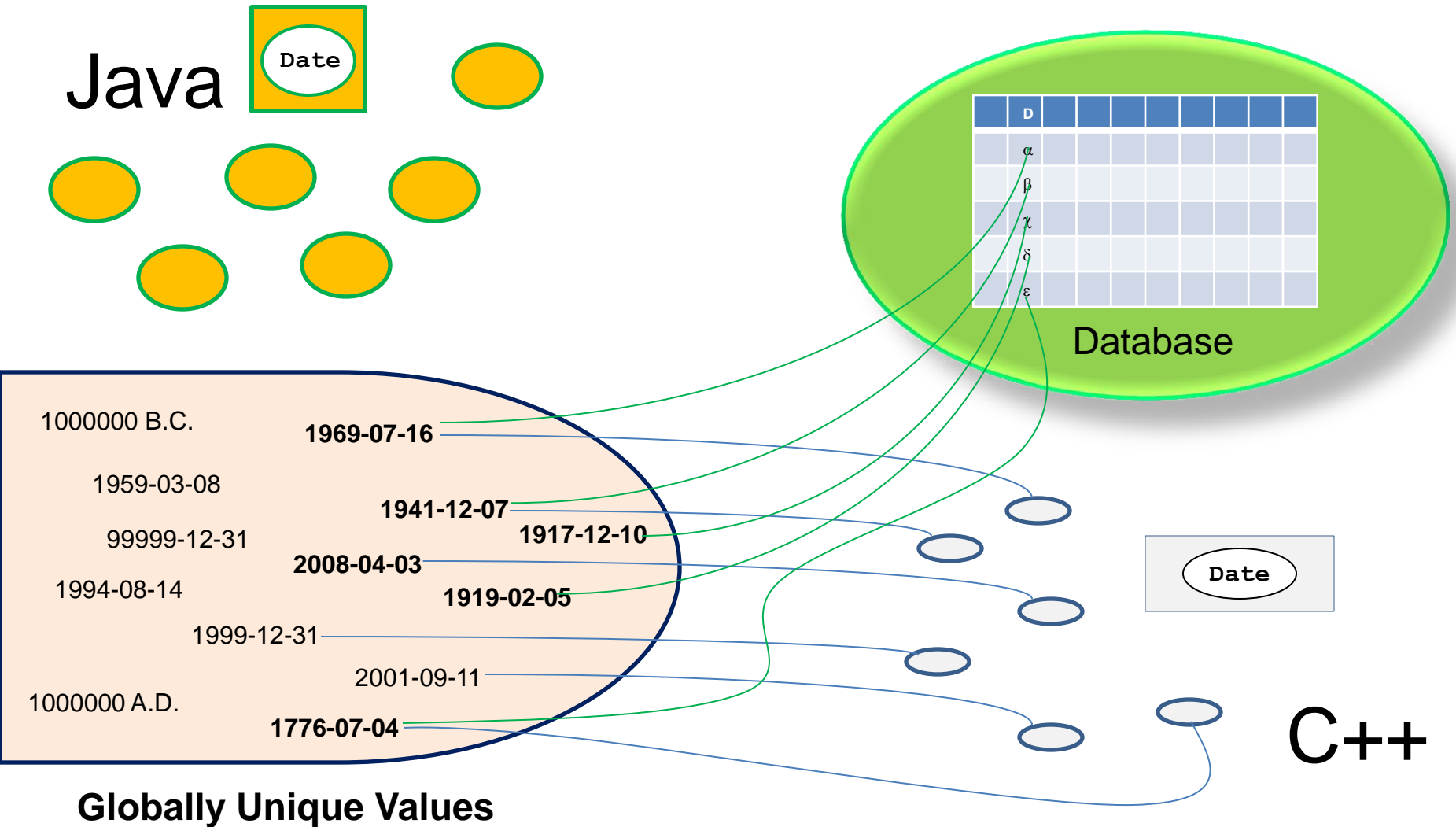
2. Understanding Value Semantics

Why are unique values important?



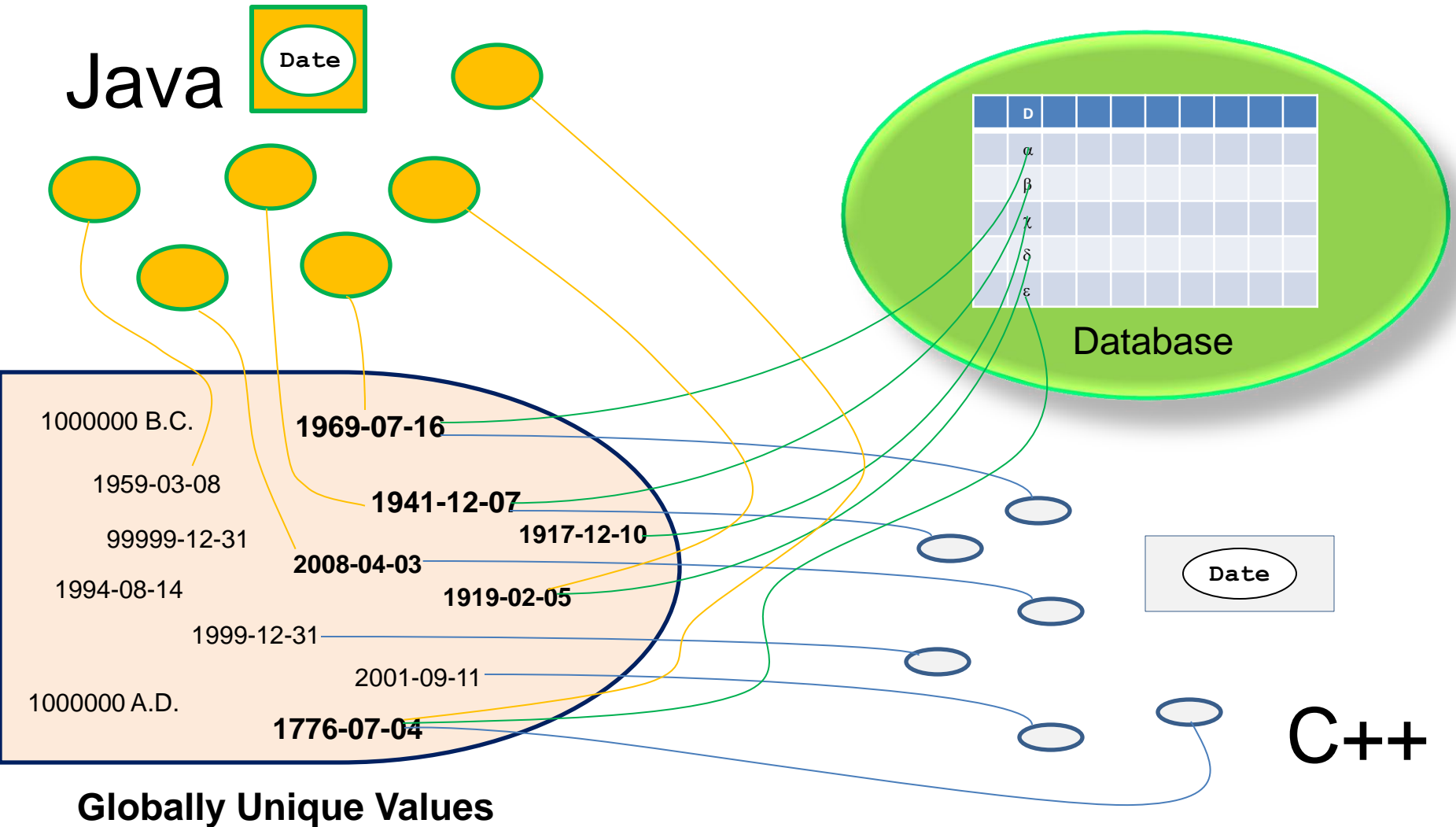
2. Understanding Value Semantics

Why are unique values important?



2. Understanding Value Semantics

Why are unique values important?



2. Understanding Value Semantics

Why are unique values important?

(Not *just* an academic exercise.)

2. Understanding Value Semantics

Why are unique values important?

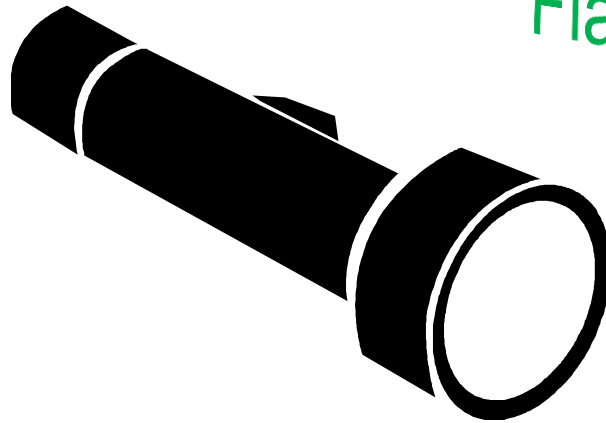
(Not *just* an academic exercise.)

When we communicate a value outside of a running process, we know that **everyone** is referring to “**the same**” value.

Which types
are naturally
value types?

2. Understanding Value Semantics

Does **state** *always* imply a “**value**”?



Flashlight Object

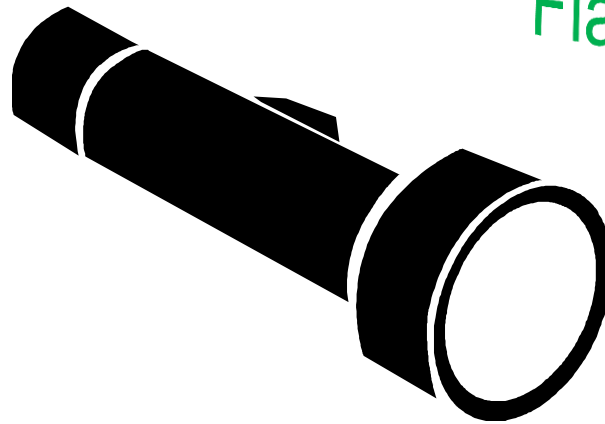
2. Understanding Value Semantics

Does **state** *always* imply a “**value**”?



2. Understanding Value Semantics

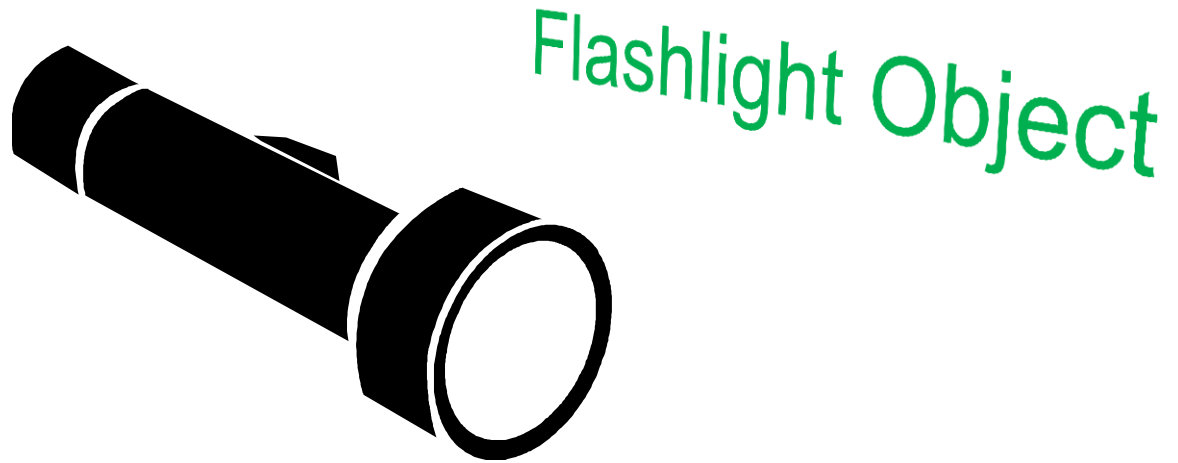
Does **state** *always* imply a “**value**”?



Flashlight Object

2. Understanding Value Semantics

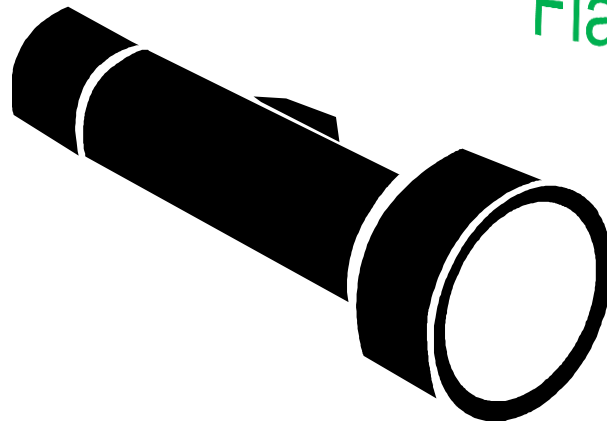
Does **state** *always* imply a “**value**”?



What is its state?

2. Understanding Value Semantics

Does **state** *always* imply a “**value**”?



Flashlight Object

What is its state? OFF

2. Understanding Value Semantics

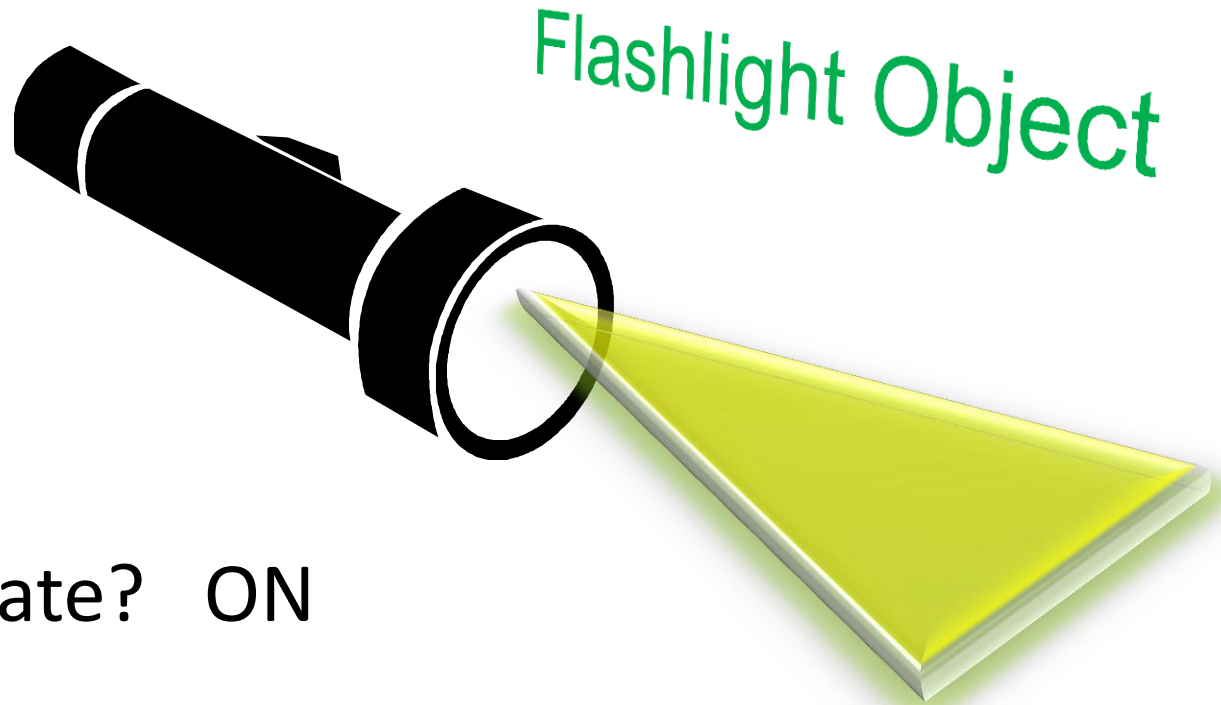
Does **state** *always* imply a “**value**”?



What is its state?

2. Understanding Value Semantics

Does **state** *always* imply a “**value**”?



What is its state? ON

2. Understanding Value Semantics

Does **state** *always* imply a “**value**”?

Flashlight Object

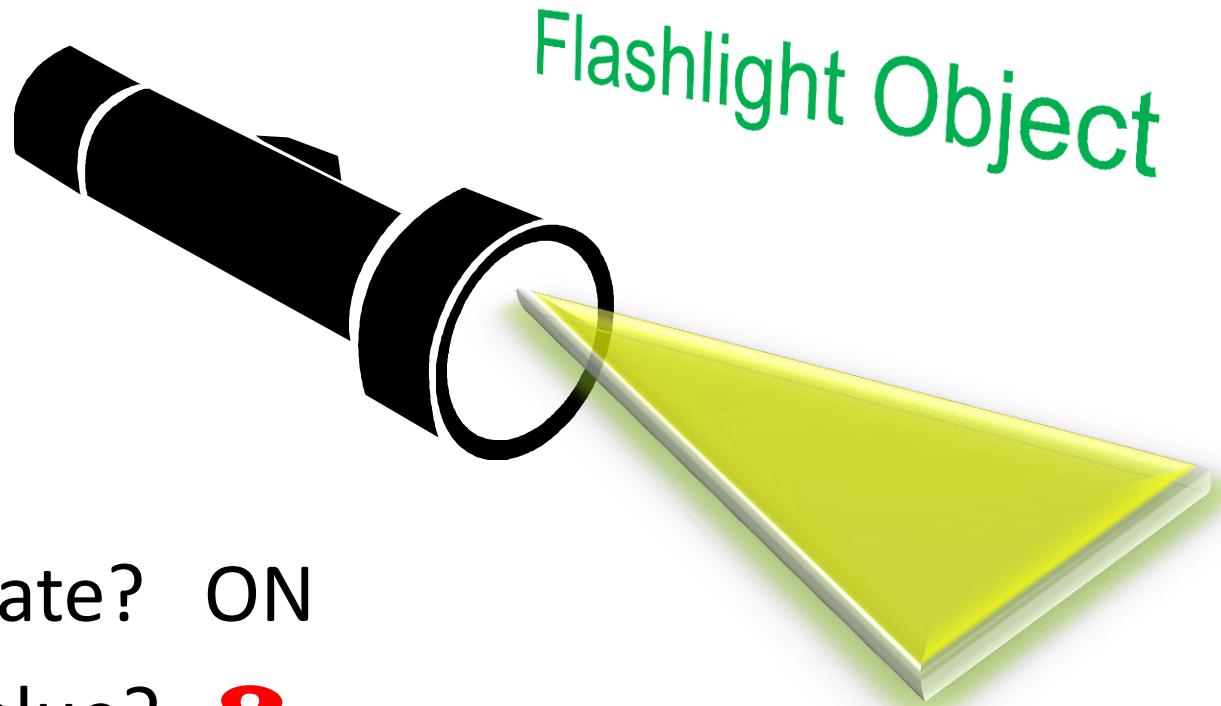


What is its state? ON

What is its value?

2. Understanding Value Semantics

Does **state** *always* imply a “**value**”?

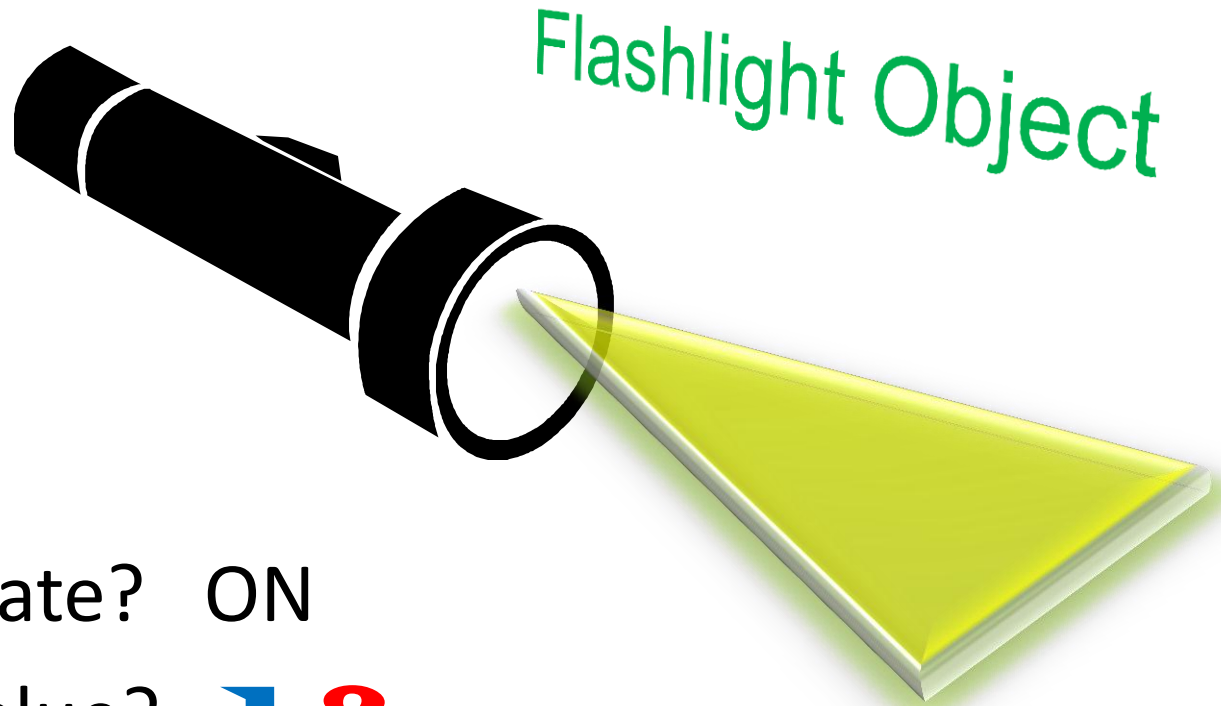


What is its state? ON

What is its value? ?

2. Understanding Value Semantics

Does **state** *always* imply a “**value**”?

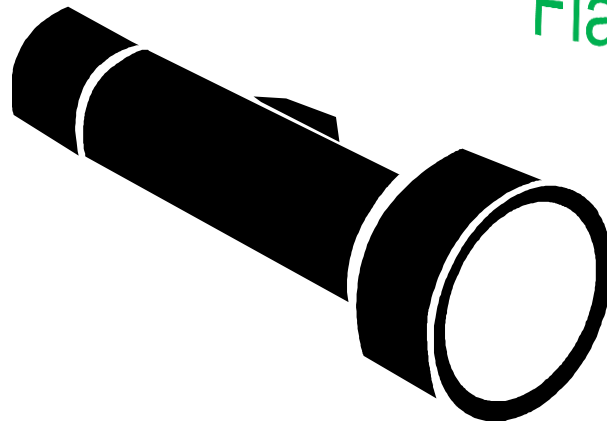


What is its state? ON

What is its value?  ?

2. Understanding Value Semantics

Does **state** *always* imply a “**value**”?



Flashlight Object

What is its state? ON

What is its value? **false** ?

2. Understanding Value Semantics

Does **state** *always* imply a “**value**”?



What is its state? ON

What is its value? **£5.00** ?

2. Understanding Value Semantics

Does **state** *always* imply a “**value**”?

Flashlight Object



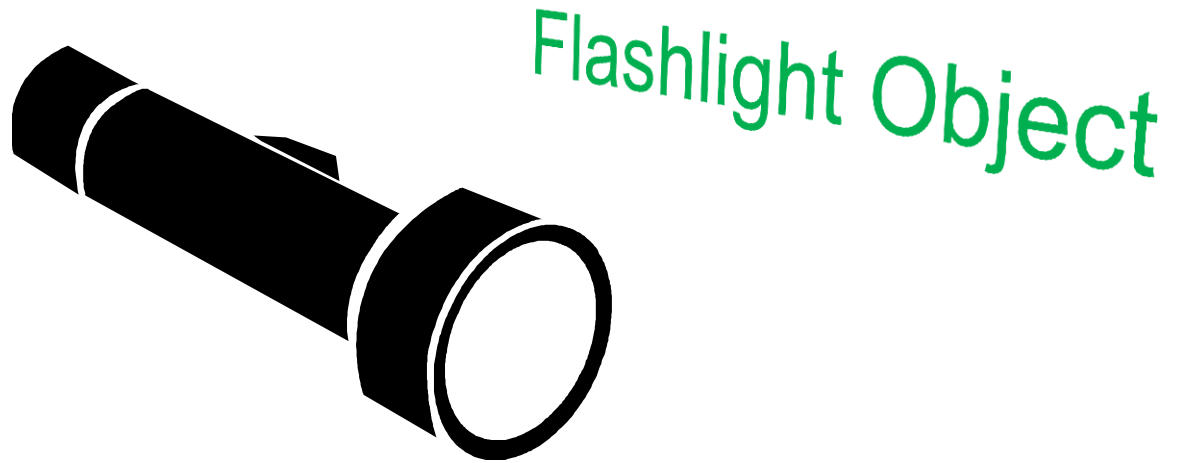
What is its state? ON

What is its value? **\$5.00** ?

Cheap at half
the price!

2. Understanding Value Semantics

Does **state** *always* imply a “**value**”?



What is its state? ON

What is its value? ?

Any notion of “value”
here would be artificial!

2. Understanding Value Semantics

Does **state** *always* imply a “**value**”?

Not every ***stateful*** object has an ***obvious*** value.

2. Understanding Value Semantics

Does **state** *always* imply a “**value**”?

Not every *stateful* object has an *obvious* value.

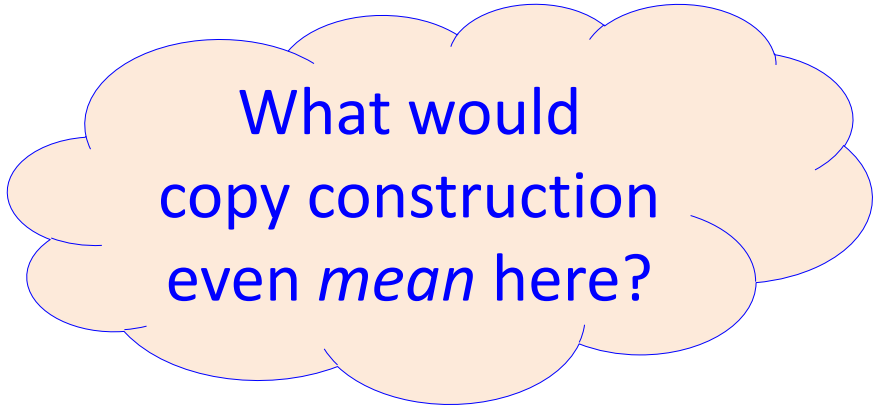
- TCP/IP Socket
- Thread Pool
- Condition Variable
- Mutex Lock
- Reader/Writer Lock
- Scoped Guard

2. Understanding Value Semantics

Does **state** *always* imply a “**value**”?

Not every *stateful* object has an *obvious* value.

- TCP/IP Socket
- Thread Pool ○ ○ ○
- Condition Variable
- Mutex Lock
- Reader/Writer Lock
- Scoped Guard



What would
copy construction
even *mean* here?

2. Understanding Value Semantics

Does **state** *always* imply a “**value**”?

Not every *stateful* object has an *obvious* value.

- TCP/IP Socket
- Thread Pool ○ ○ ○
- Condition Variable
- Mutex Lock
- Reader/Writer Lock
- Scoped Guard ○ ○ ○

What would
copy construction
even *mean* here?

We could *invent*
some notion of value,
but to what end??

2. Understanding Value Semantics

Does **state** *always* imply a “**value**”?

Not every *stateful* object has an *obvious* value.

- TCP/IP Socket
- Thread Pool
- Condition Variable
- Mutex Lock
- Reader/Writer Lock
- Scoped Guard
- Base64 En(De)coder
- Expression Evaluator
- Language Parser
- Event Logger
- Object Persistor
- Widget Factory

2. Understanding Value Semantics

Does **state** *always* imply a “**value**”?

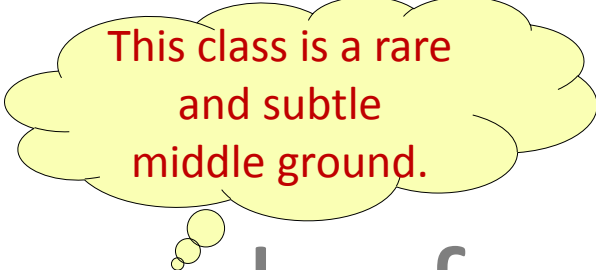
QUESTION:

Suppose we have a thread-safe queue used for inter-task communication: Is it a value type?

2. Understanding Value Semantics

Does **state** *always* imply a “**value**”?

QUESTION:



This class is a rare
and subtle
middle ground.

Suppose we have a thread-safe queue used for inter-task communication: Is it a value type? Should this object type support value-semantic syntax?

2. Understanding Value Semantics

Does **state** *always* imply a “**value**”?

We refer to *stateful* objects that do not represent a value as “**Mechanisms**”.

The Big Picture

Common Category

zo::Loader



2. Understanding Value Semantics

Categorizing Object Types



MyObjectType

2. Understanding Value Semantics

Categorizing Object Types

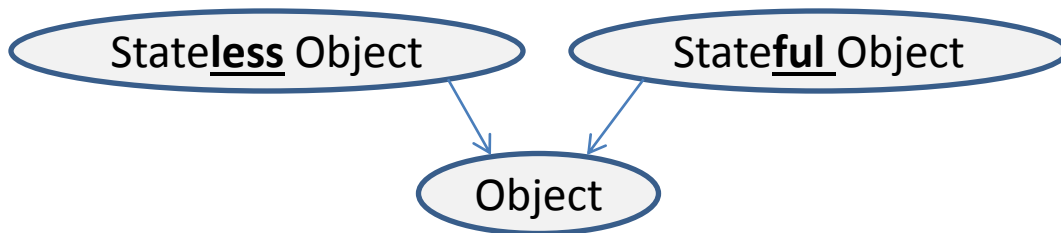
The first question: “Does it have state?”



2. Understanding Value Semantics

Categorizing Object Types

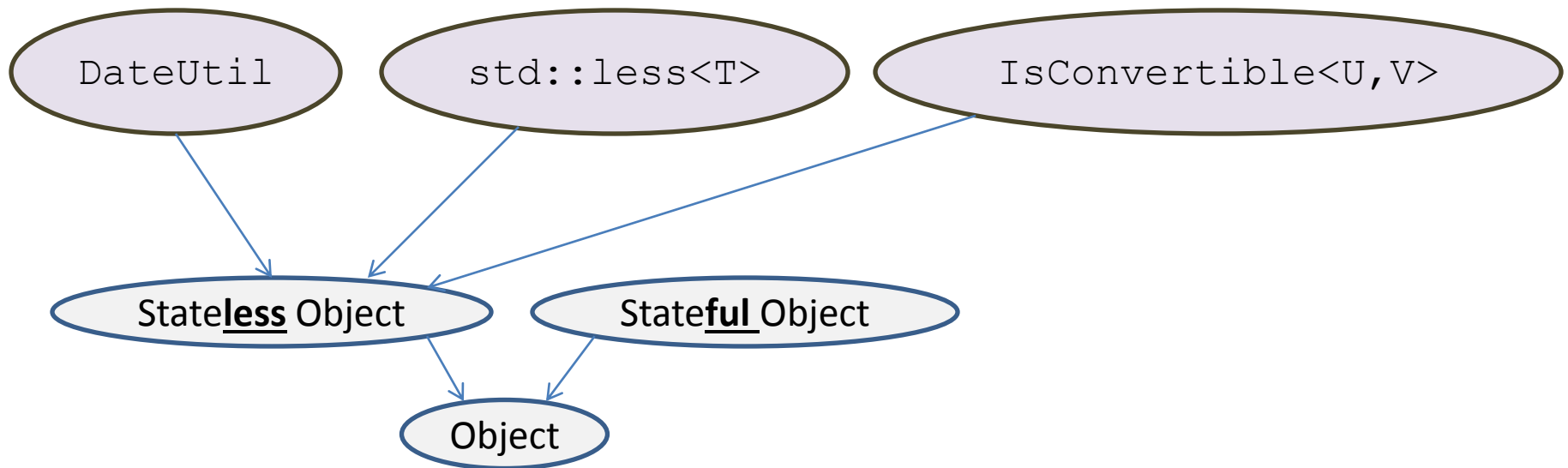
The first question: “Does it have state?”



2. Understanding Value Semantics

Categorizing Object Types

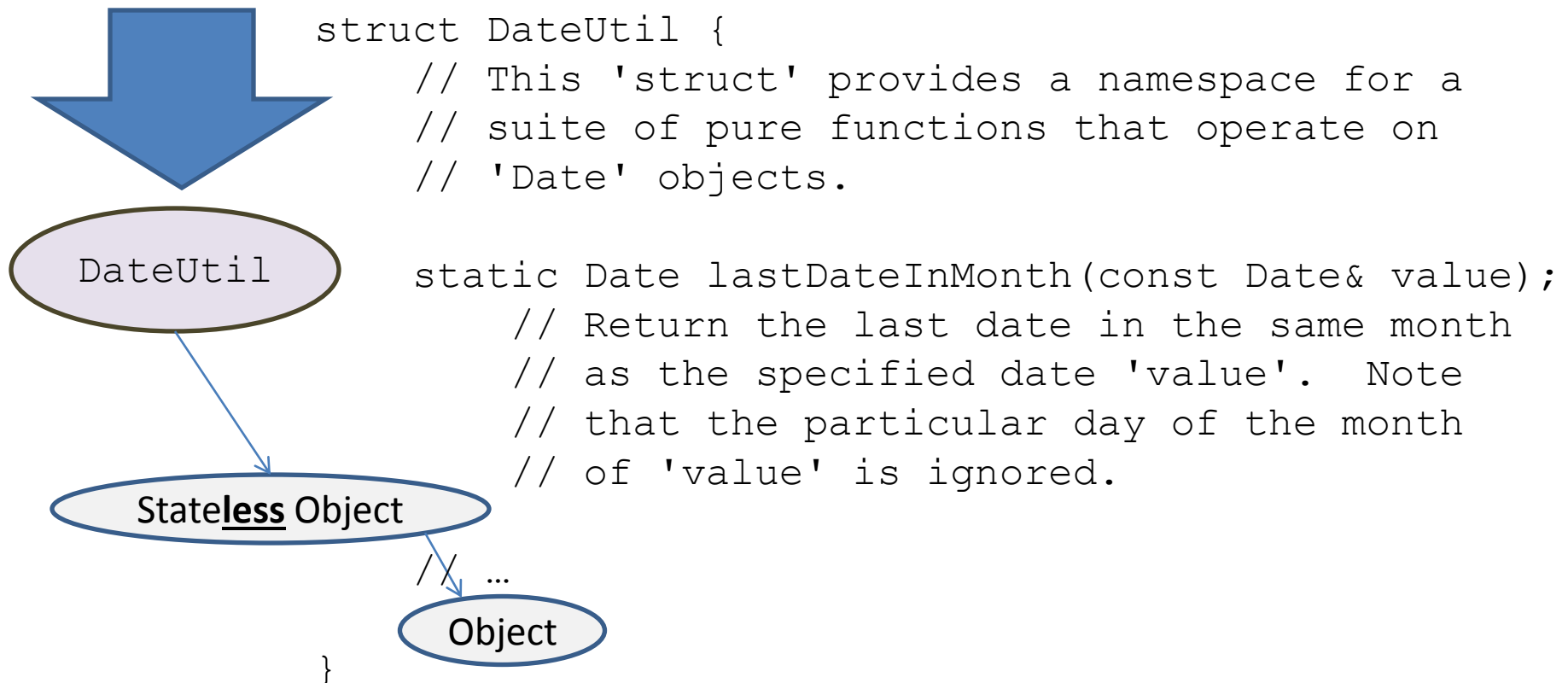
The first question: “Does it have state?”



2. Understanding Value Semantics

Categorizing Object Types

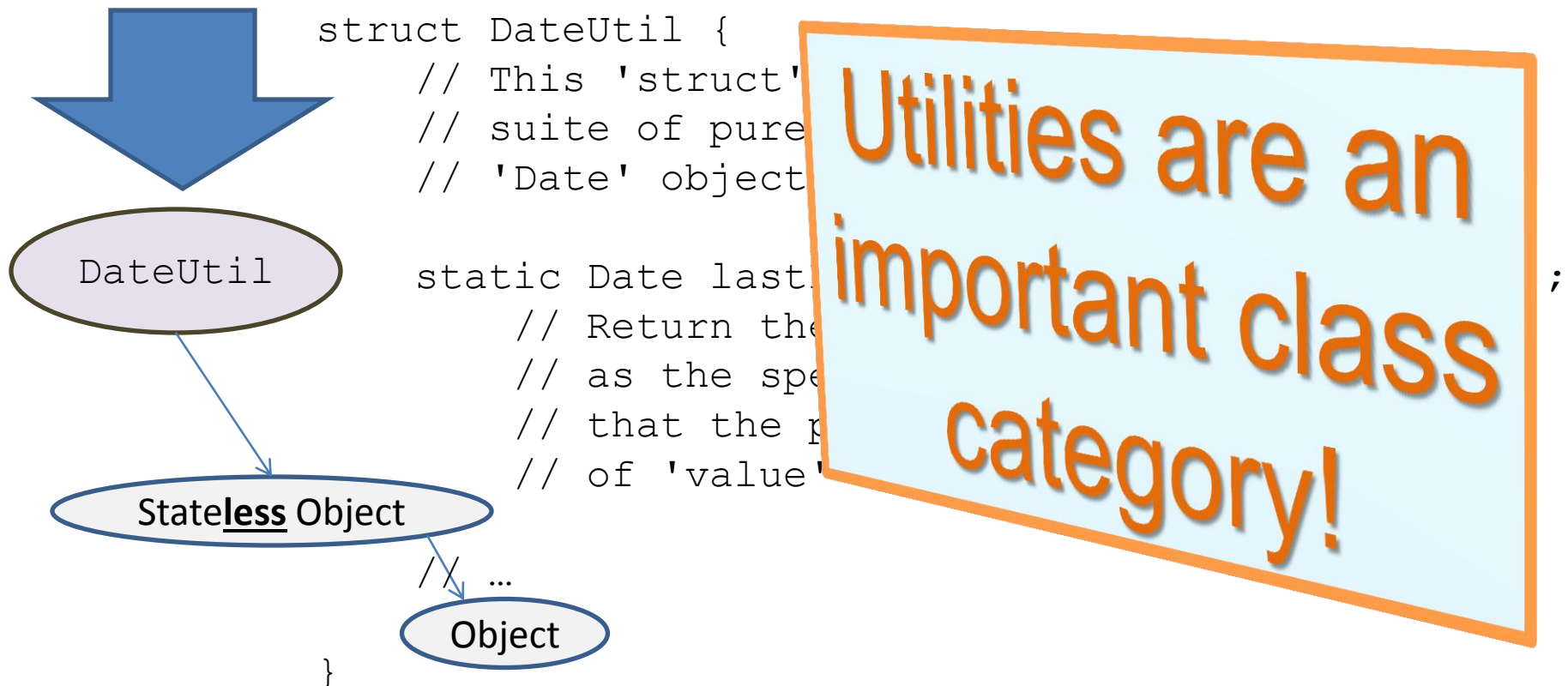
The first question: “Does it have state?”



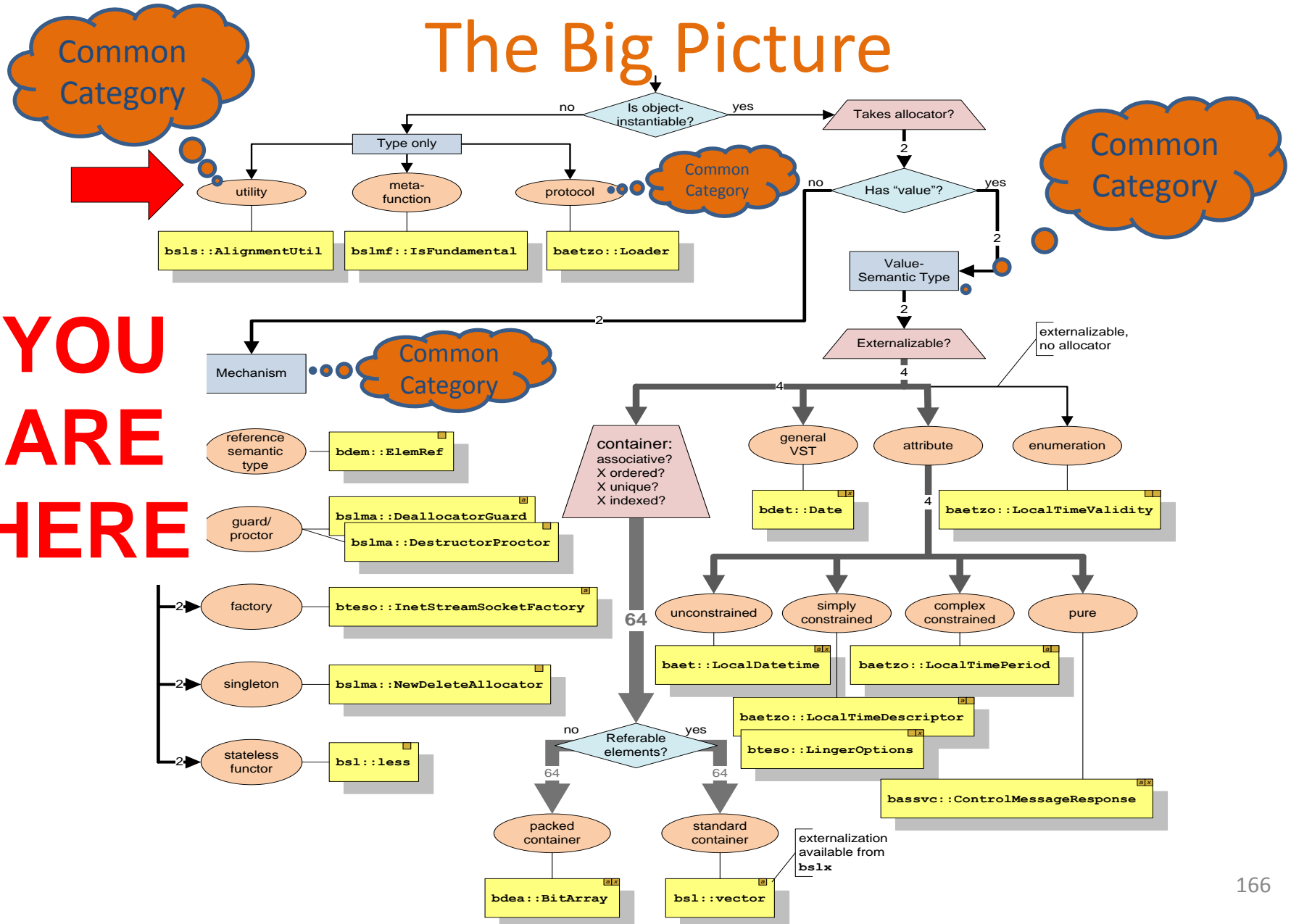
2. Understanding Value Semantics

Categorizing Object Types

The first question: “Does it have state?”



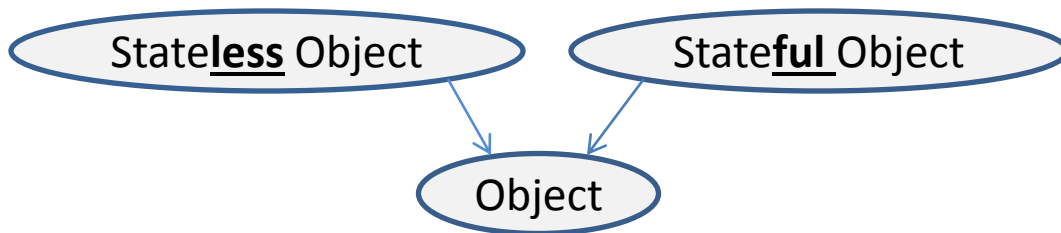
The Big Picture



2. Understanding Value Semantics

Categorizing Object Types

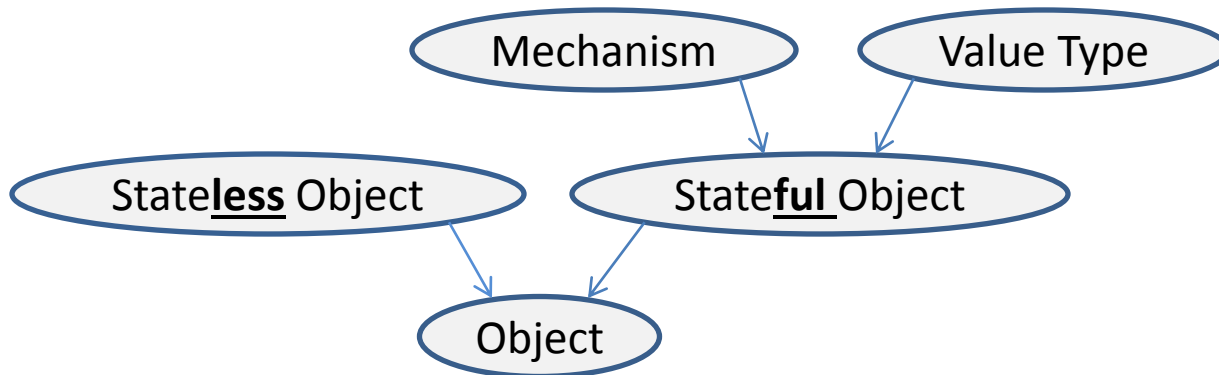
The second question: “Does it have value?”



2. Understanding Value Semantics

Categorizing Object Types

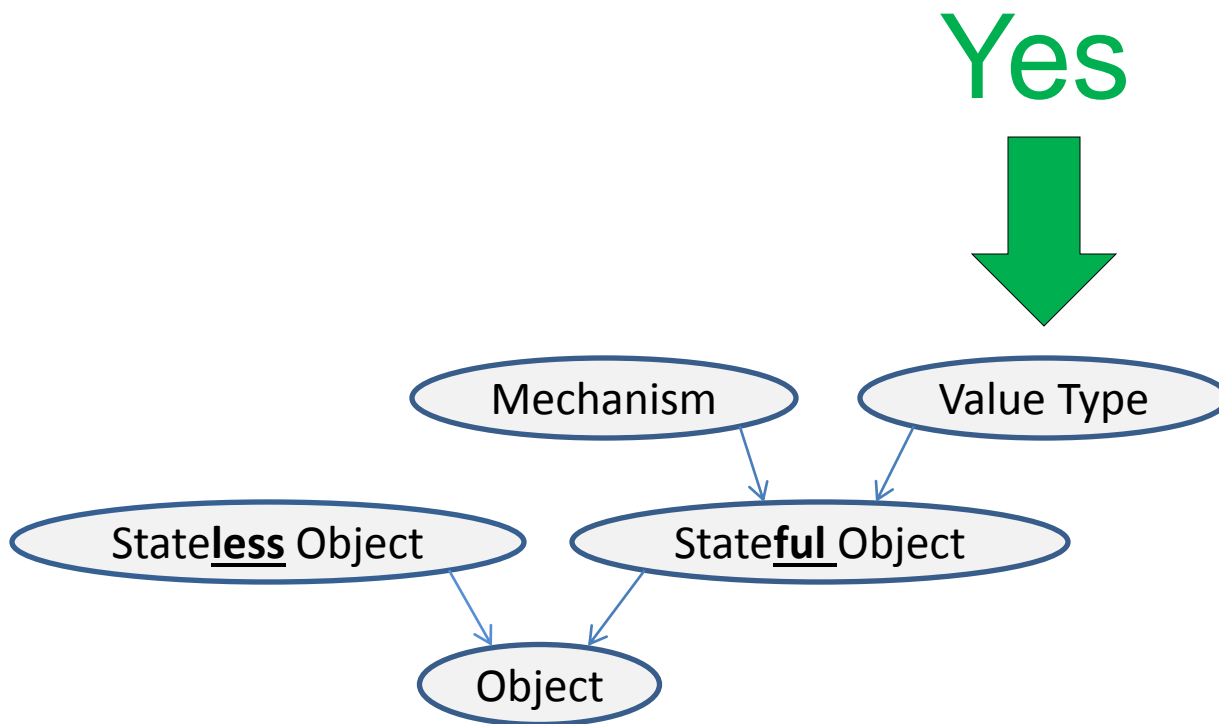
The second question: “Does it have value?”



2. Understanding Value Semantics

Categorizing Object Types

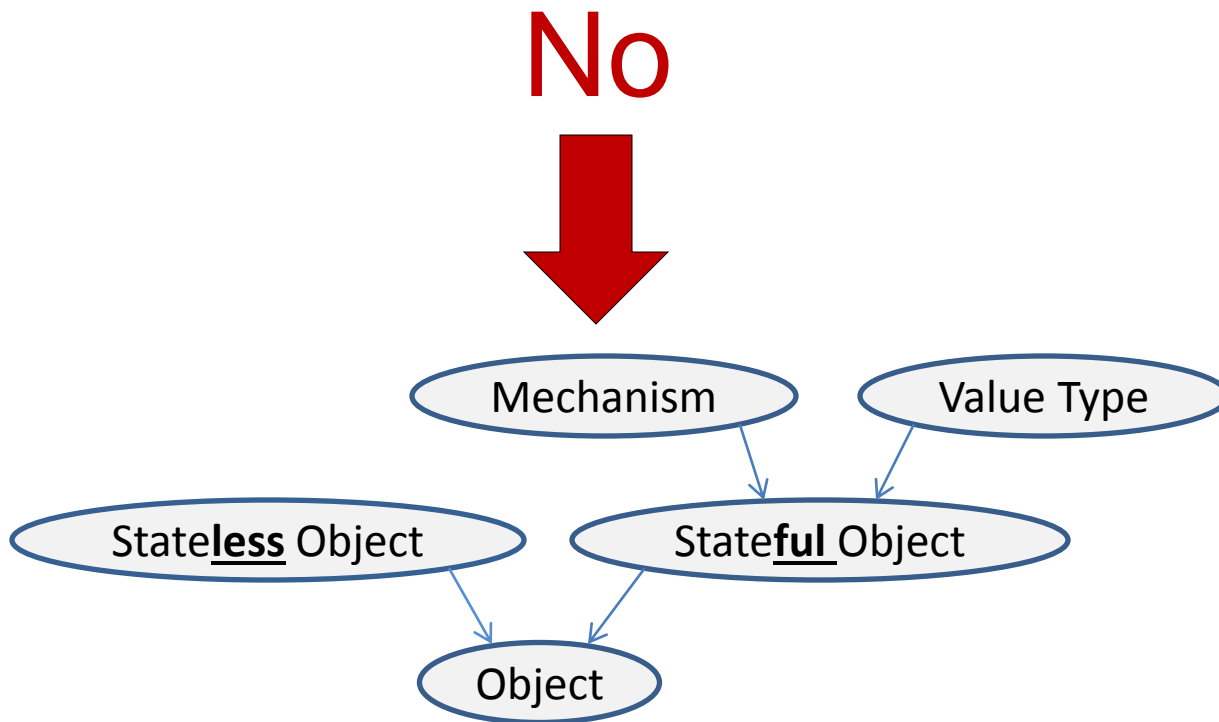
The second question: “Does it have value?”



2. Understanding Value Semantics

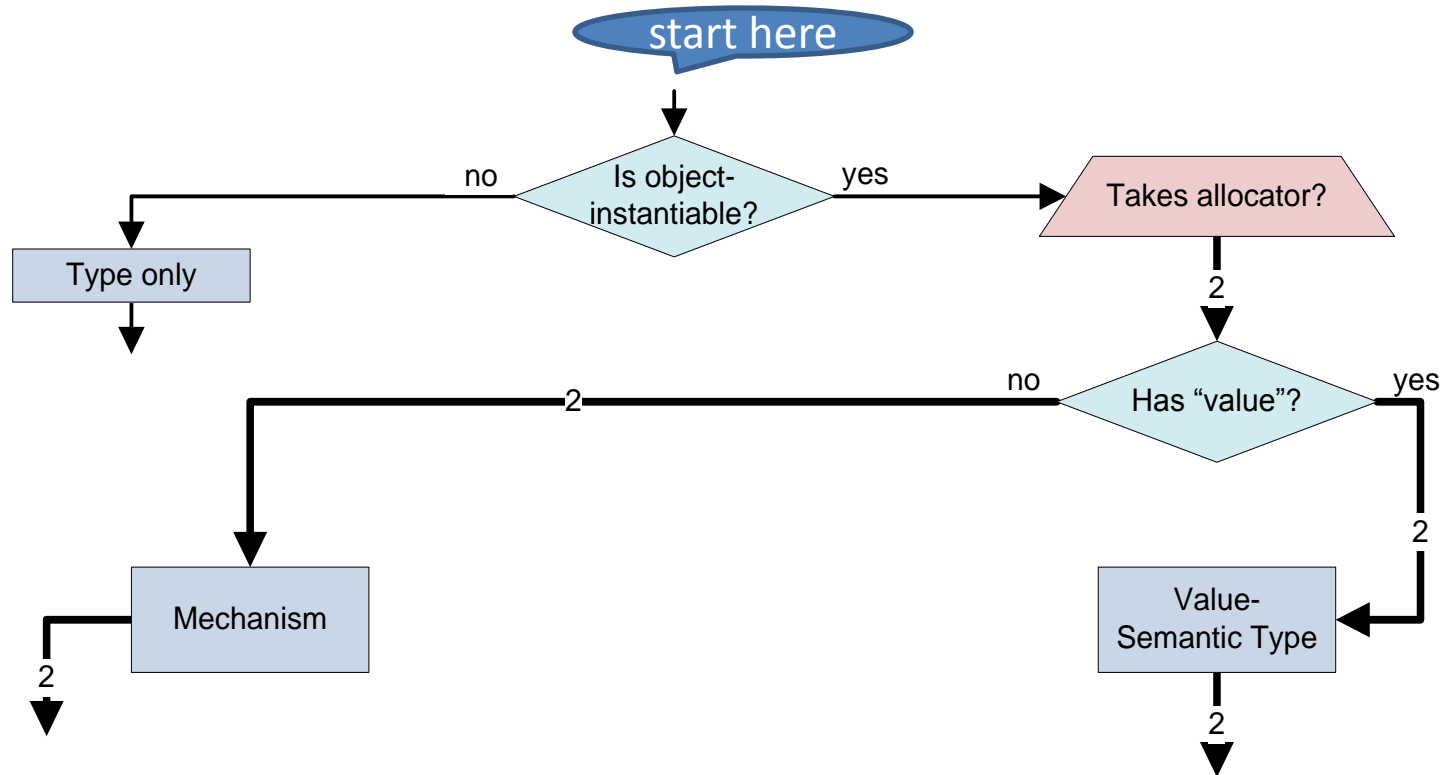
Categorizing Object Types

The second question: “Does it have value?”



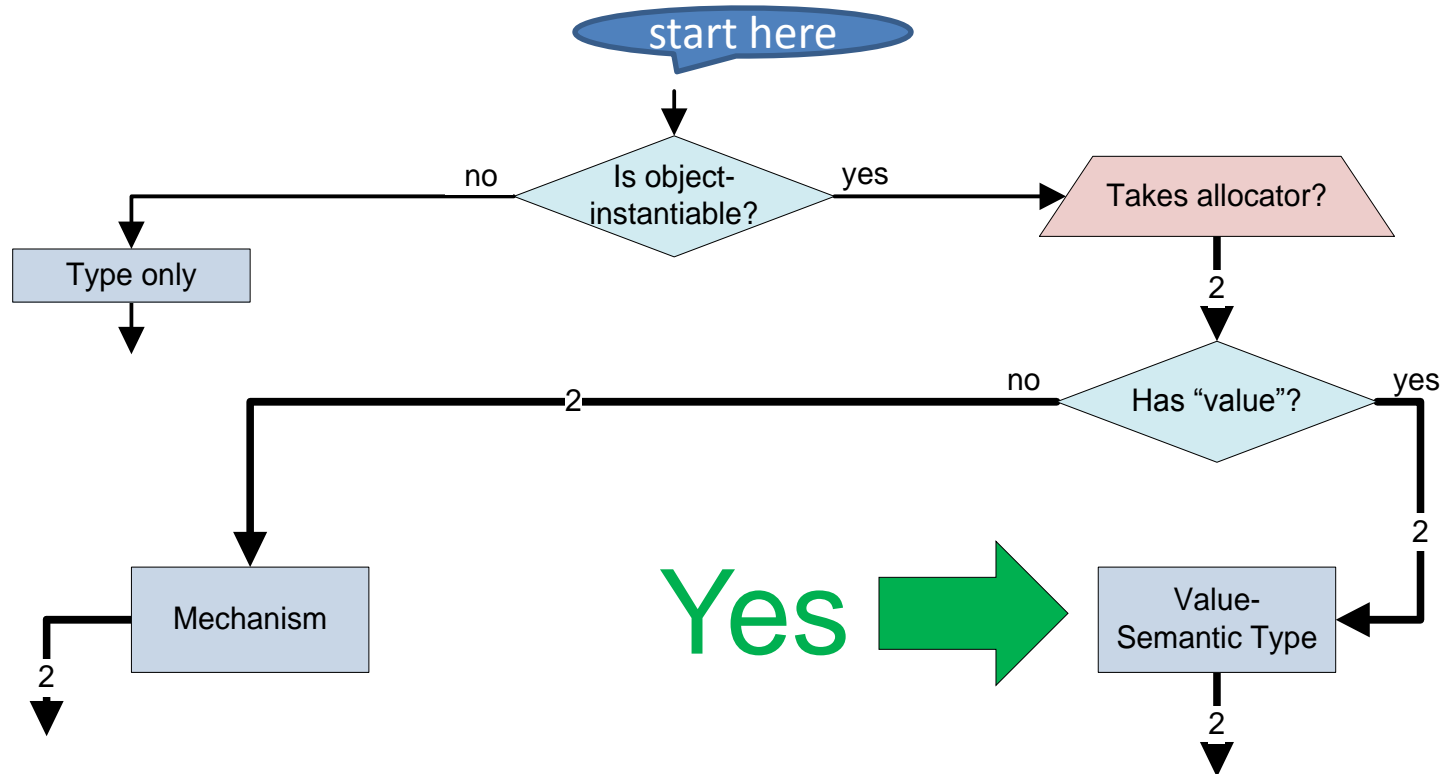
2. Understanding Value Semantics

Top-Level Categorizations



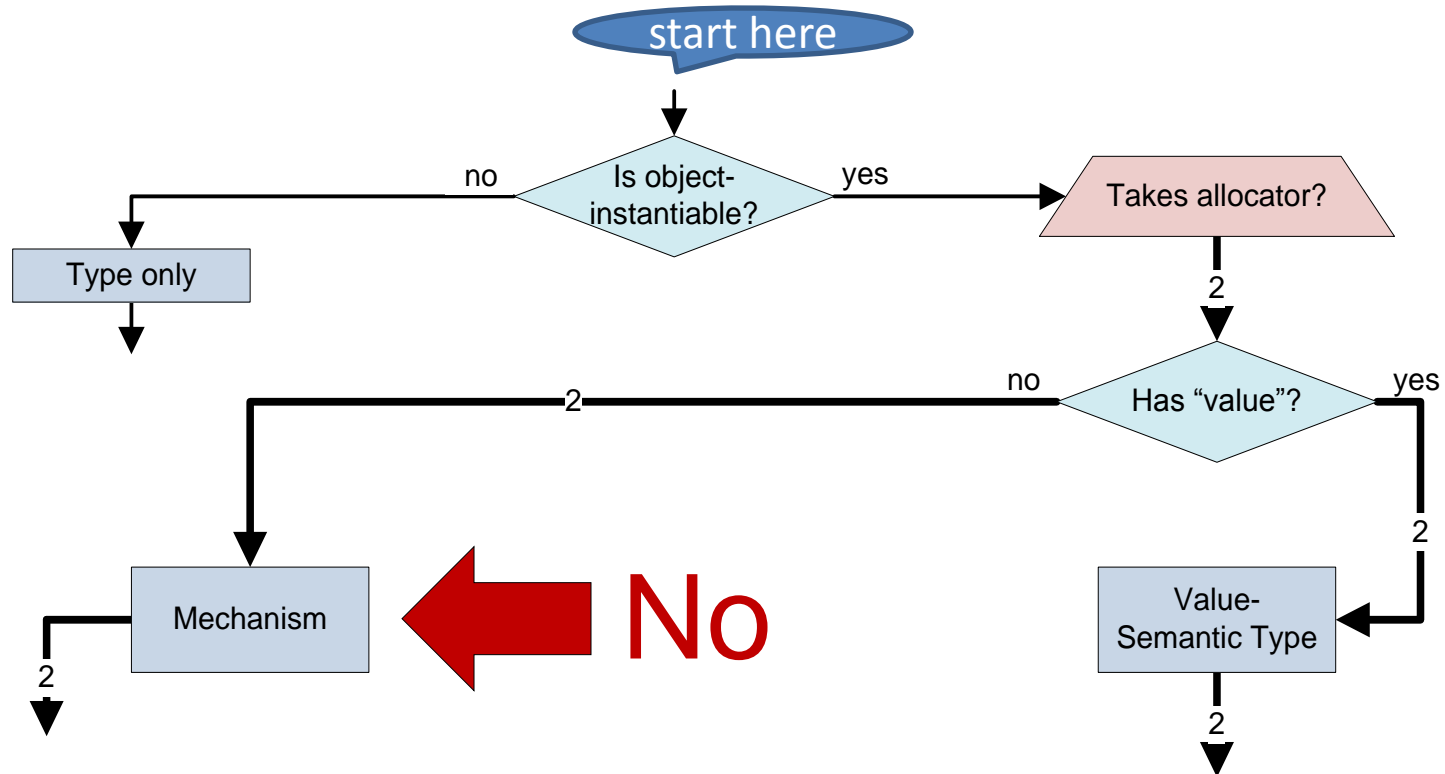
2. Understanding Value Semantics

Top-Level Categorizations



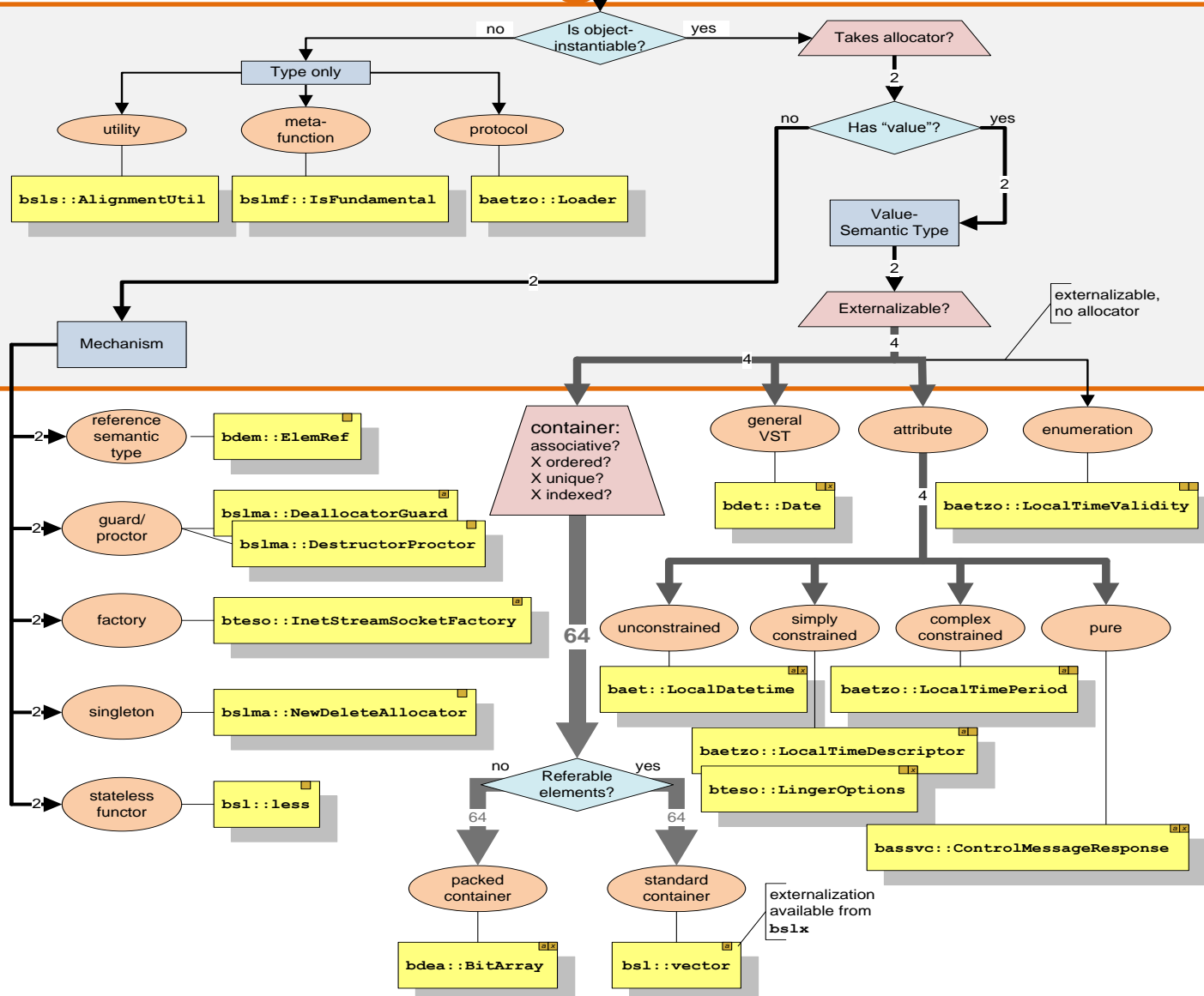
2. Understanding Value Semantics

Top-Level Categorizations



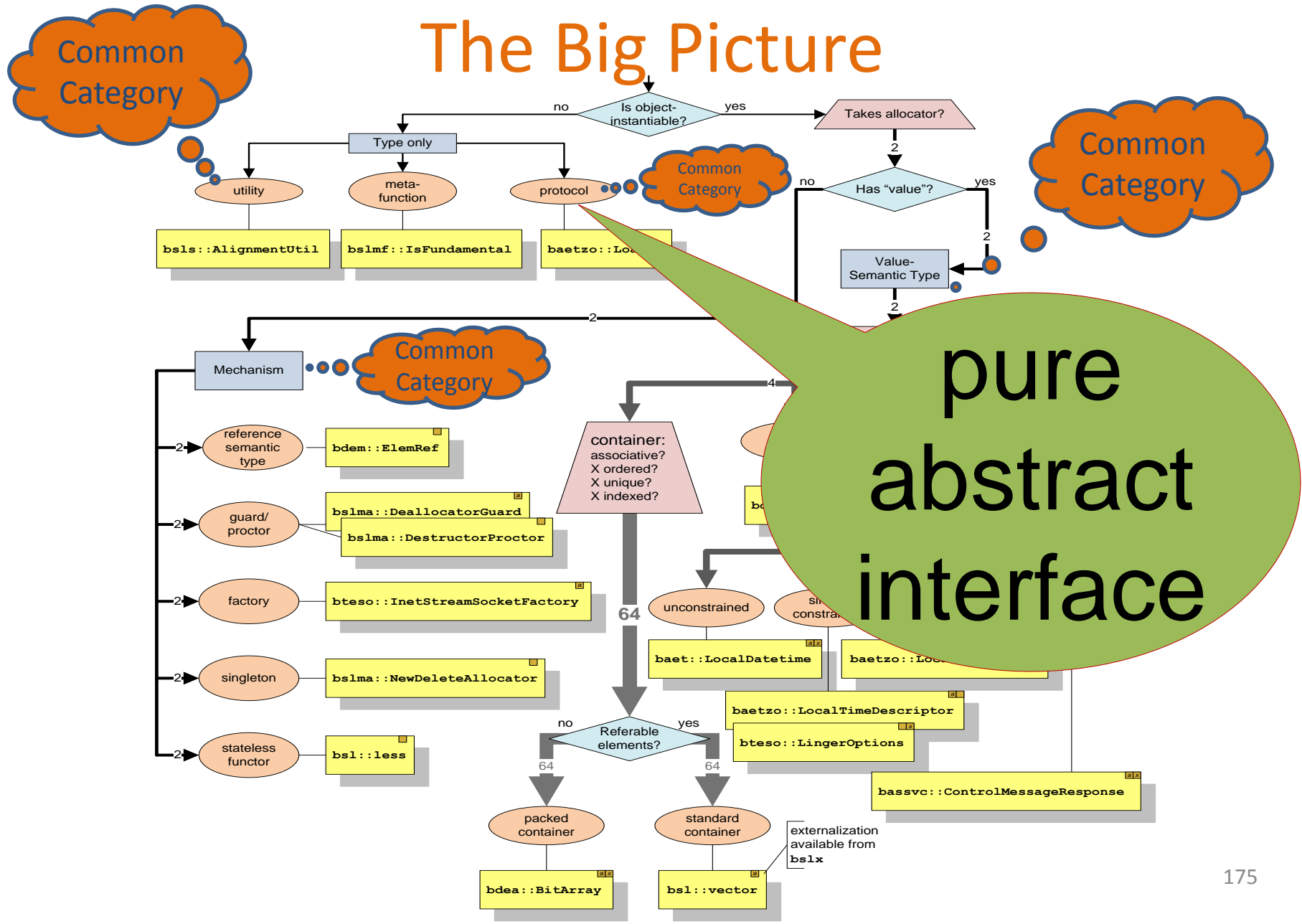
2. Understanding Value Semantics

The Big Picture



2. Understanding Value Semantics

The Big Picture



2. Understanding Value Semantics

The Big Picture

QUESTION:

What does it mean for two abstract types to compare equal?

2. Understanding Value Semantics

The Big Picture

QUESTION:

~~What does it mean for two
abstract types to compare equal?~~

2. Understanding Value Semantics

The Big Picture

QUESTION:

~~What does it mean for two
abstract types to compare equal?~~

Data members are for:

“Variation in Value”

—Tom Cargill (c. 1992)

What syntax
should value
types have?

2. Understanding Value Semantics

Value-Semantic Properties

A value-semantic type T defines the following:

2. Understanding Value Semantics

Value-Semantic Properties

A *value-semantic* type T defines the following:

- Default construction: $T \text{ } \mathbf{a}, \mathbf{b}; \quad \text{assert}(\mathbf{a} == \mathbf{b});$

2. Understanding Value Semantics

Value-Semantic Properties

A *value-semantic* type T defines equality by:

Typically, but
not necessarily
(e.g., `int`)

- Default construction: `T a, b; assert(a == b);`

2. Understanding Value Semantics

Value-Semantic Properties

A *value-semantic* type T defines equality by:

Typically, but
not necessarily
(e.g., `int`)

- Default construction: `T a, b; assert(a == b);`

However “zero” initialization
`assert(T() == T());`
Is true

2. Understanding Value Semantics

Value-Semantic Properties

A *value-semantic* type T defines the following:

- Default construction: `T a, b; assert(a == b);`
- Copy construction: `T a, b(a); assert(a == b);`

2. Understanding Value Semantics

Value-Semantic Properties

A *value-semantic* type T defines the following:

- Default construction: $T\ a, b;$ $\text{assert}(a == b);$
- Copy construction: $T\ a, b(a);$ $\text{assert}(a == b);$
- Destruction: *(Release all resources.)*

2. Understanding Value Semantics

Value-Semantic Properties

A *value-semantic* type T defines the following:

- Default construction: $T\ a, b;$ $\text{assert}(a == b);$
- Copy construction: $T\ a, b(a);$ $\text{assert}(a == b);$
- Destruction: *(Release all resources.)*
- Copy assignment: $a = b;$ $\text{assert}(a == b);$

2. Understanding Value Semantics

Value-Semantic Properties

A *value-semantic* type T defines the following:

- Default construction: $T \mathbf{a}, \mathbf{b}; \quad \text{assert}(\mathbf{a} == \mathbf{b});$
- Copy construction: $T \mathbf{a}, \mathbf{b}(\mathbf{a}); \quad \text{assert}(\mathbf{a} == \mathbf{b});$
- Destruction: *(Release all resources.)*
- Copy assignment: $\mathbf{a} = \mathbf{b}; \quad \text{assert}(\mathbf{a} == \mathbf{b});$
- Swap (if well-formed): $T \mathbf{a}(\alpha), \mathbf{b}(\beta); \quad \text{swap}(\mathbf{a}, \mathbf{b});$
 $\text{assert}(\beta == \mathbf{a});$
 $\text{assert}(\alpha == \mathbf{b});$

2. Understanding Value Semantics

Value-Semantic Properties

A *value-semantic* type T defines the following:

- Default construction: $T\ a\ b;$

- Copy constructor:

“Regular Type”

- Swap (if well-formed): $T\ a(\alpha),\ b(\beta);$ swap(a, b);
assert($\beta == a$);
assert($\alpha == b$);

2. Understanding Value Semantics

Value-Semantic Properties

`operator==(T, T)` describes what's called an *equivalence relation*:

1. $a == a$ (reflexive)
2. $a == b \Leftrightarrow b == a$ (symmetric)
3. $a == b \ \&\& \ b == c \Rightarrow a == c$ (transitive)

2. Understanding Value Semantics

Value-Semantic Properties

`operator==` (`T`, `T`) describes what's called an *equivalence relation*:

1. $a == a$ (reflexive)
 2. $a == b \Leftrightarrow b == a$ (symmetric)
 3. $a == b \ \&\& \ b == c \Rightarrow a == c$ (transitive)
- $! (a == b) \Leftrightarrow a != b$

2. Understanding Value Semantics


Value-Semantic Properties

`operator==(T, T)` describes what's called an *equivalence relation*:

1. $a == a$ (reflexive)
 2. $a == b \Leftrightarrow b == a$ (symmetric)
 3. $a == b \ \&\& \ b == c \Rightarrow a == c$ (transitive)
- $! (a == b) \Leftrightarrow a != b$
- $a == d \text{ (compiles)} \Leftrightarrow d == a \text{ (compiles)}$
(Note that d is not of the same type as a .)

2. Understanding Value Semantics

Value-Semantic Properties

- operator== (T, T) is called an *equivalence relation*.
- 
1. $a == a$ (reflexive)
 2. $a == b \Leftrightarrow b == a$ (symmetric)
 3. $a == b \ \&\& \ b == c \Rightarrow a == c$ (transitive)
- $!(a == b) \Leftrightarrow a != b$
- $a == d \text{ (compiles)} \Leftrightarrow d == a \text{ (compiles)}$
(Note that ***d*** is not of the same type as ***a***.)

2. Understanding Value Semantics

Value-Semantic Properties

Member operator==

```
class T {  
    // ...  
public:  
    // ...  
    bool operator==(const T& rhs) const;  
    // ...  
};
```

2. Understanding Value Semantics

Value-Semantic Properties

Member `operator==`

```
class T {  
    // ...  
    public:  
        // ...  
        bool operator==(const T& rhs) const;  
        // ...  
};
```

```
class D {  
    // ...  
    public:  
        // ...  
        operator const T&() const;  
        // ...  
};
```

2. Understanding Value Semantics

Value-Semantic Properties

Member `operator==`

```
class T {  
    // ...  
public:  
    // ...  
    bool operator==(const T& rhs) const;  
    // ...  
};
```

```
class D {  
    // ...  
public:  
    // ...  
    operator const T&() const;  
    // ...  
};
```

```
void f(const T& a, const D& d)  
{  
    if (a == d) { /* ... */ }  
}
```

2. Understanding Value Semantics

Value-Semantic Properties

Member operator==

```
class T {  
    // ...  
    public:  
    // ...  
    bool operator==(const T& rhs) const;  
    // ...  
};
```



```
class D {  
    // ...  
    public:  
    // ...  
    operator const T&() const;  
    // ...  
};
```

```
void f(const T& a, const D& d)  
{  
    if (a == d) { /* ... */ }  
    if (d == a) { /* ... */ }  
}
```

2. Understanding Value Semantics

Value-Semantic Properties

Free operator==

```
class T {  
    // ...  
    public:  
    // ...  
};  
// ...  
bool operator==(const T& lhs, const T& rhs);
```

```
class D {  
    // ...  
    public:  
    // ...  
    operator const T&() const;  
    // ...  
};
```

```
void f(const T& a, const D& d)  
{  
    if (a == d) { /* ... */ }  
}
```


2. Understanding Value Semantics

Value-Semantic Properties

Free operator==

```
class T {  
    // ...  
    public:  
        // ...  
};  
// ...  
bool operator==(const T& lhs, const T& rhs);
```

(proper)

```
class D {  
    // ...  
    public:  
        // ...  
        operator const T&() const;  
        // ...  
};
```

```
void f(const T& a, const D& d)  
{  
    if (a == d) { /* ... */ }  
    if (d == a) { /* ... */ }  
}
```

2. Understanding Value Semantics

Value-Semantic Properties

```
class Str {  
    // ...  
public:  
    Str(const char *other);  
    // ...  
  
    // ...  
};  
// ...
```

2. Understanding Value Semantics

Value-Semantic Properties

```
class Str {  
    // ...  
public:  
    Str(const char *other);  
    // ...  
  
    // ...  
};  
// ...  
bool operator==(const Str& lhs, const Str& rhs);
```

2. Understanding Value Semantics

Value-Semantic Properties

```
class Str {  
    // ...  
public:  
    Str(const char *other);  
    // ...  
  
    // ...  
};  
// ...  
bool operator==(const Str& lhs, const Str& rhs);  
bool operator==(const char *lhs, const Str& rhs);
```

2. Understanding Value Semantics

Value-Semantic Properties

```
class Str {      Member Operator==  
    // ...  
public:  
    Str(const char *other);  
    // ...  
    bool operator==(const char *rhs) const;  
    // ...  
};  
// ...  
bool operator==(const Str& lhs, const Str& rhs);  
bool operator==(const char *lhs, const Str& rhs);
```

2. Understanding Value Semantics

Value-Semantic Properties

```
class Str {  
    // ...  
    public:  
        Str(const char *other);  
        // ...  
        bool operator==(const char *rhs) const;  
        // ...  
};  
// ...  
bool operator==(const Str& lhs, const Str& rhs);  
bool operator==(const char *lhs, const Str& rhs);
```

```
class Foo {  
    // ...  
    public:  
        // ...  
        operator const Str&() const;  
        // ...  
};
```

2. Understanding Value Semantics

Value-Semantic Properties

```
class Str {  
    // ...  
    public:  
        Str(const char *other);  
        // ...  
        bool operator==(const char *rhs) const;  
        // ...  
};  
// ...  
bool operator==(const Str& lhs, const Str& rhs);  
bool operator==(const char *lhs, const Str& rhs);
```

```
class Foo {  
    // ...  
    public:  
        // ...  
        operator const Str&() const;  
        // ...  
};
```

```
class Bar {  
    // ...  
    public:  
        // ...  
        operator const char *() const;  
        // ...  
};
```

2. Understanding Value Semantics

Value-Semantic Properties

```
class Str {  
    // ...  
public:  
    Str(const char *other);  
    // ...  
    bool operator==(const char *rhs) const;  
    // ...  
};  
// ...  
bool operator==(const Str& lhs, const Str& rhs);  
bool operator==(const char *lhs, const Str& rhs);
```

```
class Foo {  
    // ...  
public:  
    // ...  
    operator const Str&() const;  
    // ...  
};
```

```
void f(const Foo& foo, const Bar& bar)  
{  
    if (bar == foo) { /* ... */ }  
}
```

```
class Bar {  
    // ...  
public:  
    // ...  
    operator const char *() const;  
    // ...  
};
```


2. Understanding Value Semantics

Value-Semantic Properties

```
class Str {  
    // ...  
public:  
    Str(const char *other);  
    // ...  
    bool operator==(const char *rhs) const;  
    // ...  
};  
// ...  
bool operator==(const Str& lhs, const Str& rhs);  
bool operator==(const char *lhs, const Str& rhs);
```

Bad Idea

Member Operator==

```
class Foo {  
    // ...  
public:  
    // ...  
    operator const Str&() const;  
    // ...  
};
```

```
void f(const Foo& foo, const Bar& bar)  
{  
    if (bar == foo) { /* ... */ }  
    if (foo == bar) { /* ... */ }  
}
```

```
class Bar {  
    // ...  
public:  
    // ...  
    operator const char *() const;  
    // ...  
};
```

2. Understanding Value Semantics

Value-Semantic Properties

```
class Str {  
    // ...  
public:  
    Str(const char *other);  
    // ...  
};  
// ...  
bool operator==(const Str& lhs, const Str& rhs);  
bool operator==(const char *lhs, const Str& rhs);  
bool operator==(const Str& lhs, const char *rhs);
```

Free Operator==

```
class Foo {  
    // ...  
public:  
    // ...  
    operator const Str&() const;  
    // ...  
};
```

```
void f(const Foo& foo, const Bar& bar)  
{  
    if (bar == foo) { /* ... */ }  
}
```

```
class Bar {  
    // ...  
public:  
    // ...  
    operator const char *() const;  
    // ...  
};
```

2. Understanding Value Semantics

Value-Semantic Properties

```
class Str {  
    // ...  
public:  
    Str(const char *other);  
    // ...  
};  
// ...  
bool operator==(const Str& lhs, const Str& rhs);  
bool operator==(const char *lhs, const Str& rhs);  
bool operator==(const Str& lhs, const char *rhs);
```

~~Free~~ Operator== (proper)

```
class Foo {  
    // ...  
public:  
    // ...  
    operator const Str&() const;  
    // ...  
};
```

```
void f(const Foo& foo, const Bar& bar)  
{  
    if (bar == foo) { /* ... */ }  
    if (foo == bar) { /* ... */ }  
}
```

```
class Bar {  
    // ...  
public:  
    // ...  
    operator const char *() const;  
    // ...  
};
```

2. Understanding Value Semantics

Value-Semantic Properties

The operator `==` should ALWAYS be free!

2. Understanding Value Semantics

Value-Semantic Properties

The `operator==` should ALWAYS be free!

Same for *most** binary operators with `const` parameters:

*Except for operators such as `operator[]` that return a *reference* instead of a *value*, and `operator()`.

2. Understanding Value Semantics

Value-Semantic Properties

The `operator==` should ALWAYS be **free!**

Same for *most** binary operators with `const` parameters:

✓ `==` `!=` (equality)

*Except for operators such as `operator[]` that return a **reference** instead of a **value**, and `operator()`.

2. Understanding Value Semantics

Value-Semantic Properties

The operator `==` should ALWAYS be **free!**

Same for *most** binary operators with `const` parameters:

✓ `==` `!=` (equality)

✓ `<` `<=` `>` `=>` (relational)

*Except for operators such as `operator[]` that return a **reference** instead of a **value**, and `operator()`.

2. Understanding Value Semantics

Value-Semantic Properties

The `operator==` should ALWAYS be **free!**

Same for *most** binary operators with `const` parameters:

✓	<code>==</code>	<code>!=</code>				(equality)
✓	<code><</code>	<code><=</code>	<code>></code>	<code>=></code>		(relational)
✓	<code>+</code>	<code>-</code>	<code>*</code>	<code>/</code>	<code>%</code>	(arithmetic)

*Except for operators such as `operator[]` that return a **reference** instead of a **value**, and `operator()`.

2. Understanding Value Semantics

Value-Semantic Properties

The `operator==` should ALWAYS be **free!**

Same for *most** binary operators with `const` parameters:

✓	<code>==</code>	<code>!=</code>				(equality)
✓	<code><</code>	<code><=</code>	<code>></code>	<code>=></code>		(relational)
✓	<code>+</code>	<code>-</code>	<code>*</code>	<code>/</code>	<code>%</code>	(arithmetic)
✓	<code> </code>	<code>&</code>	<code>^</code>	<code><<</code>	<code>>></code>	(logical)

*Except for operators such as `operator[]` that return a **reference** instead of a **value**, and `operator()`.

2. Understanding Value Semantics

Value-Semantic Properties

The operator `==` should ALWAYS be free!

But not operator `@=`

✓	<code>==</code>	<code>!=</code>				(equality)
✓	<code><</code>	<code><=</code>	<code>></code>	<code>=></code>		(relational)
✓	<code>+</code>	<code>-</code>	<code>*</code>	<code>/</code>	<code>%</code>	(arithmetic)
✓	<code> </code>	<code>&</code>	<code>^</code>	<code><<</code>	<code>>></code>	(logical)

*Except for operators such as `operator[]` that return a *reference* instead of a *value*, and `operator()`.

2. Understanding Value Semantics

Value-Semantic Properties

The operator== should ALWAYS be free!

But not operator@=

✓	==	!=				(equality)
✓	<	<=	>	=>		(relational)
✓	+	-	*	/	%	(arithmetic)
✓		&	^	<<	>>	(logical)
✗	+=	-=	*=	/=	%=	(assignment)

*Except for operators such as `operator[]` that return a *reference* instead of a *value*, and `operator()`.

2. Understanding Value Semantics

Value-Semantic Properties

The operator== should ALWAYS be free!

But not operator@=

✓ == != (equality)

✓ < <= > ==> (relational)

✓ + - * / % (arithmetic)

✓ | & ^ << >> (logical)

✗ += -= *= /= %= (assignment)

✗ |= &= ^= <<= >>= (assignment)

*Except for operators such as operator[] that return a *reference* instead of a *value*, and operator().

What semantics
should value-type
operations have?

2. Understanding Value Semantics

Where is “Value” Defined?

2. Understanding Value Semantics

Where is “Value” Defined?

The ***salient attributes*** of a type \mathbb{T} are the documented set of named attributes whose respective values for a given instance of \mathbb{T} ...

2. Understanding Value Semantics

Where is “Value” Defined?

The *salient attributes* of a type \mathbb{T} are the documented set of named attributes whose respective values for a given instance of \mathbb{T}

1. Derive from the physical state of *only* that instance of \mathbb{T} .

2. Understanding Value Semantics

Where is “Value” Defined?

The *salient attributes* of a type \mathbb{T} are the documented set of named attributes whose respective values for a given instance of \mathbb{T}

1. Derive from the physical state of *only* that instance of \mathbb{T} .
2. Must *respectively* “have” (refer to) the same value in order for two instances of \mathbb{T} to have (refer to) the same value *as a whole*.

2. Understanding Value Semantics

Where is “Value” Defined?

The ***salient attributes*** of a type \mathbb{T} are the documented set of named attributes whose respective values for a given instance of \mathbb{T} that

1. Derive from the physical state of *only* that instance of \mathbb{T} .
2. Must *respectively* “have” (refer to) the same value in order for two instances of \mathbb{T} to have (refer to) the same value *as a whole*.

2. Understanding Value Semantics

Where is “Value” Defined? Copy Constructor?

The *salient attributes* of a type \mathbb{T} are the documented set of named attributes whose respective values for a given instance of \mathbb{T} that

1. Derive from the physical state of *only* that instance of \mathbb{T} .
2. Must *respectively* “have” (refer to) the same value in order for two instances of \mathbb{T} to have (refer to) the same value *as a whole*.

2. Understanding Value Semantics

Where is “Value” Defined? Copy Constructor?

- By def., *all salient attributes* must be copied.

2. Understanding Value Semantics

Where is “Value” Defined? Copy Constructor?

- By def., *all salient attributes* must be copied.
- What about “non-salient” attributes?
 - E.g., `capacity()`

2. Understanding Value Semantics

Where is “Value” Defined? Copy Constructor?

- By def., *all salient attributes* must be copied.
- What about “non-salient” attributes?
 - E.g., `capacity()`
- Non-salient attributes may or may not be copied.

More on this later...

2. Understanding Value Semantics

Where is “Value” Defined? Copy Constructor?

- By def., *all salient attributes* must be copied.
- What about “non-salient” attributes?
 - E.g., `capacity()`
- Non-salient attributes may or may not be copied.
- Hence, we **cannot** infer from the implementation of a Copy Constructor which attributes are “salient.”

2. Understanding Value Semantics

Where is “Value” Defined? Copy Constructor?

- By def., *all salient attributes* must be copied.
- What about “non-salient” attributes?
 - E.g., `capacity()`
- Non-salient attributes may or may not be copied.
- Hence, we **cannot** infer from the implementation of a Copy Constructor which attributes are “salient.”
- **Cannot** tell us if two objects have *the same value*!

2. Understanding Value Semantics

Where is “Value” Defined?

The ***salient attributes*** of a type \mathbb{T} are the documented set of named attributes whose respective values for a given instance of \mathbb{T} that

1. Derive from the physical state of *only* that instance of \mathbb{T} .
2. Must *respectively* “have” (refer to) the same value in order for two instances of \mathbb{T} to “have” (refer to) the same value *as a whole*.

2. Understanding Value Semantics

Where is “Value” Defined?

The ***salient attributes*** of a type \mathbb{T} are the documented set of named attributes whose respective values for a given instance of \mathbb{T} that

1. Derive from the physical state of *only* that instance of \mathbb{T} .
2. Must *respectively* *compare equal* in order for two instances of \mathbb{T} to *compare equal* *as a whole*.

2. Understanding Value Semantics

Where is “Value” Defined?

operator==

The ***salient attributes*** of a type \mathbb{T} are the documented set of named attributes whose respective values for a given instance of \mathbb{T} that

1. Derive from the physical state of *only* that instance of \mathbb{T} .
2. Must *respectively* compare equal in order for two instances of \mathbb{T} to compare equal *as a whole*.

2. Understanding Value Semantics

Where is “Value” Defined?

`operator==`

The associated, homogeneous (free) `operator==`
for a type T

2. Understanding Value Semantics

Where is “Value” Defined?

`operator==`

The associated, homogeneous (free) `operator==`
for a type \mathbb{T}

Implementation

1. **Provides** an *operational definition* of what it means for two objects of type \mathbb{T} to have “the same” *value*.

2. Understanding Value Semantics

Where is “Value” Defined?

`operator==`

The associated, homogeneous (free) `operator==`
for a type \mathbb{T} **Implementation**

1. **Provides** an *operational definition* of what it means for two objects of type \mathbb{T} to have “the same” *value*.

2. **Defines** the *salient attributes* of \mathbb{T} as those attributes whose respective values must *compare equal* in order for two instances of \mathbb{T} to *compare equal*.

Interface/Contract

2. Understanding Value Semantics

Value-Semantic Properties

Value-semantic objects share many properties.

2. Understanding Value Semantics

Value-Semantic Properties

Value-semantic objects share many properties.

- Each of these properties is objectively verifiable, irrespective of the intended application domain.

2. Understanding Value Semantics

Value-Semantic Properties

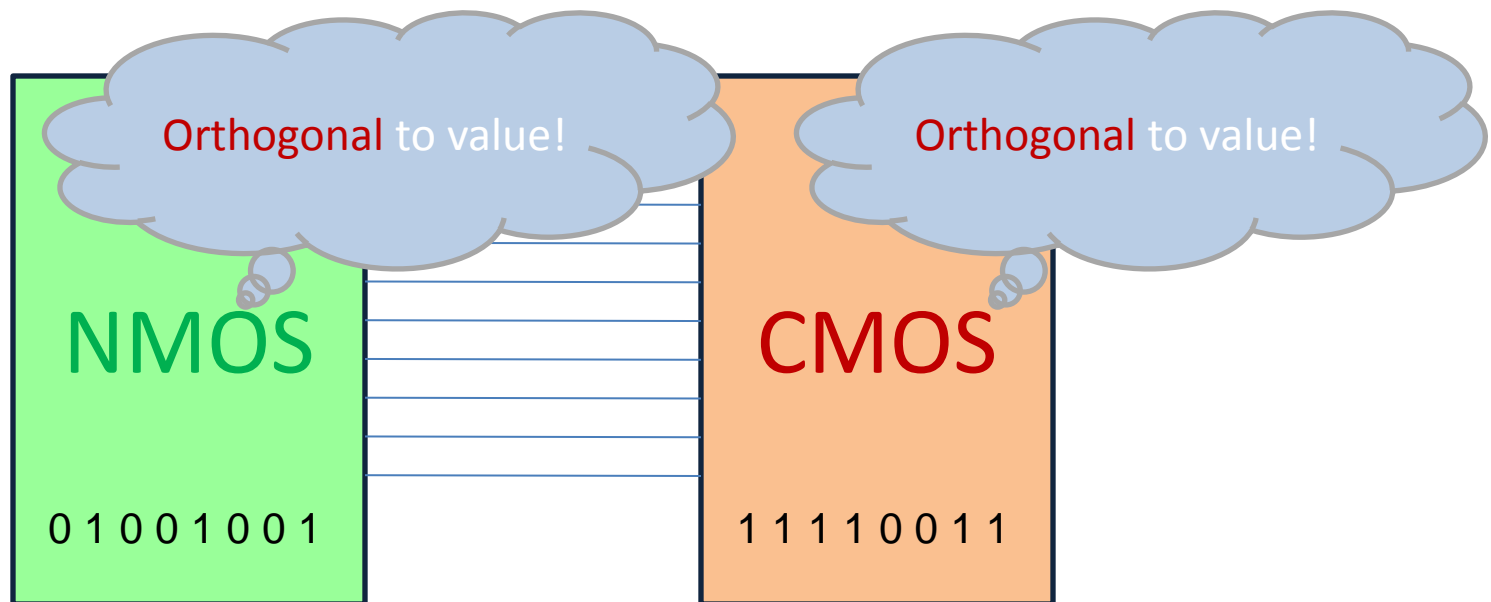
Value-semantic objects share many properties.

- Each of these properties is objectively verifiable, irrespective of the intended application domain.
- Most are (or should be) intuitive.

2. Understanding Value Semantics

What should be copied?

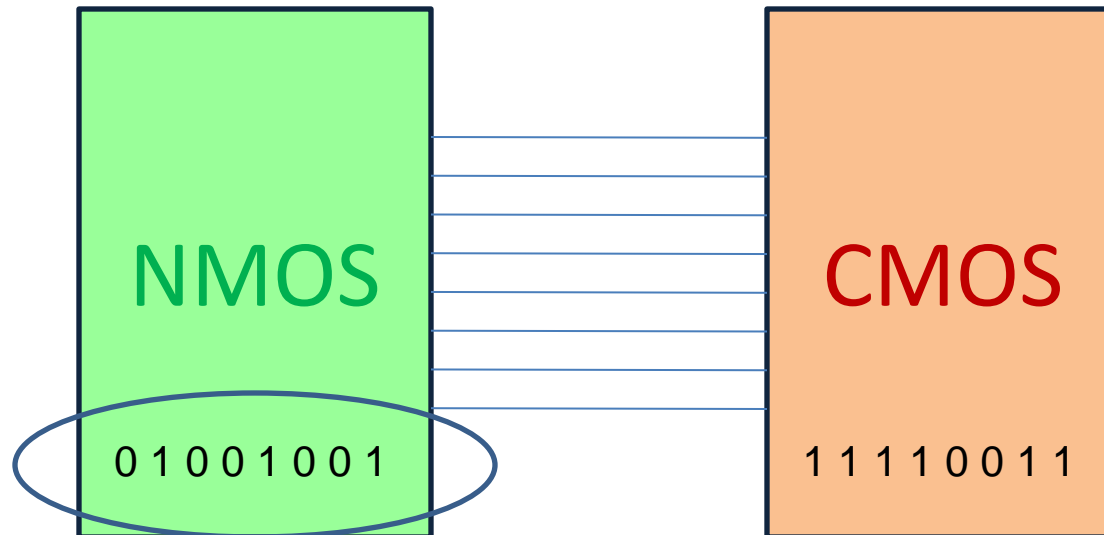
Should attributes that are **orthogonal** to value be copied?



2. Understanding Value Semantics

What should be copied?

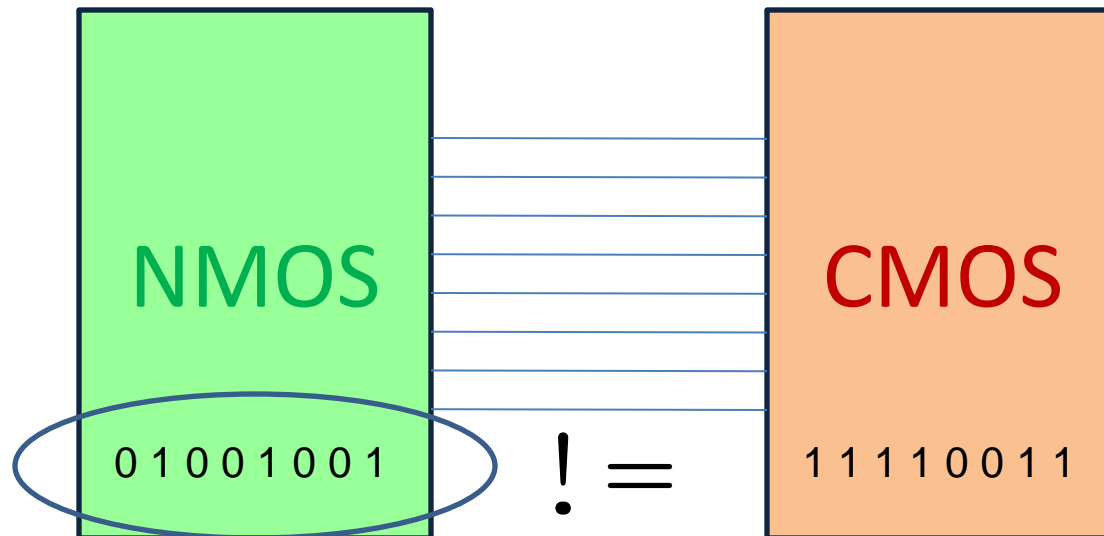
Should attributes that are **orthogonal** to value be copied?



2. Understanding Value Semantics

What should be copied?

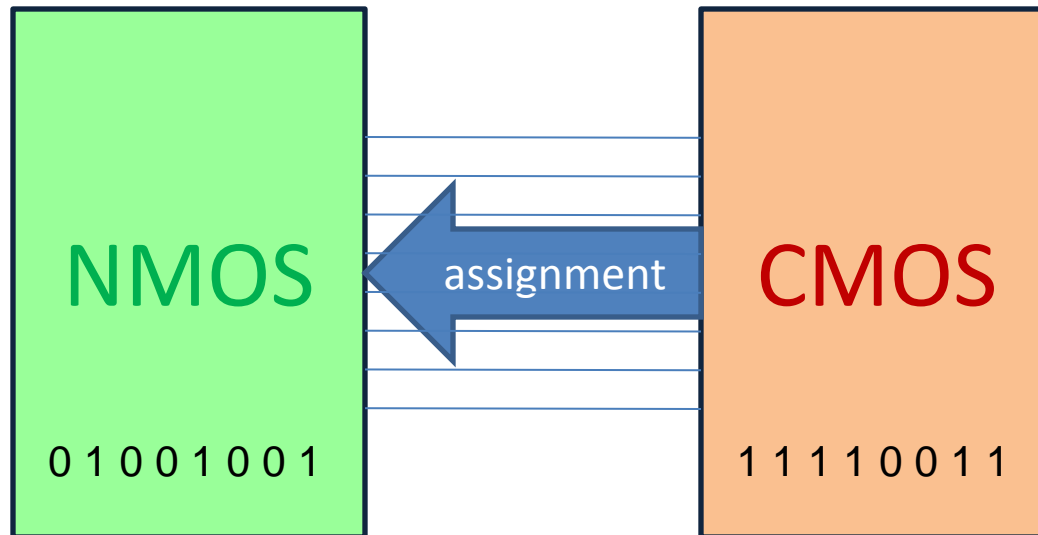
Should attributes that are **orthogonal** to value be copied?



2. Understanding Value Semantics

What should be copied?

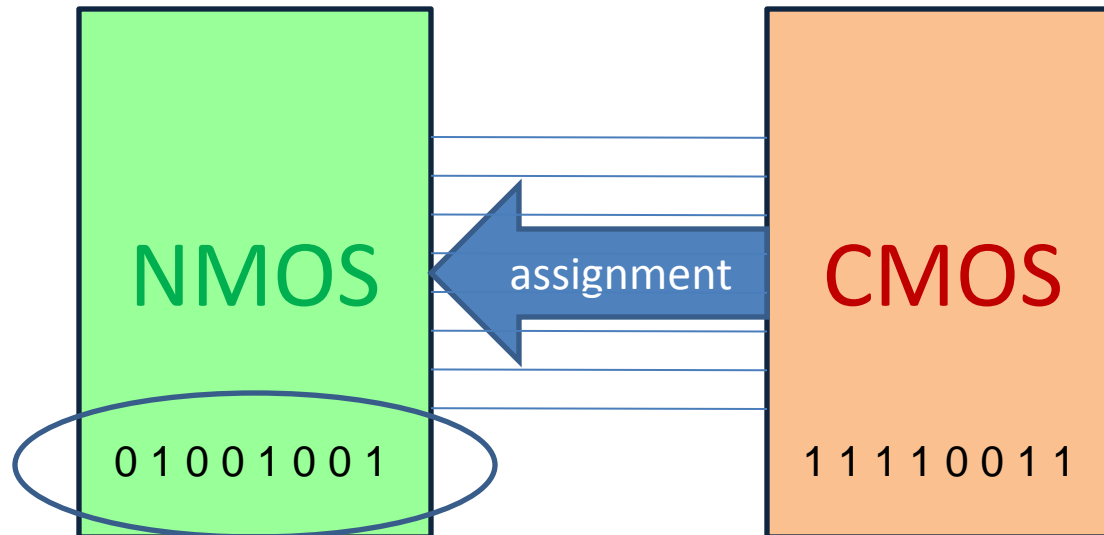
Should attributes that are **orthogonal** to value be copied?



2. Understanding Value Semantics

What should be copied?

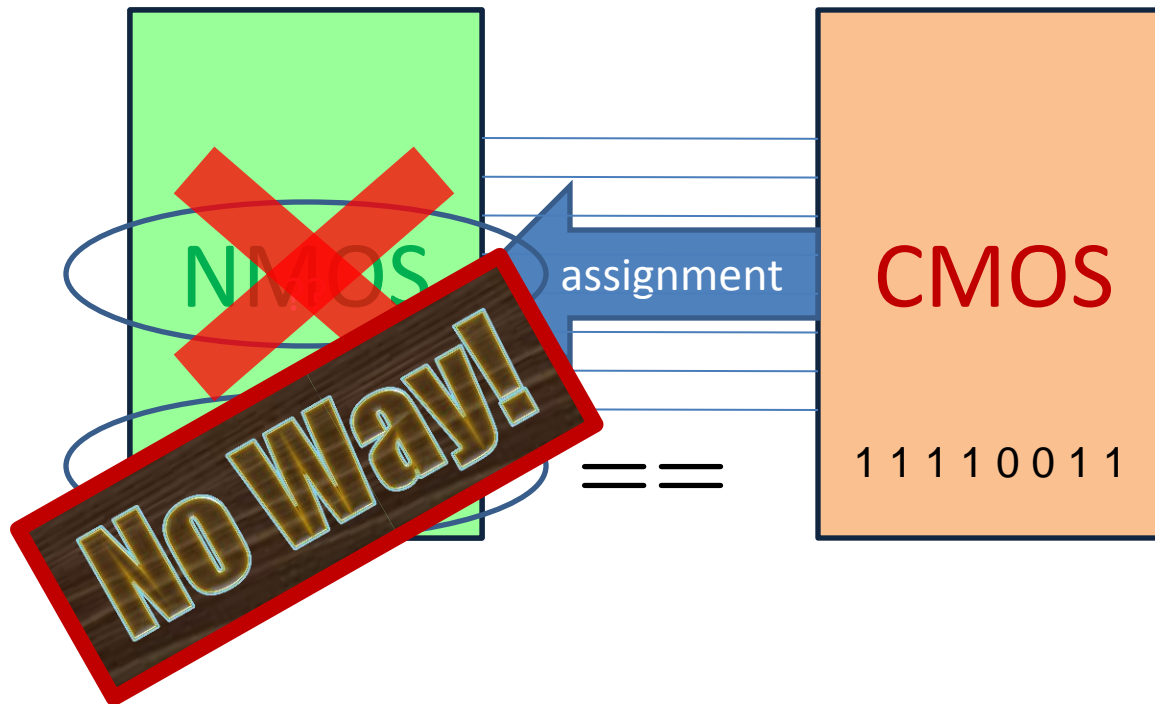
Should attributes that are **orthogonal** to value be copied?



2. Understanding Value Semantics

What should be copied?

Should attributes that are **orthogonal** to value be copied?



2. Understanding Value Semantics

What should be copied?

V-TABLE POINTER?

ALLOCATOR?

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

As it turns out...

Choosing salient attributes
appropriately *will* affect our
ability to test thoroughly.

2. Understanding Value Semantics

Value-Semantic Properties

If \mathbb{T} is a value-semantic type,

a, ***b***, and ***c*** are objects of type \mathbb{T} , and

d is an object of some *other* type \mathbb{D} , then

2. Understanding Value Semantics

Value-Semantic Properties

If \mathbb{T} is a value-semantic type,

\mathbf{a} , \mathbf{b} , and \mathbf{c} are objects of type \mathbb{T} , and

\mathbf{d} is an object of some *other* type \mathbb{D} , then

➤ $\mathbf{a} == \mathbf{b} \Leftrightarrow \mathbf{a}$ and \mathbf{b} have the same value
(assuming an associated `operator==` exists).

2. Understanding Value Semantics

Value-Semantic Properties

If \mathbb{T} is a value-semantic type,

a , b , and c are objects of type \mathbb{T} , and

d is an object of some *other* type \mathbb{D} , then

➤ $a == b \Leftrightarrow a$ and b have the same value
(assuming an associated `operator==` exists).

2. Understanding Value Semantics

Value-Semantic Properties

If \mathbb{T} is a value-semantic type,

a , b , and c are objects of type \mathbb{T} , and

d is an object of some *other* type \mathbb{D} , then

➤ $a == b \Leftrightarrow a$ and b have the same value
(assuming an associated `operator==` exists).

(Sometimes a value-semantic type is “almost” *regular*.)

2. Understanding Value Semantics

Value-Semantic Properties

If \mathbb{T} is a value-semantic type,

a , b , and c are objects of type \mathbb{T} , and

d is an object of some *other* type \mathbb{D} , then

➤ $a == b \Leftrightarrow a$ and b have the same value
(assuming an associated `operator==` exists).

(Sometimes a value-semantic type is “almost” regular.)

MORE ON THIS LATER

2. Understanding Value Semantics

Value-Semantic Properties

If \mathbb{T} is a value-semantic type,

\mathbf{a} , \mathbf{b} , and \mathbf{c} are objects of type \mathbb{T} , and

\mathbf{d} is an object of some *other* type \mathbb{D} , then

- $\mathbf{a} == \mathbf{b} \Leftrightarrow \mathbf{a}$ and \mathbf{b} have the same value
(assuming an associated `operator==` exists).
- The *value* of \mathbf{a} is independent of *any* external object or state; any change to \mathbf{a} must be accomplished via \mathbf{a} 's (public) interface.

2. Understanding Value Semantics

Value-Semantic Properties

Suppose a “*value-semantic*” object refers to another autonomous object in memory:

2. Understanding Value Semantics

Value-Semantic Properties

Suppose a “*value-semantic*” object refers to another autonomous object in memory:

```
class ElemPtr {  
    Record *d_record_p;  
    int     d_elementIndex;  
public:  
    // ...  
};
```

2. Understanding Value Semantics

Value-Semantic Properties

Suppose a “*value-semantic*” object refers to another autonomous object in memory:

```
class ElemPtr {  
    Record *d_record_p;  
    int      d_elementIndex;  
public:  
    // ...  
};
```

2. Understanding Value Semantics

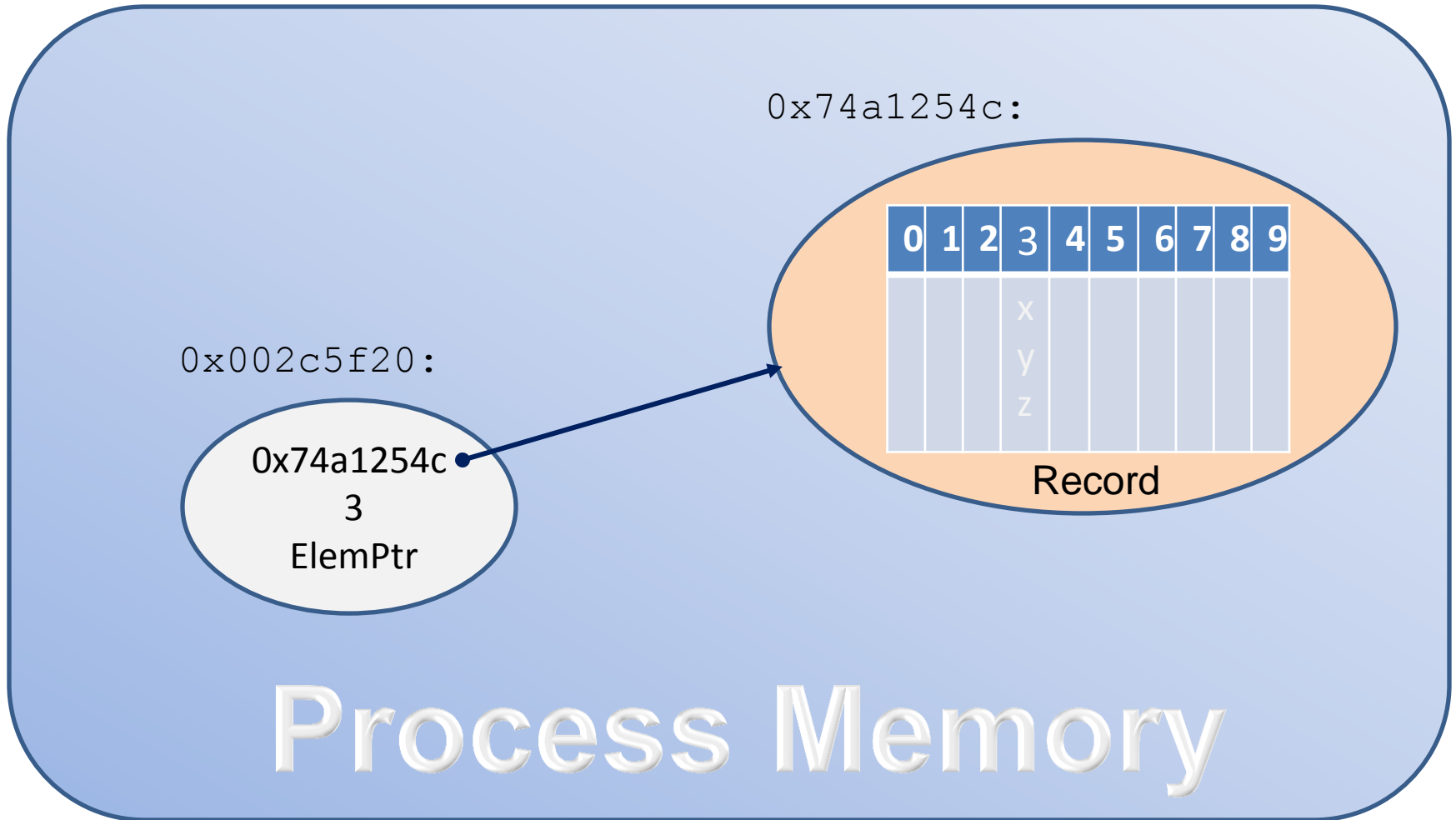
Value-Semantic Properties

Suppose a “*value-semantic*” object refers to another autonomous object in memory:

```
class ElemPtr {  
    Record *d_record_p;  
    int      d_elementIndex;  
public:  
    // ...  
};
```

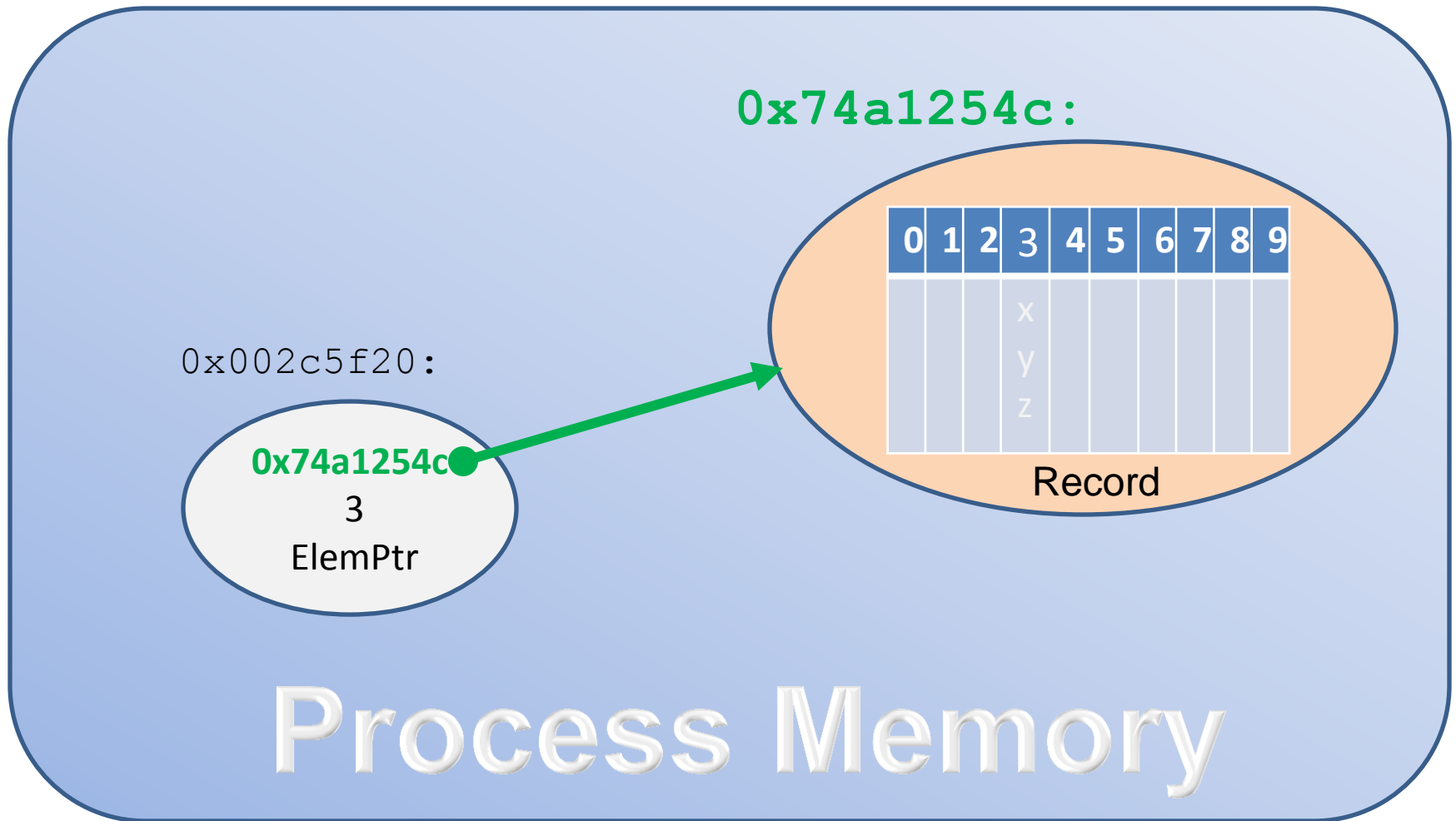
2. Understanding Value Semantics

Value-Semantic Properties



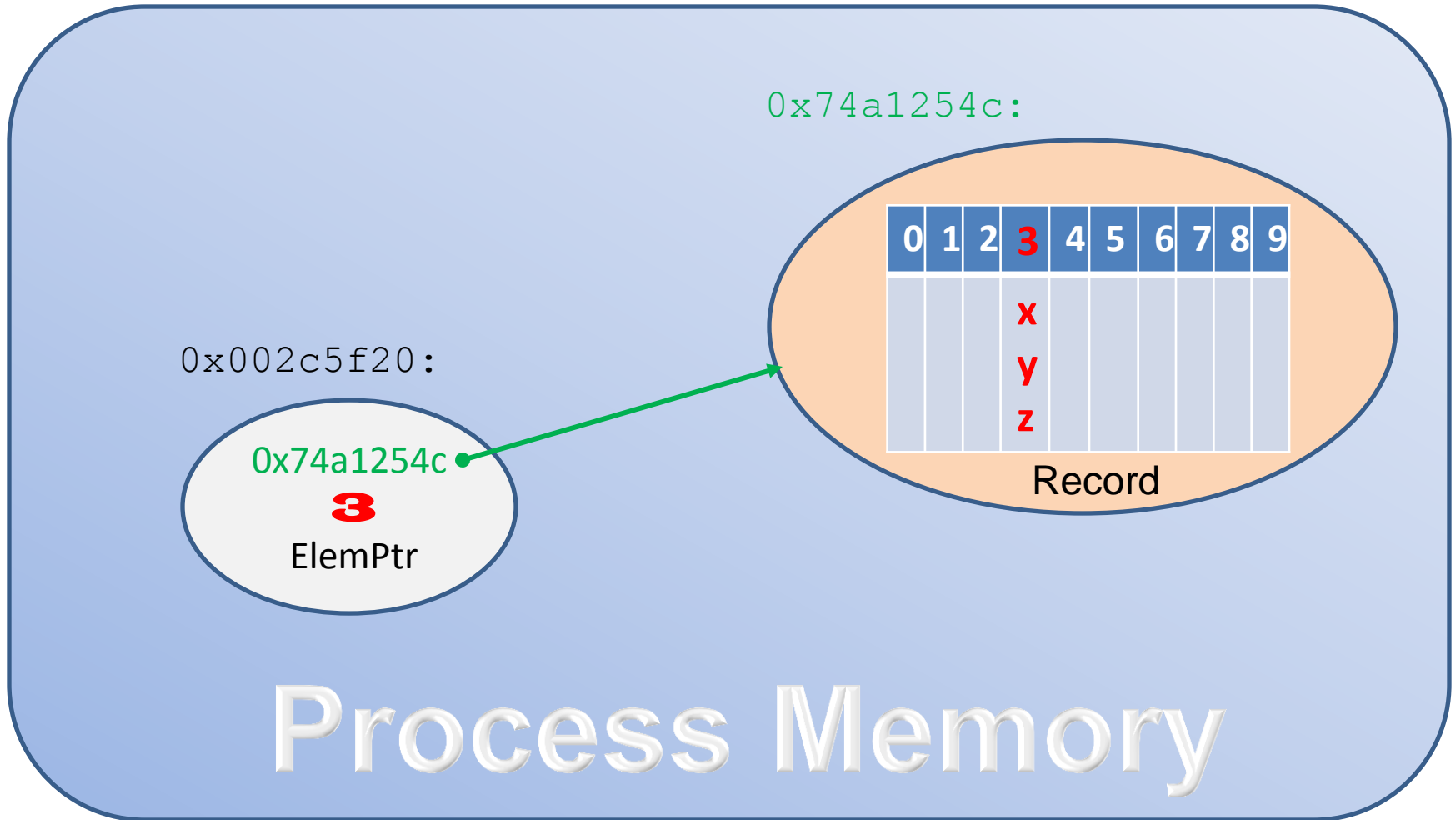
2. Understanding Value Semantics

Value-Semantic Properties



2. Understanding Value Semantics

Value-Semantic Properties



2. Understanding Value Semantics

Value-Semantic Properties

```
bool operator==(const ElemPtr& lhs,  
                const ElemPtr& rhs);
```

2. Understanding Value Semantics

Value-Semantic Properties

```
bool operator==(const ElemPtr& lhs,  
                const ElemPtr& rhs);  
// Two 'ElemPtr' objects have the  
// same value if they ...
```


2. Understanding Value Semantics

Value-Semantic Properties

```
bool operator==(const ElemPtr& lhs,  
                const ElemPtr& rhs);  
  
// Two 'ElemPtr' objects have the  
// same value if they (1) refer  
// to the same 'Record' object  
// (in the current process) ...
```

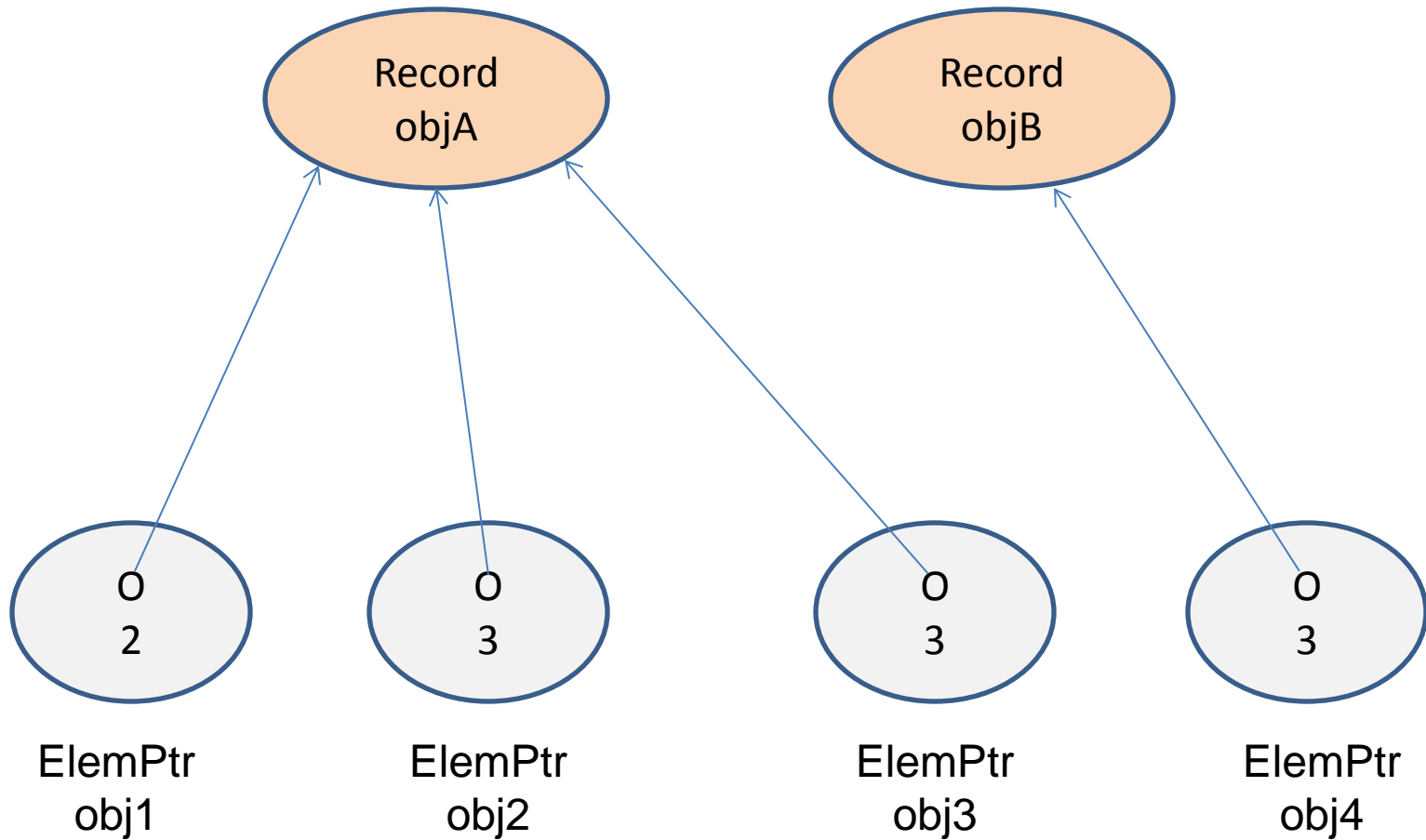
2. Understanding Value Semantics

Value-Semantic Properties

```
bool operator==(const ElemPtr& lhs,  
                const ElemPtr& rhs);  
  
// Two 'ElemPtr' objects have the  
// same value if they (1) refer  
// to the same 'Record' object  
// (in the current process), and  
// (2) have the same element  
// index.
```

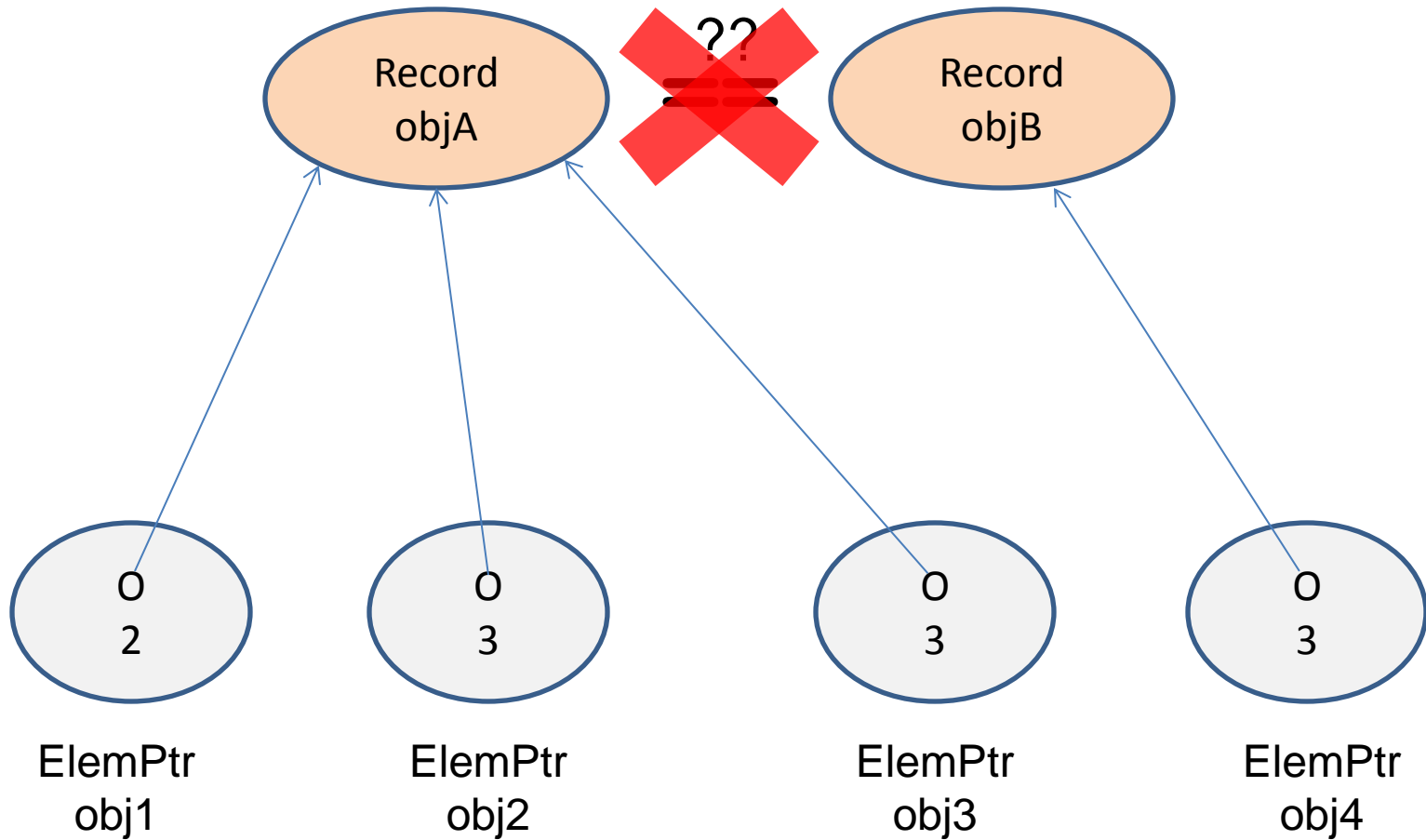
2. Understanding Value Semantics

Value-Semantic Properties



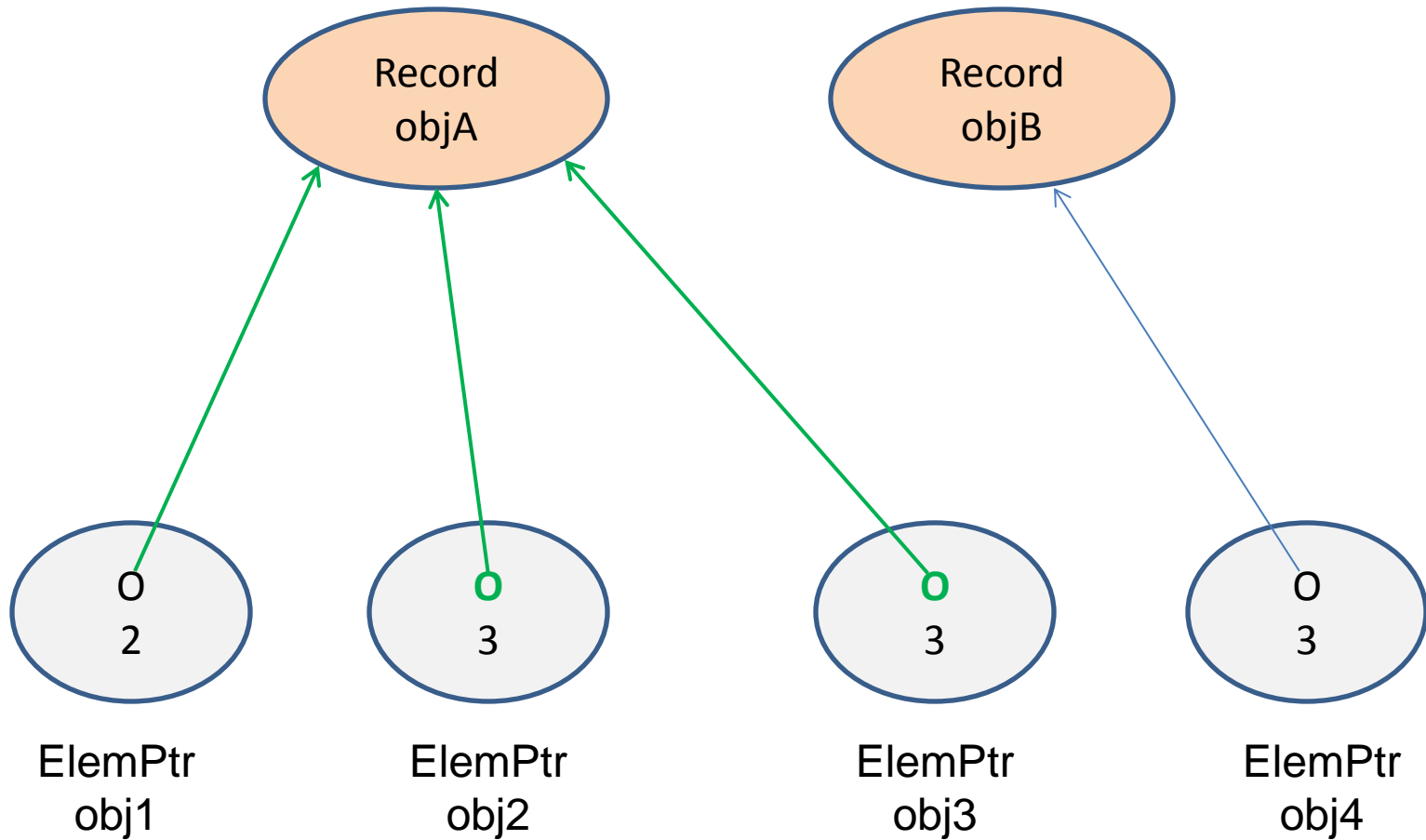
2. Understanding Value Semantics

Value-Semantic Properties



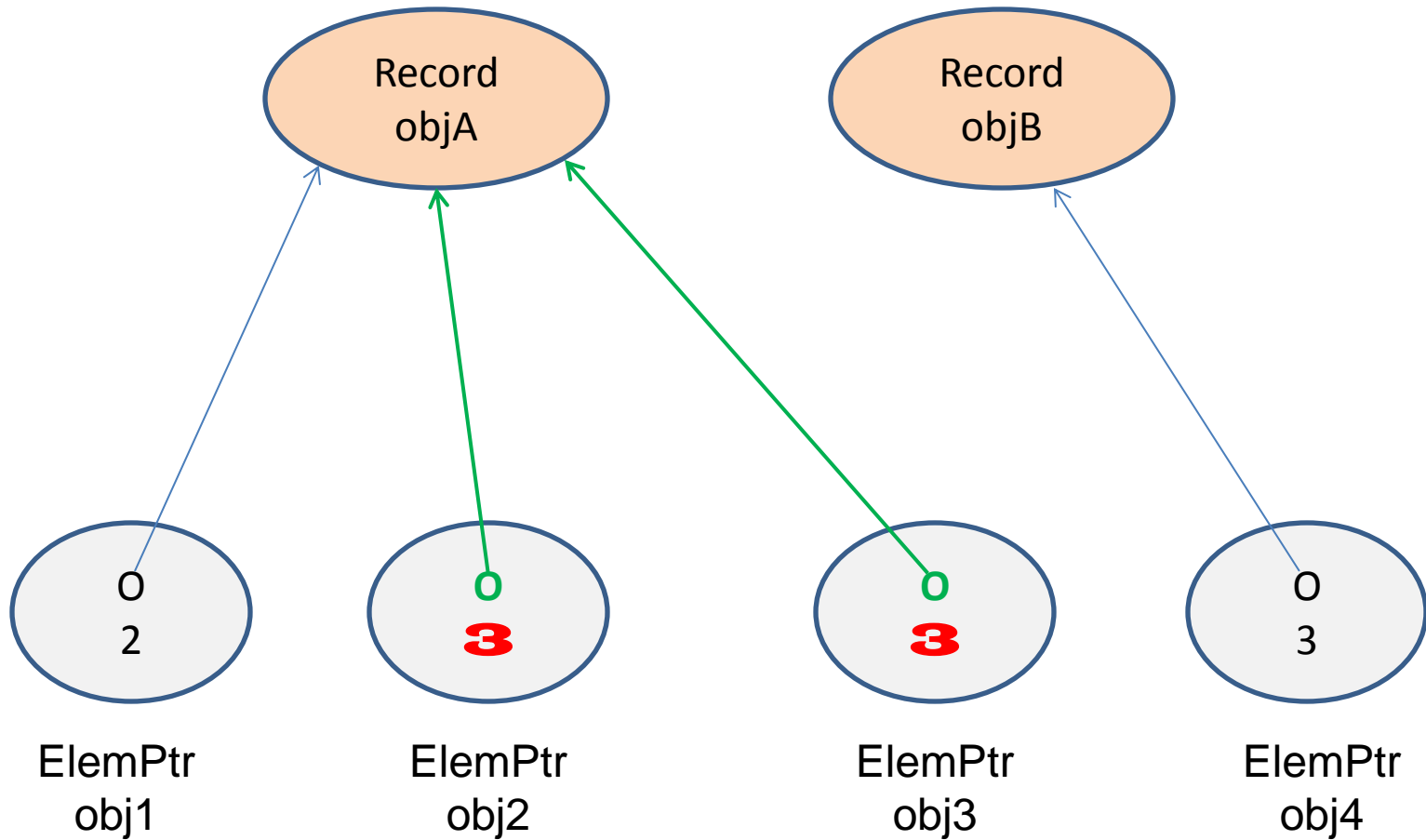
2. Understanding Value Semantics

Value-Semantic Properties



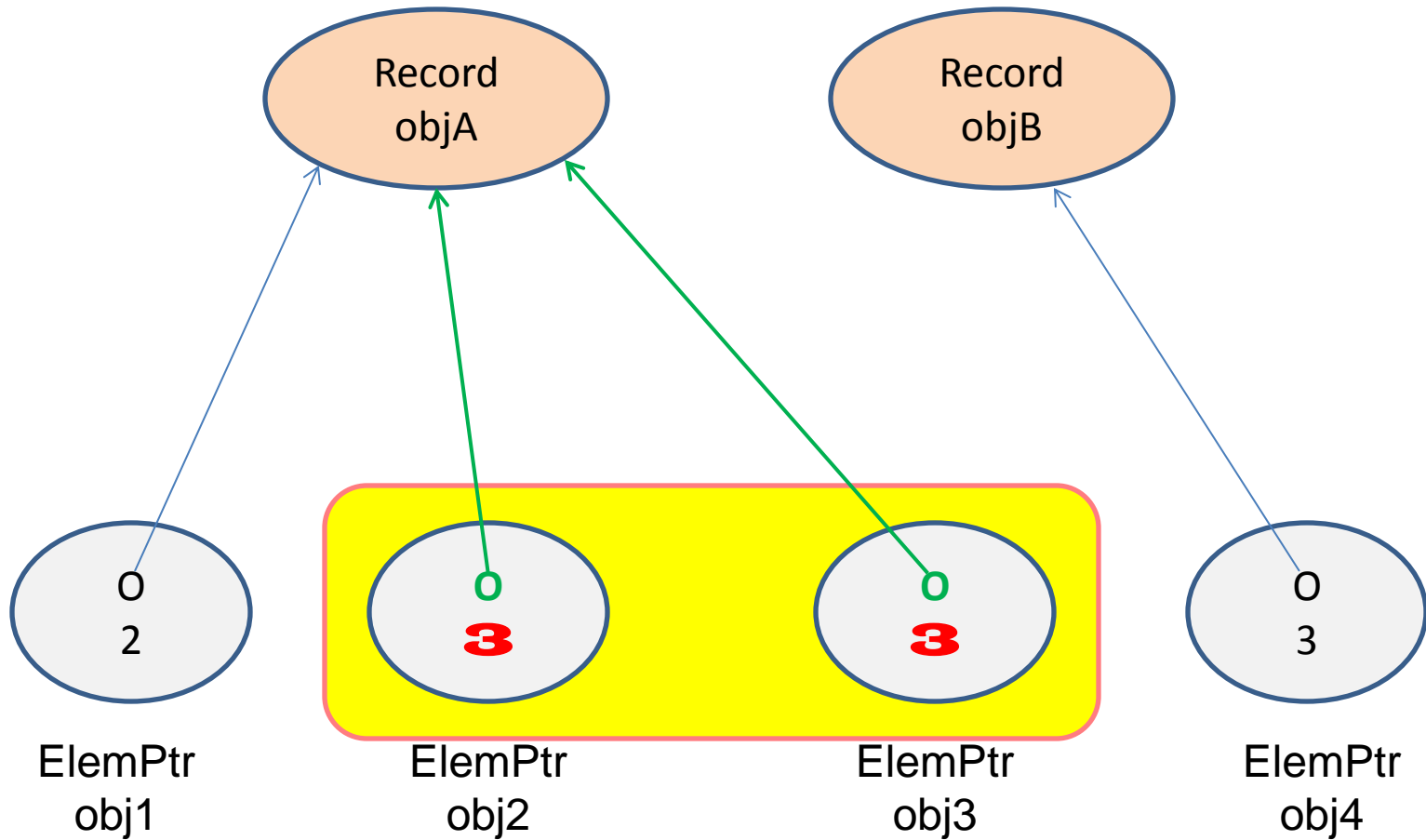
2. Understanding Value Semantics

Value-Semantic Properties



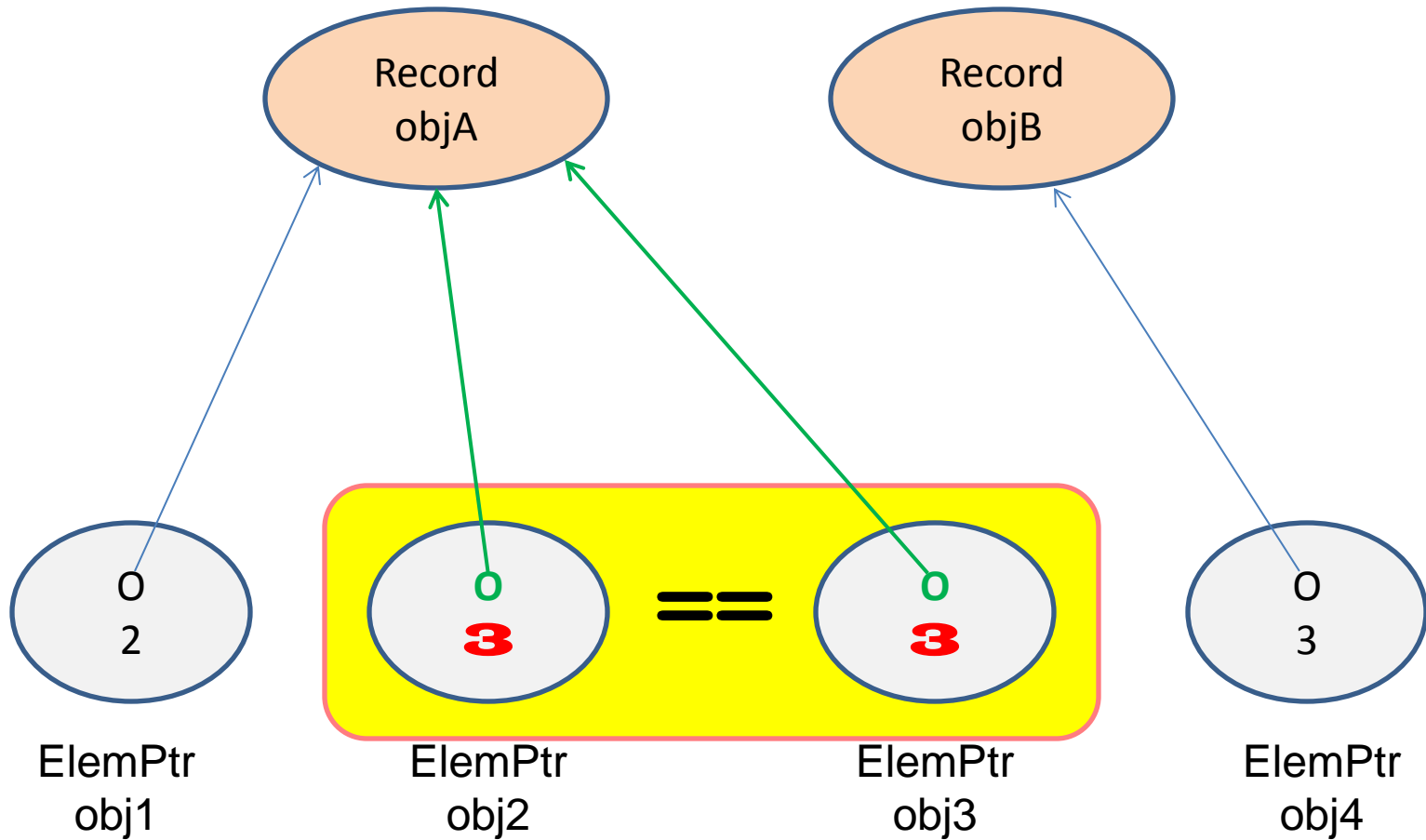
2. Understanding Value Semantics

Value-Semantic Properties



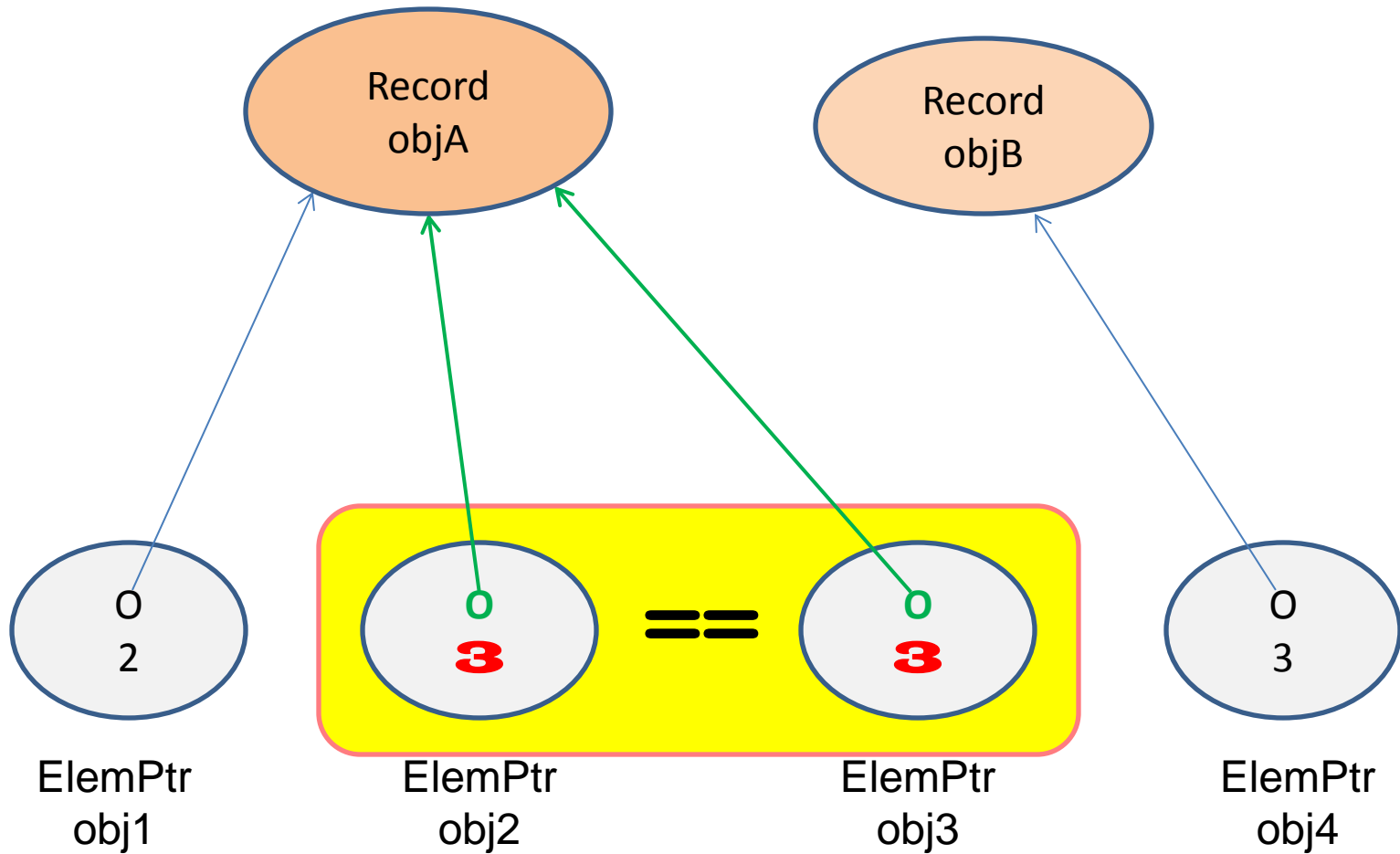
2. Understanding Value Semantics

Value-Semantic Properties



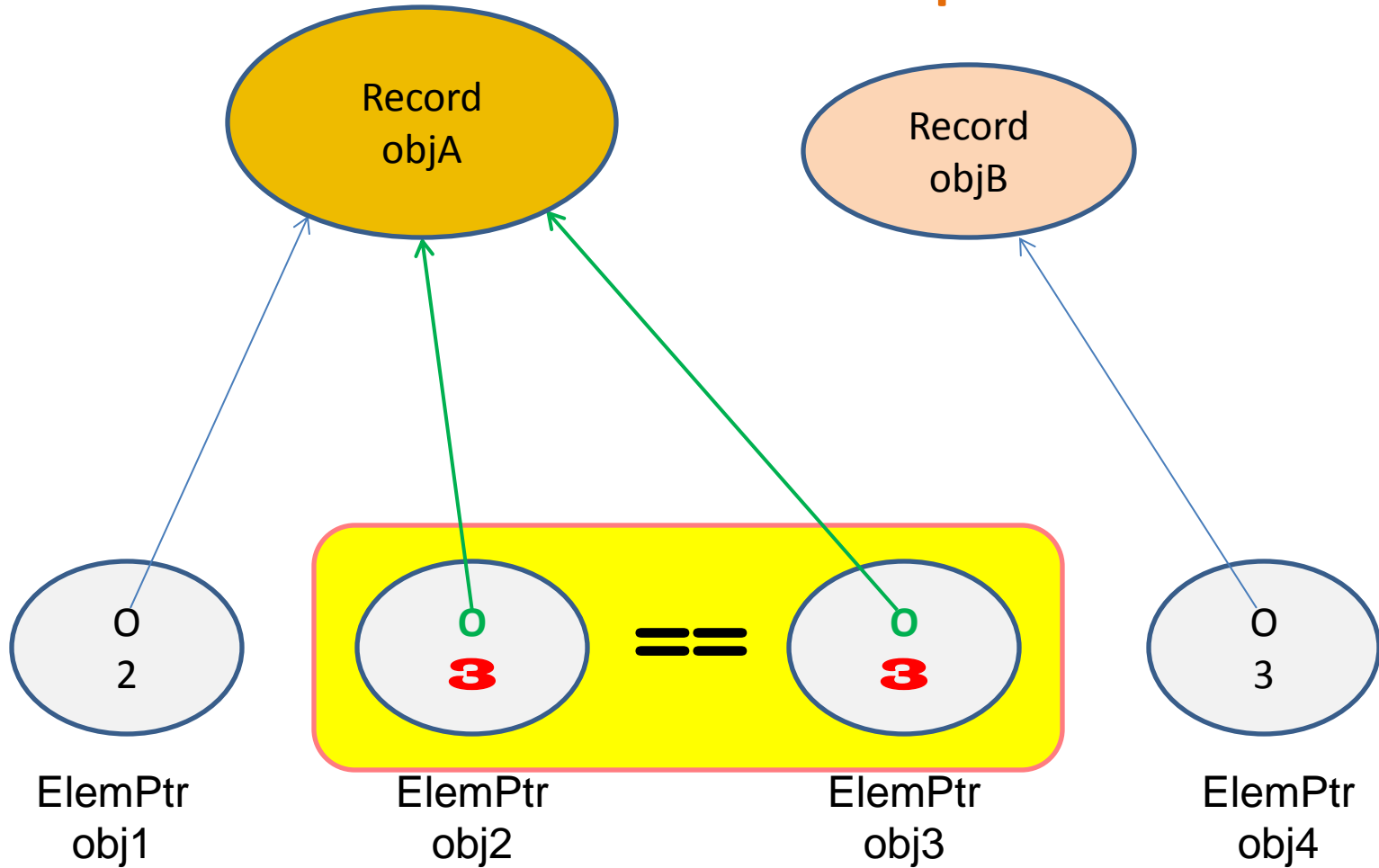
2. Understanding Value Semantics

Value-Semantic Properties



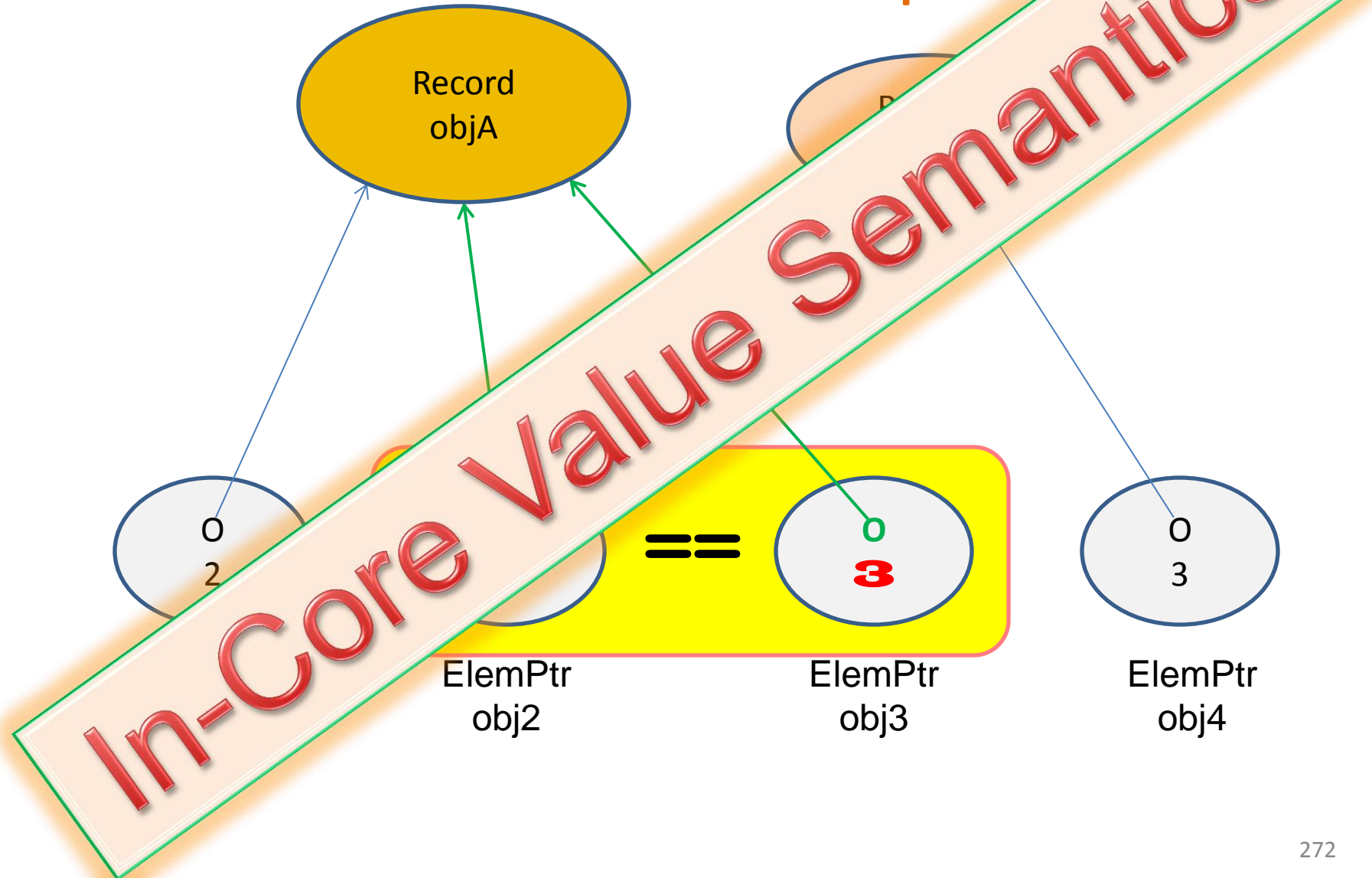
2. Understanding Value Semantics

Value-Semantic Properties



2. Understanding Value Semantics

Value-Semantic Properties



2. Understanding Value Semantics

Value-Semantic Properties

**I.E., NOT
FULL VALUE
SEMANTICS**

Element
obj2

obj3

2. Understanding Value Semantics

Value-Semantic Properties

**In-Core Value Semantics,
While Important, Is Not
The Focus of Today's Talk**

Note that if we were to ascribe a notion of value to, say, a *scoped guard*, it would clearly be in-core only.

2. Understanding Value Semantics

“Value Types” having Value Semantics

2. Understanding Value Semantics

“Value Types” having Value Semantics

A C++ type that “properly” represents (a subset of) the values of an abstract “mathematical” type is said to have ***value semantics***.

2. Understanding Value Semantics

“Value Types” having Value Semantics

A C++ type that “properly” represents (a subset of) the values of an abstract “mathematical” type is said to have *value semantics*.

2. Understanding Value Semantics

Value-Semantic Properties

Recall that two *distinct* objects **a** and **b** of type T that have *the same **value** might not* exhibit “the same” ***observable behavior***.

2. Understanding Value Semantics

Value-Semantic Properties

Recall that two *distinct* objects **a** and **b** of type T that have *the same value might not* exhibit “the same” ***observable behavior***.

E.g., one *might* allocate memory on an append operation, whereas another *might not*.

2. Understanding Value Semantics

Value-Semantic Properties

Recall that two *distinct* objects **a** and **b** of type **T** that have *the same value might not* exhibit “the same” *observable behavior*.

HOWEVER

2. Understanding Value Semantics

Value-Semantic Properties

Recall that two *distinct* objects **a** and **b** of type T that have *the same value might not* exhibit “the same” *observable behavior*.

HOWEVER

1. If **a** and **b** initially have the same value, and

2. Understanding Value Semantics

Value-Semantic Properties

Recall that two *distinct* objects **a** and **b** of type T that have *the same **value** might not* exhibit “the same” ***observable behavior***.

HOWEVER

1. If **a** and **b** initially have the same value, and
2. the same operation is applied to each object, then

2. Understanding Value Semantics

Value-Semantic Properties

Recall that two *distinct* objects **a** and **b** of type T that have *the same value might not* exhibit “the same” *observable behavior*.

HOWEVER

1. If **a** and **b** initially have the same value, and
2. the same operation is applied to each object, then
3. (absent any *exceptions* or *undefined behavior*)

2. Understanding Value Semantics

Value-Semantic Properties

Recall that two *distinct* objects **a** and **b** of type **T** that have *the same **value** might not* exhibit “the same” ***observable behavior***.

HOWEVER

1. If **a** and **b** initially have the same value, and
2. the same operation is applied to each object, then
3. (absent any *exceptions* or *undefined behavior*)
4. **both objects will again have the same value!**

2. Understanding Value Semantics

Value-Semantic Properties

There is a lot more to this story!

Deciding what is (not) *salient* is surprisingly important.

SUBTLE ESSENTIAL PROPERTY OF VALUE

1. If **a** and **b** initially have the same value, and
2. the same operation is applied to each object, then
3. (absent any *exceptions* or *undefined behavior*)
4. **both objects will again have the same value!**

2. Understanding Value Semantics

Value-Semantic Properties

That is...

```
if ( a == b ) {  
    op1(a) ; op1(b) ; assert ( a == b ) ;  
    op2(a) ; op2(b) ; assert ( a == b ) ;  
    op3(a) ; op3(b) ; assert ( a == b ) ;  
    op4(a) ; op4(b) ; assert ( a == b ) ;  
    ⋮           ⋮           ⋮  
}
```

SUBTLE ESSENTIAL PROPERTY OF VALUE

2. Understanding Value Semantics

Value-Semantic Property

Note that this is not a test case, but rather a requirements specification.

That is...

```
if ( a == b ) {  
    op1(a) ; op1(b) ; assert ( a == b ) ;  
    op2(a) ; op2(b) ; assert ( a == b ) ;  
    op3(a) ; op3(b) ; assert ( a == b ) ;  
    op4(a) ; op4(b) ; assert ( a == b ) ;  
    ⋮           ⋮           ⋮  
}
```

SUBTLE ESSENTIAL PROPERTY OF VALUE

2. Understanding Value Semantics

Value-Semantic Properties

QUESTION:

Suppose we have a “home grown” ordered-set type that can be initialized to a sequence of elements in either increasing or decreasing order:

```
template <class T>
class OrderedSet {
    // ...
    OrderedSet(bool decreasingFlag = false);
    // ...
};
```

2. Understanding Value Semantics

Value-Semantic Properties

QUESTION:

Suppose we have a “home grown” ordered-set type that can be initialized to a sequence of elements in either increasing or decreasing order:

```
template <class T>
class OrderedSet {
    // ...
    OrderedSet(bool decreasingFlag = false);
    // ...
};
```

What if the two sets were constructed differently.

2. Understanding Value Semantics

Value-Semantic Properties

QUESTION:

Suppose we have a “home grown” ordered-set type that can be initialized to a sequence of elements in either increasing or decreasing order:

```
template <class T>
class OrderedSet {
    // ...
    OrderedSet(bool decreasingFlag = false);
    // ...
};
```

What if the two sets were constructed differently. Should any two empty objects be considered “equal”?

2. Understanding Value Semantics

Value-Semantic Properties

1. If **a** and **b** initially have the same value, and
2. the same operation is applied to each object, then
3. (absent any *exceptions* or *undefined behavior*)
4. **both objects will again have the same value!**

2. Understanding Value Semantics

Value-Semantic Properties

1. If **a** and **b** initially have the same value, and
2. the same operation is applied to each object, then
3. (absent any ^{^salient} *exceptions* or *undefined behavior*)
4. **both objects will again have the same value!**

2. Understanding Value Semantics

Value-Semantic Properties

By *salient* we mean operations that directly reflect those in the mathematical type this C++ type is attempting to approximate.

1. If **a** and **b** initially have the same value, and
2. the same operation is applied to each object, then
3. (absent any *exceptions* or *undefined behavior*)
4. **both objects will again have the same value!**

2. Understanding Value Semantics

Value-Semantic Properties

QUESTION:

What makes two unordered containers represent the same value?



Think about a bag of Halloween candy.

2. Understanding Value Semantics

Value-Semantic Properties

Note that this essential property applies only to objects of the *same type*:

<code>int x = 5;</code>	<code>int y = 5;</code>	<code>assert(x == y);</code>
<code>x *= x;</code>	<code>y *= y;</code>	<code>assert(x == y);</code>
<code>x *= x;</code>	<code>y *= y;</code>	<code>assert(x == y);</code>
<code>x *= x;</code>	<code>y *= y;</code>	<code>assert(x == y);</code>
<code>⋮</code>	<code>⋮</code>	<code>⋮</code>

2. Understanding Value Semantics

Value-Semantic Properties

Note that this essential property applies only to objects of the *same type*:

```
int x = 5; short y = 5; assert(x == y);
```

$x^* = x$; $y^* = y$; `assert(x == y);`

```
x *= x;      y *= y;      assert(x == y);
```

```
x *= x;      y *= y;      .assert(x == y);
```

Undefined Behavior!

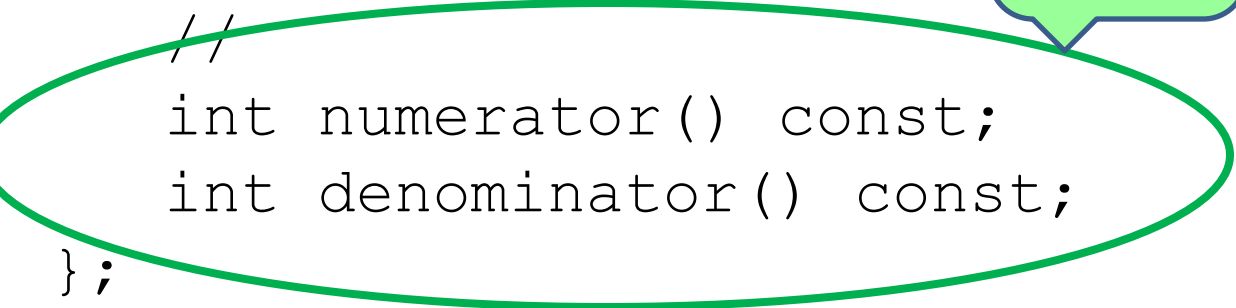

How do we
design proper
value types?

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

```
class Rational {  
    int d_numerator;  
    int d_denominator;  
public:  
    //  
    int numerator() const;  
    int denominator() const;  
};  
// ...  
bool operator==(const Rational& lhs,  
                 const Rational& rhs);
```



2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes



What about

numerator() / denominator()
as the salient attribute?

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes



What about

`numerator()` / `denominator()`
as the salient attribute?

```
bool operator==(const Rational& lhs,  
                const Rational& rhs);  
// Two 'Rational' objects have the same value if  
// the ratio of the values of 'numerator()' and  
// 'denominator ()' for 'lhs' is the same as that for 'rhs'.
```

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes



What about

numerator () / denominator ()
as the salient attribute?

$$\frac{1}{2} = \frac{2}{4} ?$$

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes



What about

numerator () / denominator ()
as the salient attribute?

$$\frac{1}{\cancel{0}} = = \frac{2}{\cancel{0}} ?$$

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes



What about

numerator () / denominator ()
as the salient attribute?

$$\frac{1}{2} = = \frac{-1}{-2} ?$$

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes



What about

numerator () / denominator ()
as the salient attribute?

$$\frac{1}{2} = = \frac{100}{200} \quad ?$$

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes



What about

numerator () / denominator ()
as the salient attribute?

$$\left[\frac{1}{2} \right]^{10} = \left[\frac{100}{200} \right]^{10} ?$$

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes



What about

~~numerator() / denominator()~~

as the salient attribute?

$$\left[\frac{1}{2} \right]^{10} = \left[\frac{100}{200} \right]^{10} ?$$

VIOLATES SUBTLE ESSENTIAL PROPERTY OF VALUE

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes



If you choose to make

`numerator()` / `denominator()`

a salient attribute

(probably a bad idea)

then do not expose numerator and
denominator as separate attributes...

2. Understanding Value Semantics

Value-Semantic Properties

...or maintain them in
“canonical form” (which
may be computationally
expensive).



(probably a bad idea)

then do not expose numerator and denominator as separate attributes...

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

Guideline

If two objects have *the same* value then the values of each ***observable attribute*** that ***contributes to value*** should respectively ***compare equal***.

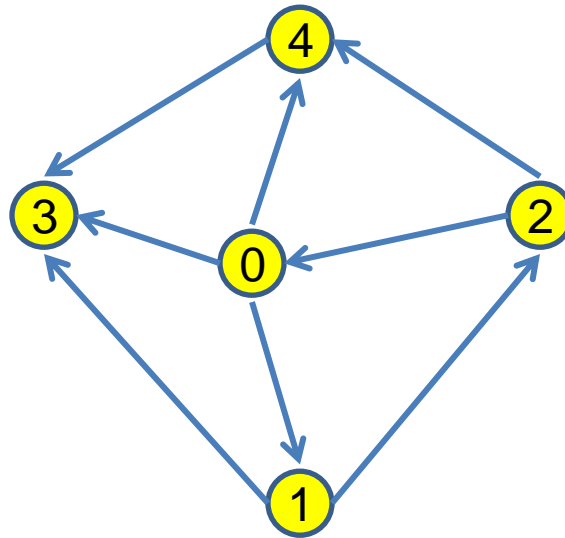
When should
we omit valid
value syntax?

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

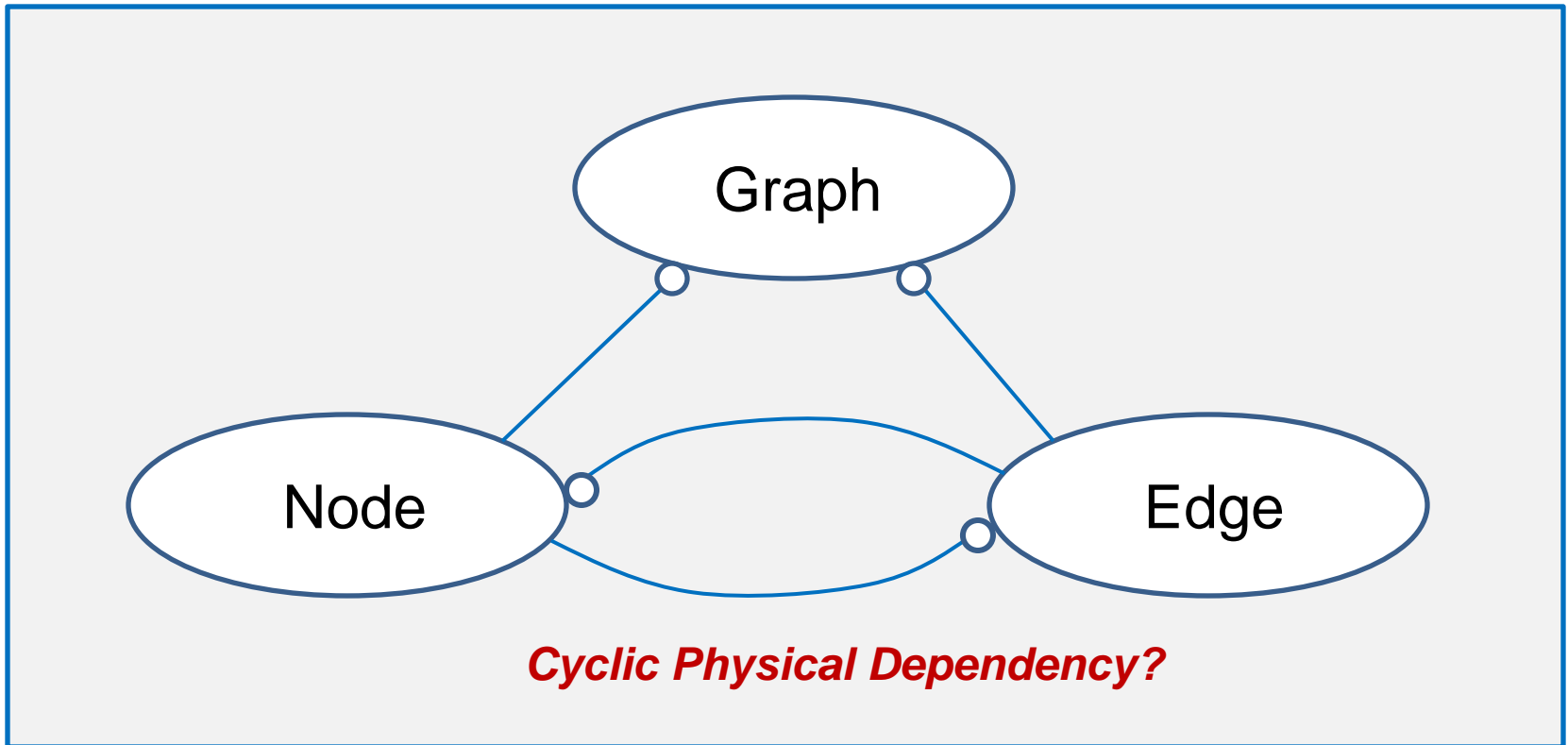
Graphs



2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

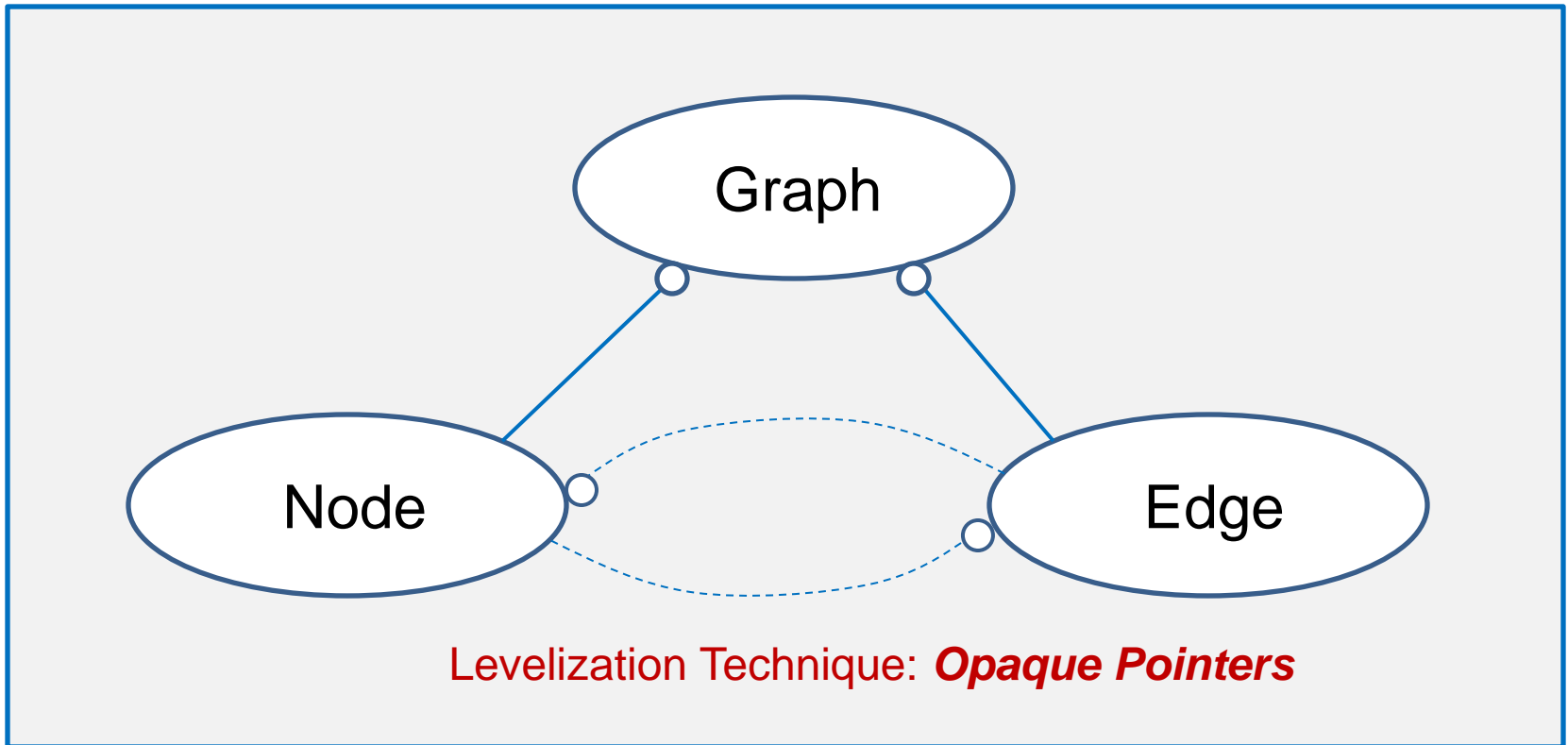


graph

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

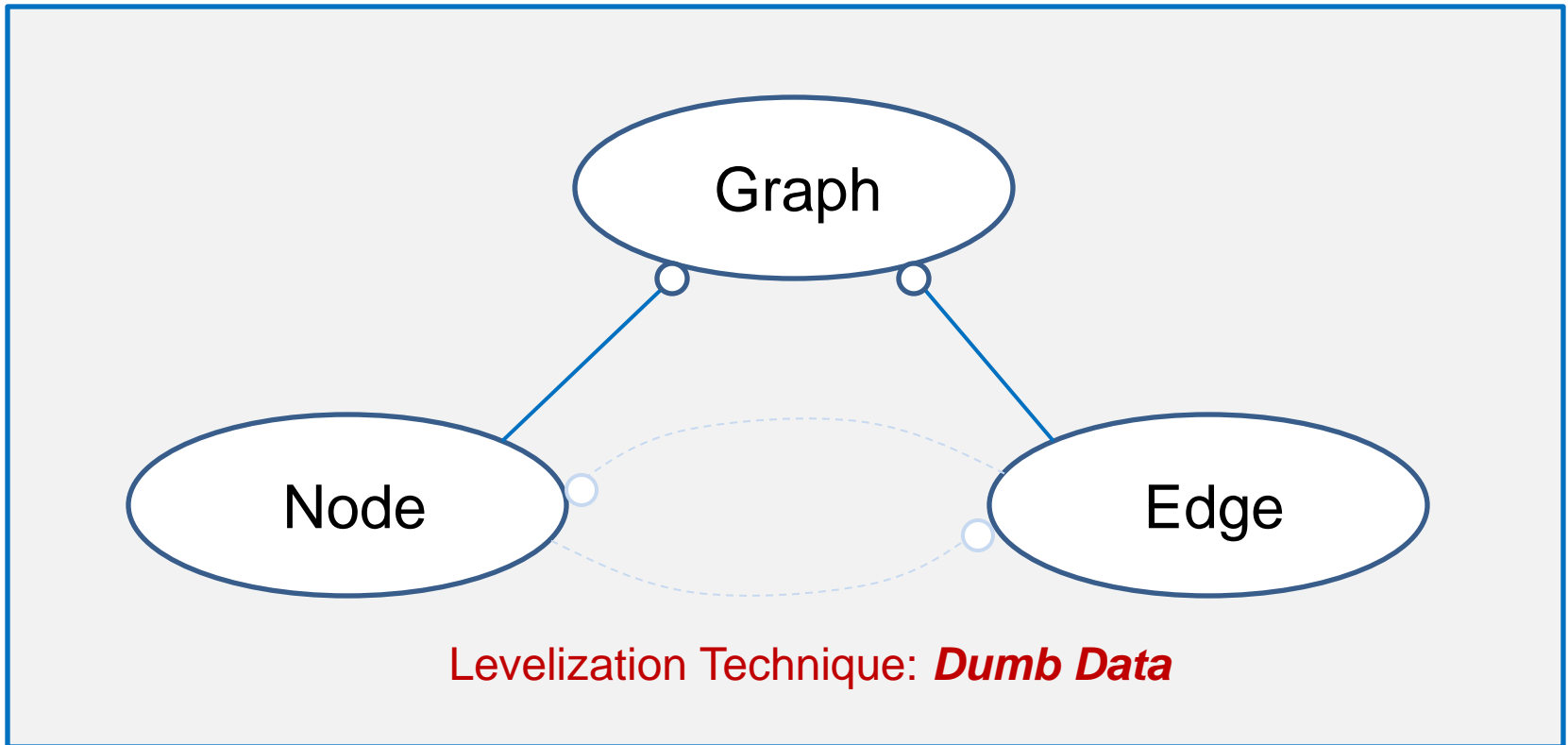


graph

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

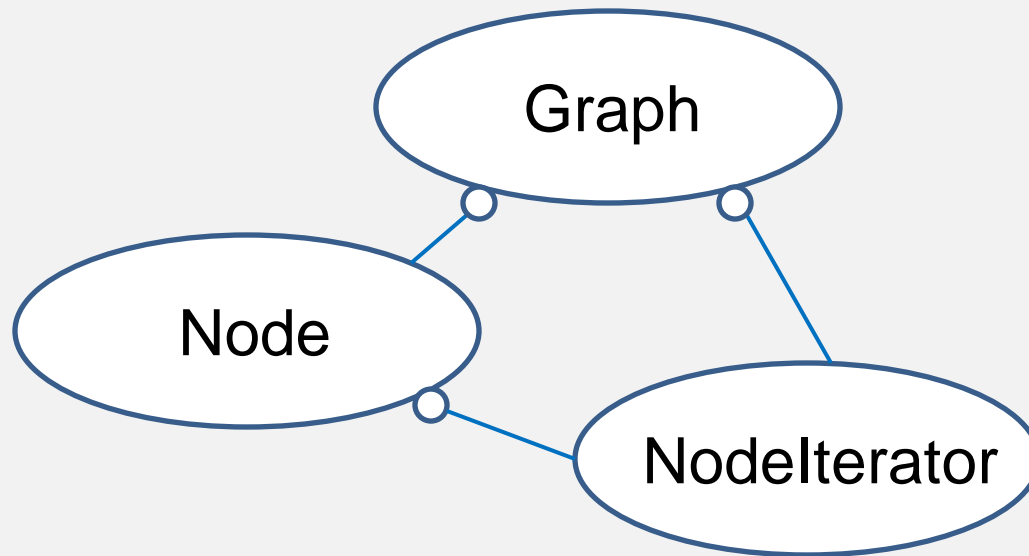


graph

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes



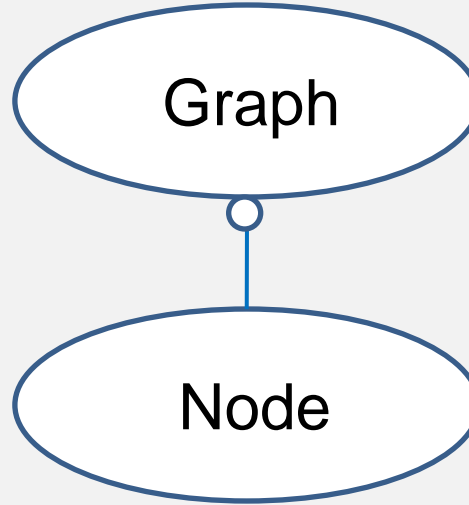
Simpler Design: ***No Explicit Edge Object***

graph

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes



Yet Simpler Design: ***No Explicit NodeIterator***

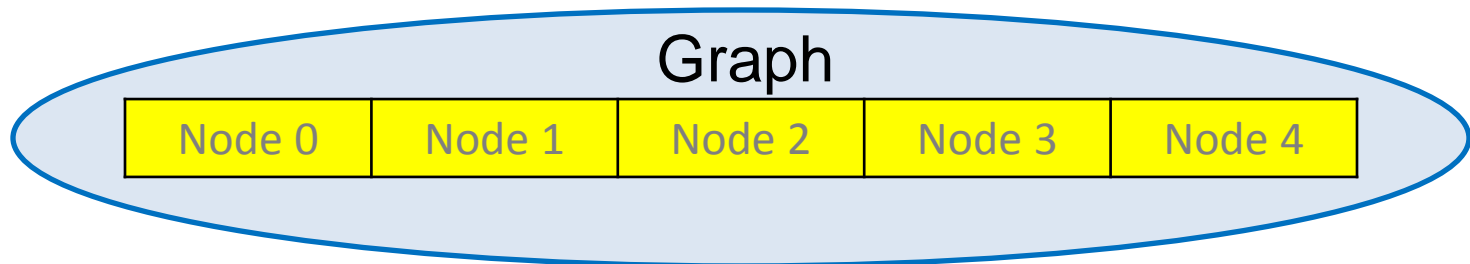
graph

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

```
class Graph {  
    // ...  
public:  
    // ...  
    int numNodes() const;  
    const Node& node(int index) const;  
};  
// ...
```

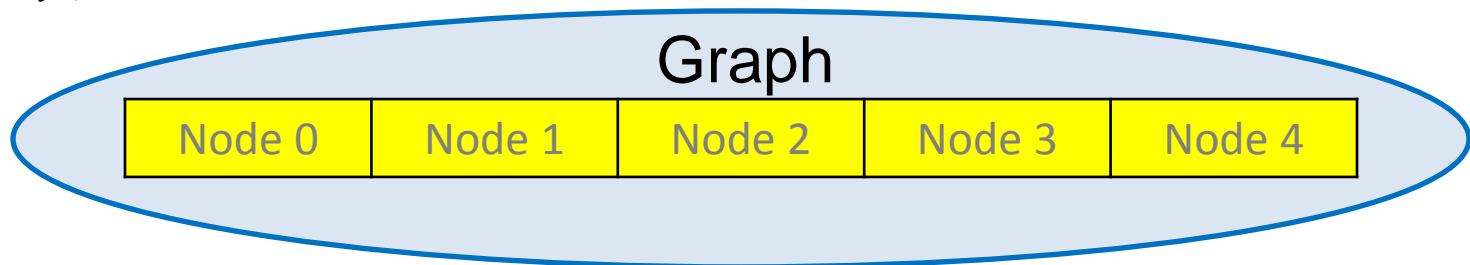


2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

```
class Node {  
    // ...  
public:  
    // ...  
    int nodeIndex() const;  
    int numAdjacentNodes() const;  
    Node& adjacentNode(int index) const;  
};
```



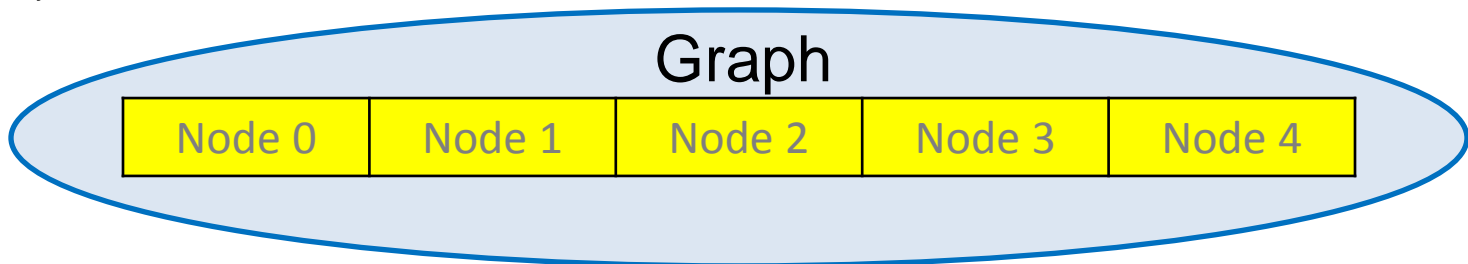
2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

```
class Node {  
    // ...  
public:  
    // ...  
    int nodeIndex() const;  
    int numAdjacentNodes() const;  
    Node& adjacentNode(int index) const;  
};
```

Really should be
declared `const` but
there's no room!

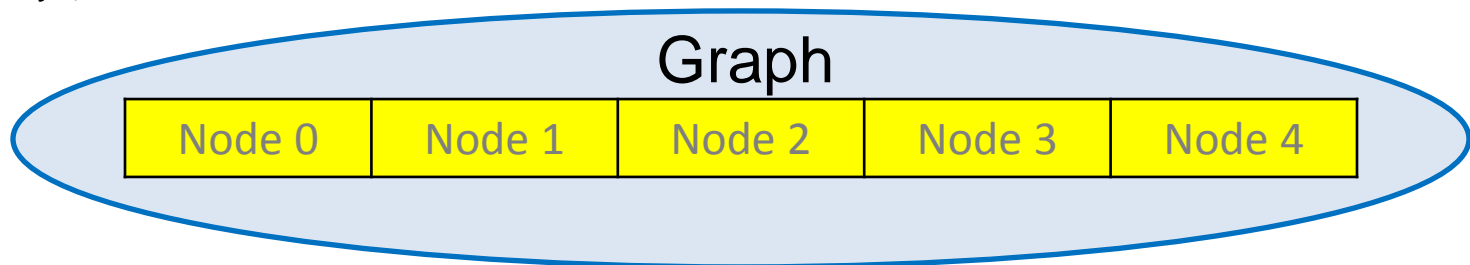


2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

```
class Node {  
    // ...  
public:  
    // ...  
    int nodeIndex() const;  
    int numAdjacentNodes() const;  
    Node& adjacentNode(int index) const;  
};
```

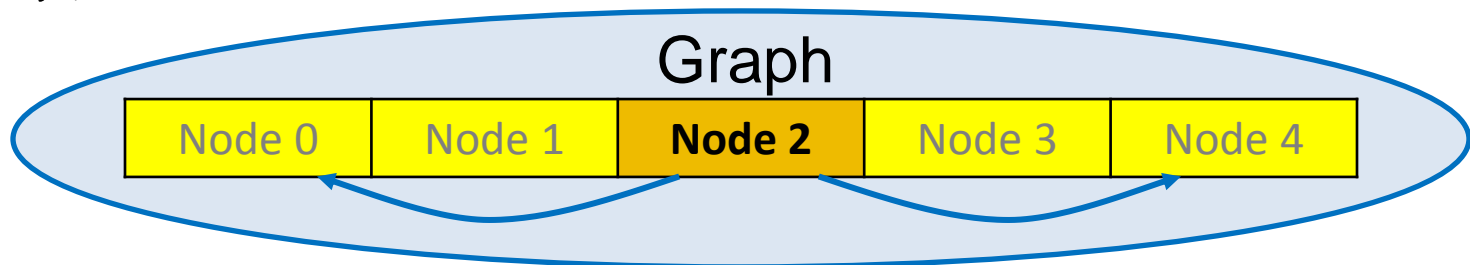
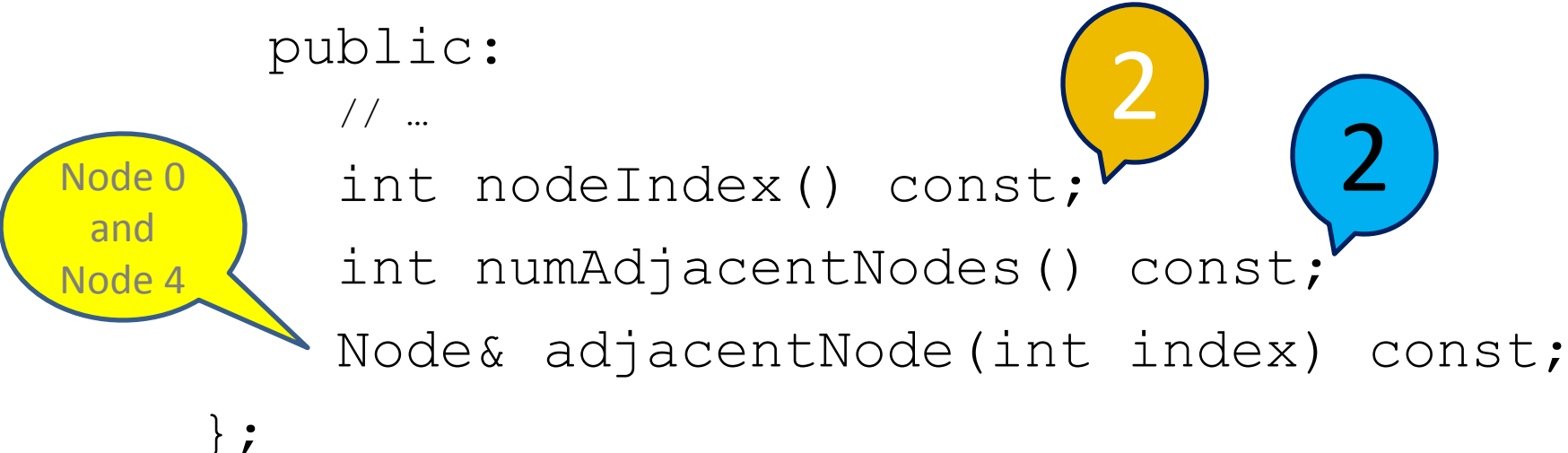


2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

```
class Node {  
    // ...  
public:  
    // ...  
    int nodeIndex() const;  
    int numAdjacentNodes() const;  
    Node& adjacentNode(int index) const;  
};
```



2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

```
class Graph {  
    // ...  
public:  
    // ...  
    int numNodes() const;  
    const Node& node(int index) const;  
};  
// ...  
bool operator==(const Graph& lhs,  
                 const Graph& rhs);
```

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

```
class Graph {  
    // ...  
public:  
    // ...  
    int numNodes() const;  
    const Node& node(int index) const;  
};  
// ...  
bool operator==(const Graph& lhs,  
                 const Graph& rhs);  
    // Two 'Graph' objects have the same  
    // value if ...???
```

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

What are the salient attributes of `Graph`?

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

What are the salient attributes of `Graph`?

- Number of nodes.

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

What are the salient attributes of `Graph`?

- Number of nodes.
- Number of edges.

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

What are the salient attributes of `Graph`?

- Number of nodes.
- Number of edges.
- Number of nodes adjacent to each node.

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

What are the salient attributes of `Graph`?

- Number of nodes.
- Number of edges.
- Number of nodes adjacent to each node.

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

What are the salient attributes of `Graph`?

- Number of nodes.
- Number of edges.
- Number of nodes adjacent to each node.
- Specific nodes adjacent to each node.

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

What are the salient attributes of `Graph`?

- Number of nodes.
- Number of edges.
- Number of nodes adjacent to each node.
- Specific nodes adjacent to each node.

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

```
bool operator==(const Graph& lhs,  
                const Graph& rhs);  
// Two 'Graph' objects have the same  
// value if
```

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

```
bool operator==(const Graph& lhs,  
                const Graph& rhs);  
// Two 'Graph' objects have the same  
// value if they have the same number of  
// nodes 'N' and,
```

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

```
bool operator==(const Graph& lhs,  
                const Graph& rhs);  
// Two 'Graph' objects have the same  
// value if they have the same number of  
// nodes 'N' and, for each node index 'i'  
// '(0 <= i < N)',
```


2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

```
bool operator==(const Graph& lhs,  
                const Graph& rhs);  
// Two 'Graph' objects have the same  
// value if they have the same number of  
// nodes 'N' and, for each node index 'i'  
// '(0 <= i < N)', the nodes adjacent to  
// node 'i' in 'lhs' have the same  
// indices as those of the nodes  
// adjacent to node 'i' in 'rhs'.
```

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

```
class Node {  
    // ...  
public:  
    // ...  
    int nodeIndex() const;  
    int numAdjacentNodes() const;  
    Node& adjacentNode(int index) const;  
};
```

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

```
class Node {  
    // ...  
public:  
    // ...  
    int nodeIndex() const;  
    int numAdjacentNodes() const;  
    Node& adjacentNode(int index) const;  
};
```

Maintained in
sorted order?

Is “edge” order a *salient attribute*?

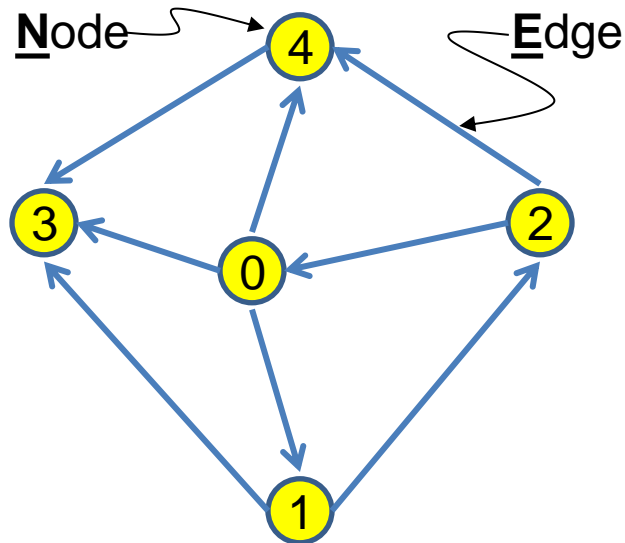
2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

Unordered Edges

0: 4 1 3
1: 3 2
2: 0 4
3:
4: 3



Ordered Edges

0: 1 3 4
1: 2 3
2: 0 4
3:
4: 3

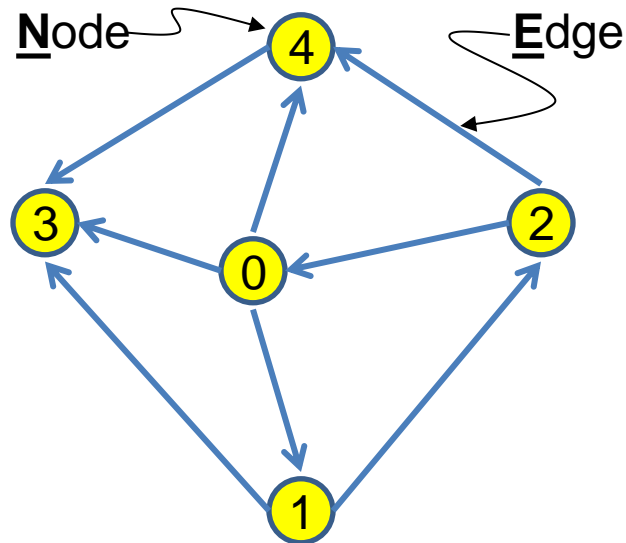
2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

Unordered Edges

0: 4 1 3
1: 3 2
2: 0 4
3:
4: 3



Ordered Edges

0: 1 3 4
1: 2 3
2: 0 4
3:
4: 3

?

O[operator==]

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

Unordered Edges

0: 4 1 3

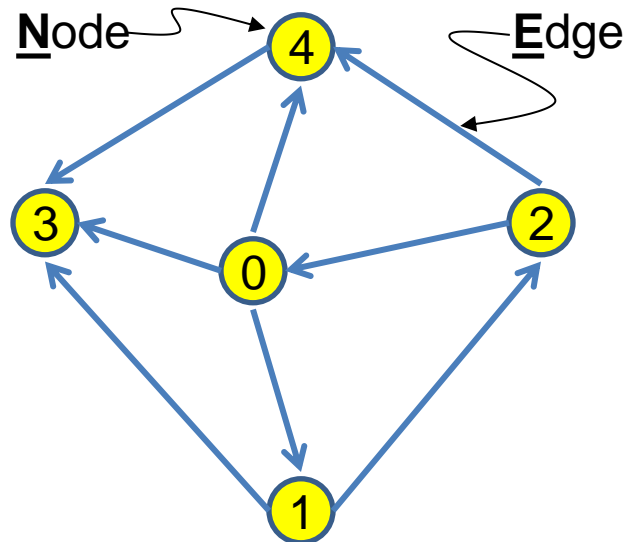
1: 3 2

2: 0 4

3:

4: 3

$O[N + E^2]$



Ordered Edges

0: 1 3 4

1: 2 3

2: 0 4

3:

4: 3

?

$O[\text{operator}==]$

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

Unordered Edges

0: 4 1 3

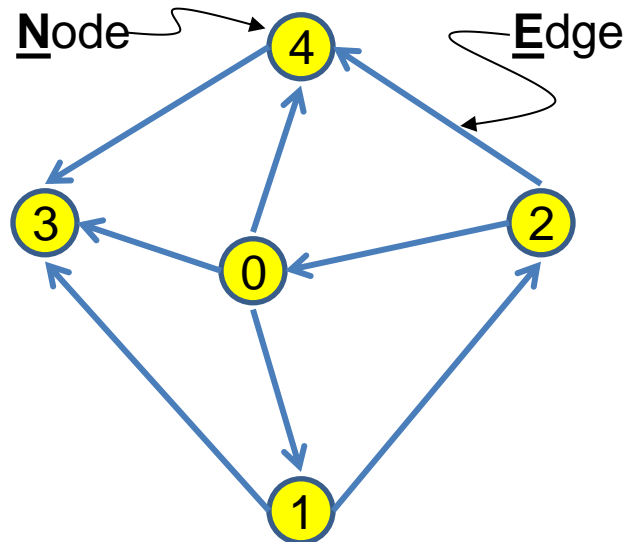
1: 3 2

2: 0 4

3:

4: 3

$O[N + E^2]$



?

$O[\text{operator}==]$

Ordered Edges

0: 1 3 4

1: 2 3

2: 0 4

3:

4: 3

$O[N + E]$

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

Unordered Edges

0: 4 1 3

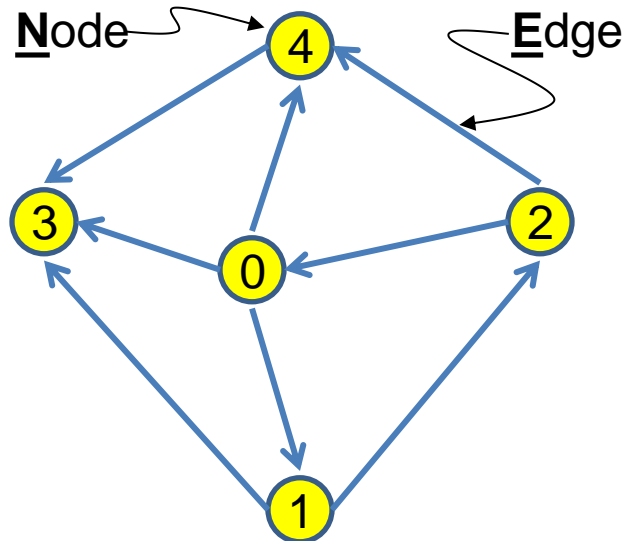
1: 3 2

2: 0 4

3:

4: 3

$O[N + E^2]$



?

$O[\text{operator}==]$

Ordered Edges

0: 1 3 4

1: 2 3

2: 0 4

3:

4: 3

$O[N + E]$

Note that we *could* make it $O[N + E * \text{Log}(E)]$.

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

Unordered Edges

0: 4 1 3

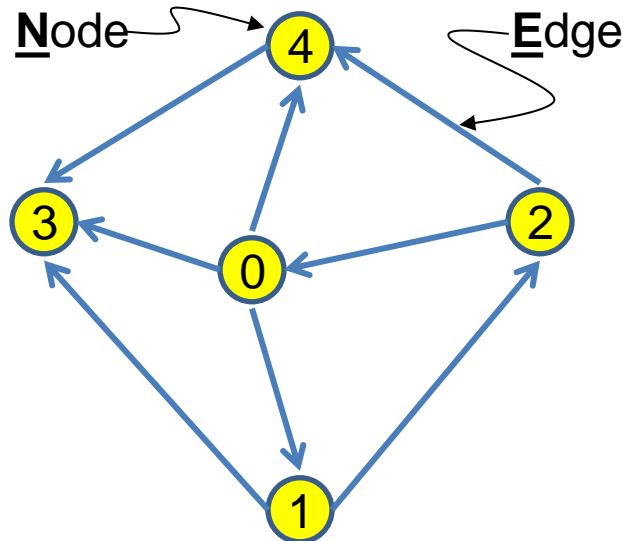
1: 3 2

2: 0 4

3:

4: 3

$O[N + E^2]$



?

$O[\text{operator}==]$

Ordered Edges

0: 1 3 4

1: 2 3

2: 0 4

3:

4: 3

$O[N + E]$

Note that we ~~could~~ make it $O[N + E * \text{Log}(E)]$.

2. Understanding Value Semantics

Value-Semantic Properties

OBSERVATION

2. Understanding Value Semantics

Value-Semantic Properties

OBSERVATION

Value Syntax: **Not all or nothing!**

2. Understanding Value Semantics

Value-Semantic Properties

OBSERVATION

Value Syntax: **Not all or nothing!**

An `std::set<int>` is a *value-semantic* type.

2. Understanding Value Semantics

Value-Semantic Properties

OBSERVATION

Value Syntax: **Not all or nothing!**

An `std::set<int>` is a *value-semantic* type.

An `std::unordered_set<int>` is a *value-semantic* type,

2. Understanding Value Semantics

Value-Semantic Properties

OBSERVATION

Value Syntax: **Not all or nothing!**

An `std::set<int>` is a *value-semantic* type.

An `std::unordered_set<int>` is a *value-semantic* type, **except that – until 2010 – it did not provide an** `operator==`.

2. Understanding Value Semantics

Value-Semantic Properties

OBSERVATION

Value Syntax: **Not all or nothing!**

An `std::set<int>` is a *value-semantic* type.

An `std::unordered_set<int>` is a *value-semantic* type, **except that – until 2010 – it did not provide an `operator==`.**

In large part due to performance concerns!

2. Understanding Value Semantics

Value-Semantic Properties

OBSERVATION

Value Syntax: Not all or nothing!

NOT REGULAR!

`unordered_set<int>` is a *value-semantic* type, **except that** – until 2010 – it did **not provide an** `operator==`.

In large part due to performance concerns!

2. Understanding Value Semantics

Value-Semantic Properties

OBSERVATION

Excellent
Starting
Point!

NO

AR!

semantic

not pro

In large p

value-

it did

ncerns!

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

What are the salient attributes of `Graph`?

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

What are the salient attributes of `Graph`?

✓ **Number of nodes.**

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

What are the salient attributes of `Graph`?

- ✓ Number of nodes.
- ✓ Specific nodes adjacent to each node.

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

What are the salient attributes of `Graph`?

- ✓ Number of nodes.
- ✓ Specific nodes adjacent to each node.

X Not adjacent-node (i.e., edge) order.

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

What are the salient attributes of Graph?

- ✓ Number of nodes.
- ✓ Specific nodes adjacent to each node.

✗ Not adjacent-node (i.e., edge) order.

➤ **What about node indices?**

(I.e., the numbering of the nodes)

2. Understanding Value Semantics

Value-Semantic Properties

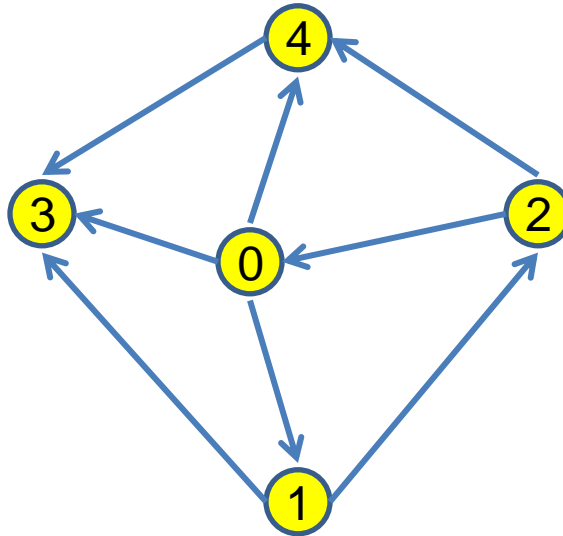
Selecting Salient Attributes

```
bool operator==(const Graph& lhs,
                const Graph& rhs);
// Two 'Graph' objects have the same
// value if they have the same number of
// nodes 'N' and there exists a renumbering
// of the nodes in 'rhs' such that, for
// each node-index 'i' '(0 <= i < N)',
// the nodes adjacent to node 'i' in 'lhs'
// have the same indices as those of the
// nodes adjacent to node 'i' in 'rhs'.
```

2. Understanding Value Semantics

Value-Semantic Properties

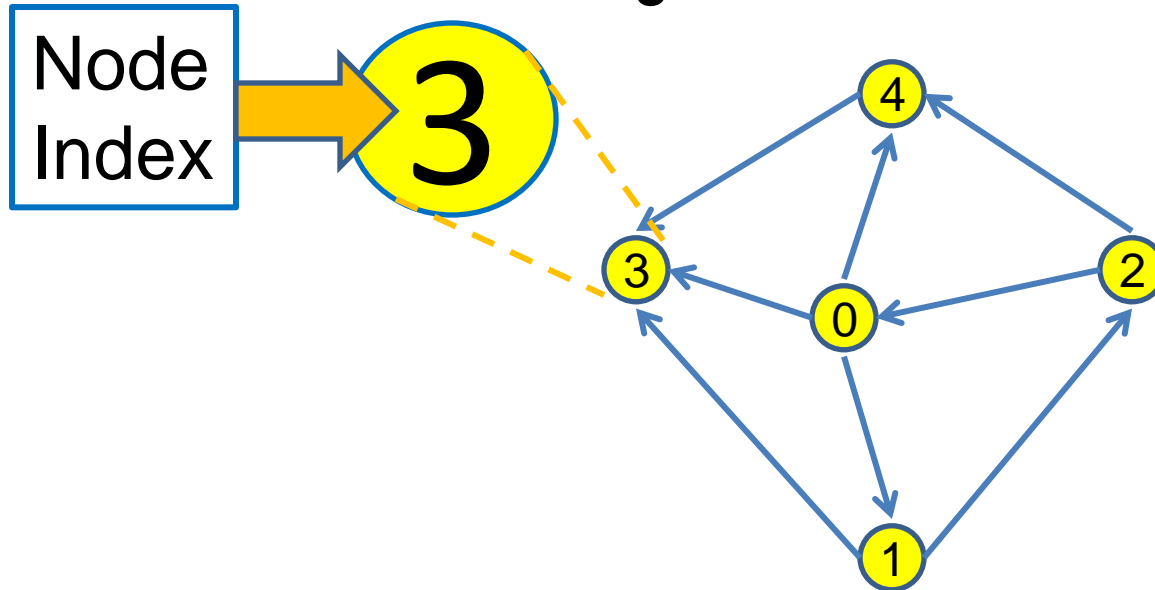
Selecting Salient Attributes



2. Understanding Value Semantics

Value-Semantic Properties

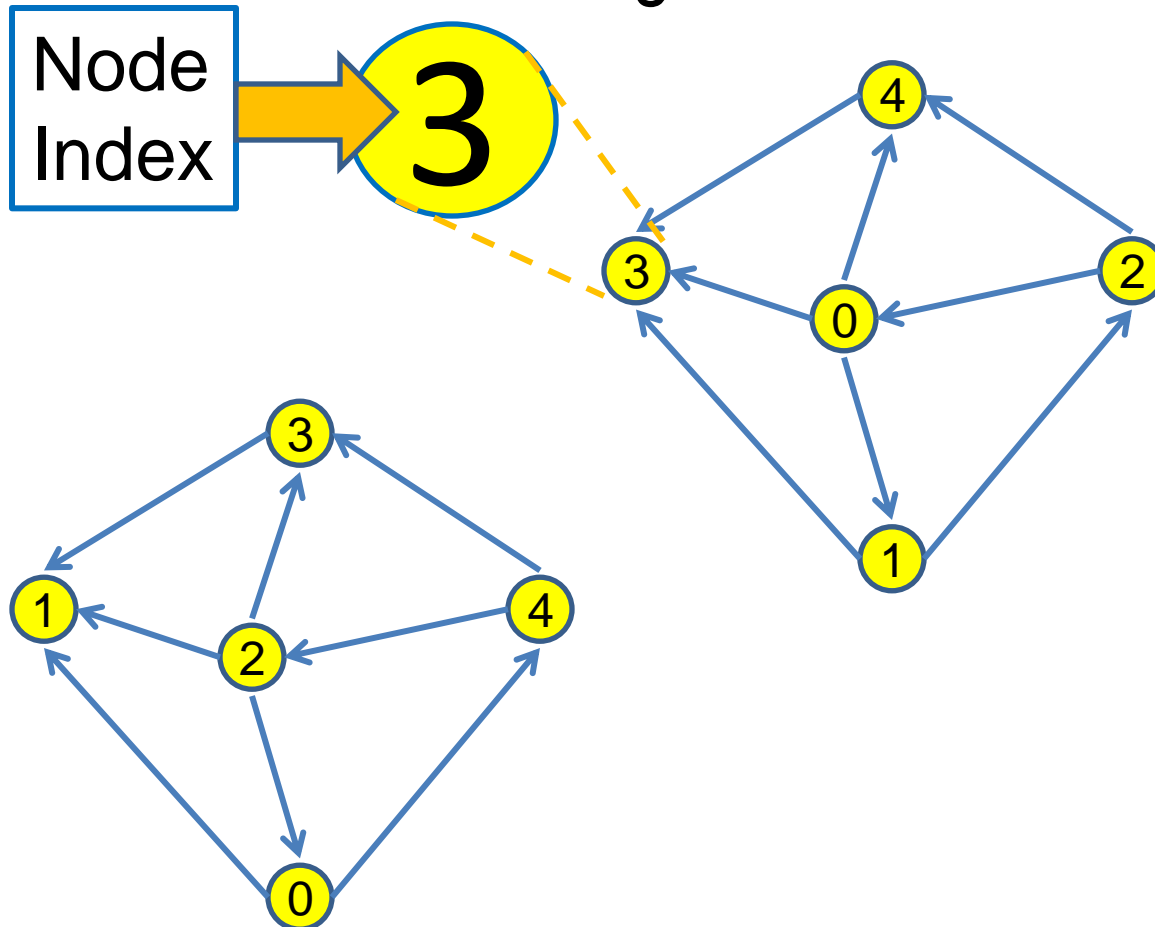
Selecting Salient Attributes



2. Understanding Value Semantics

Value-Semantic Properties

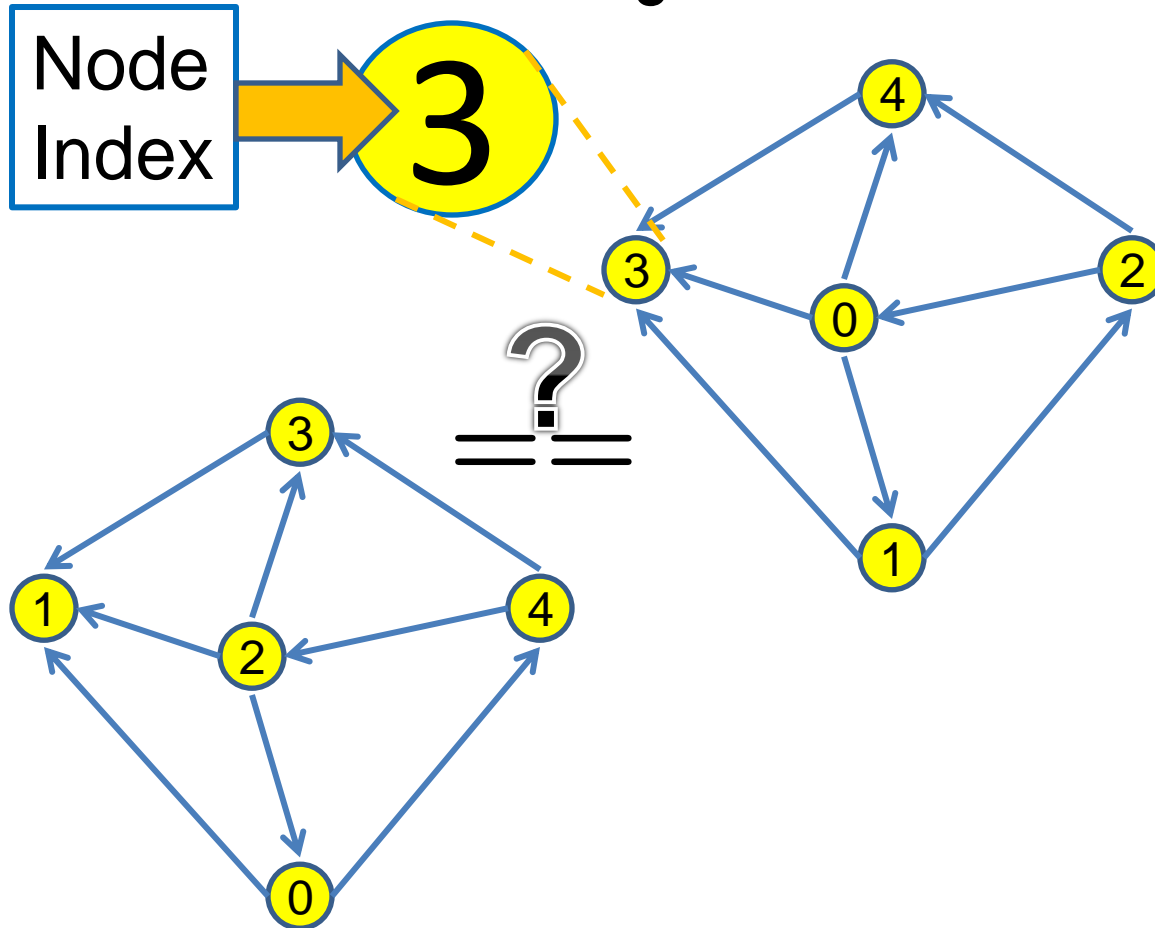
Selecting Salient Attributes



2. Understanding Value Semantics

Value-Semantic Properties

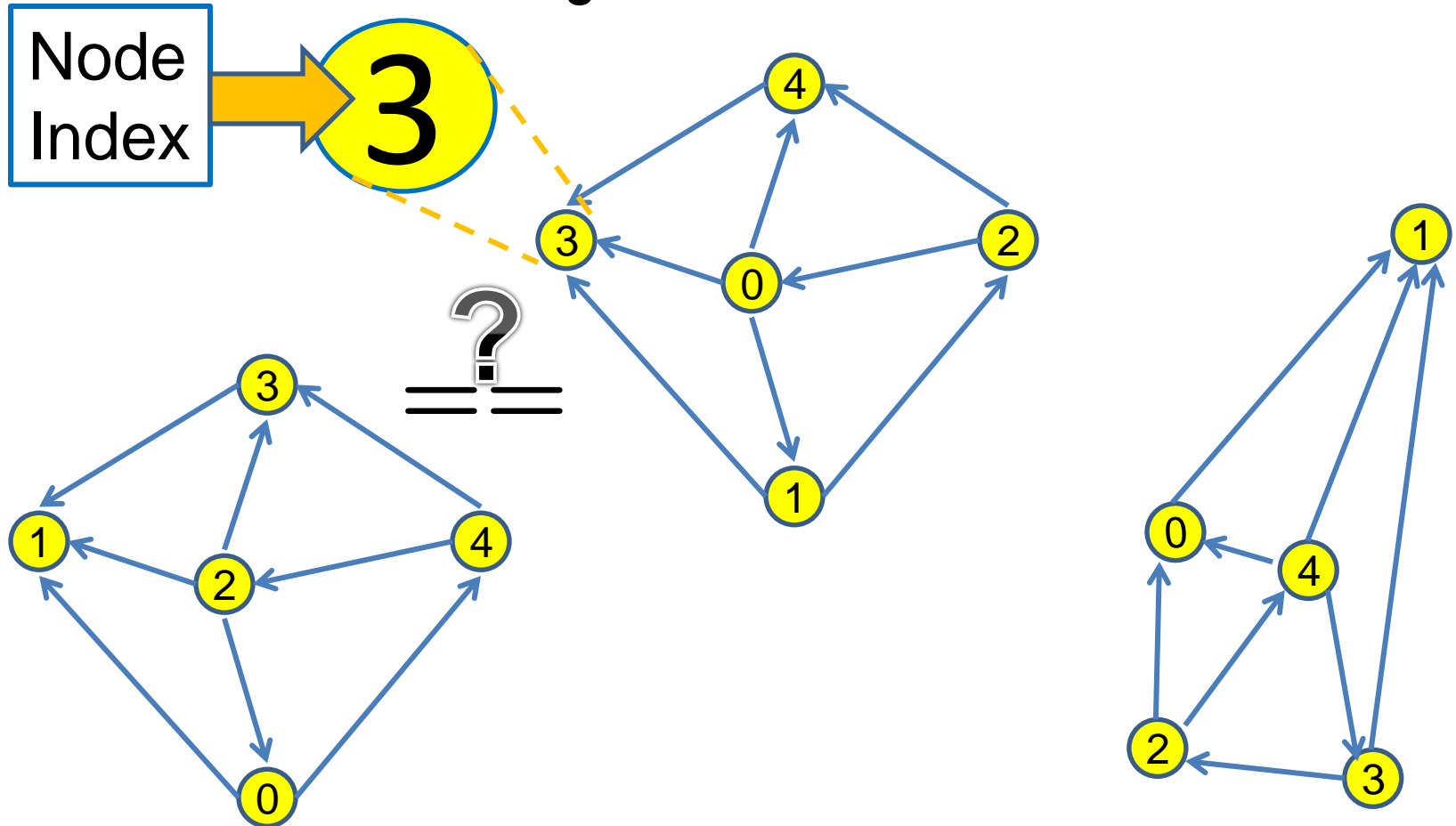
Selecting Salient Attributes



2. Understanding Value Semantics

Value-Semantic Properties

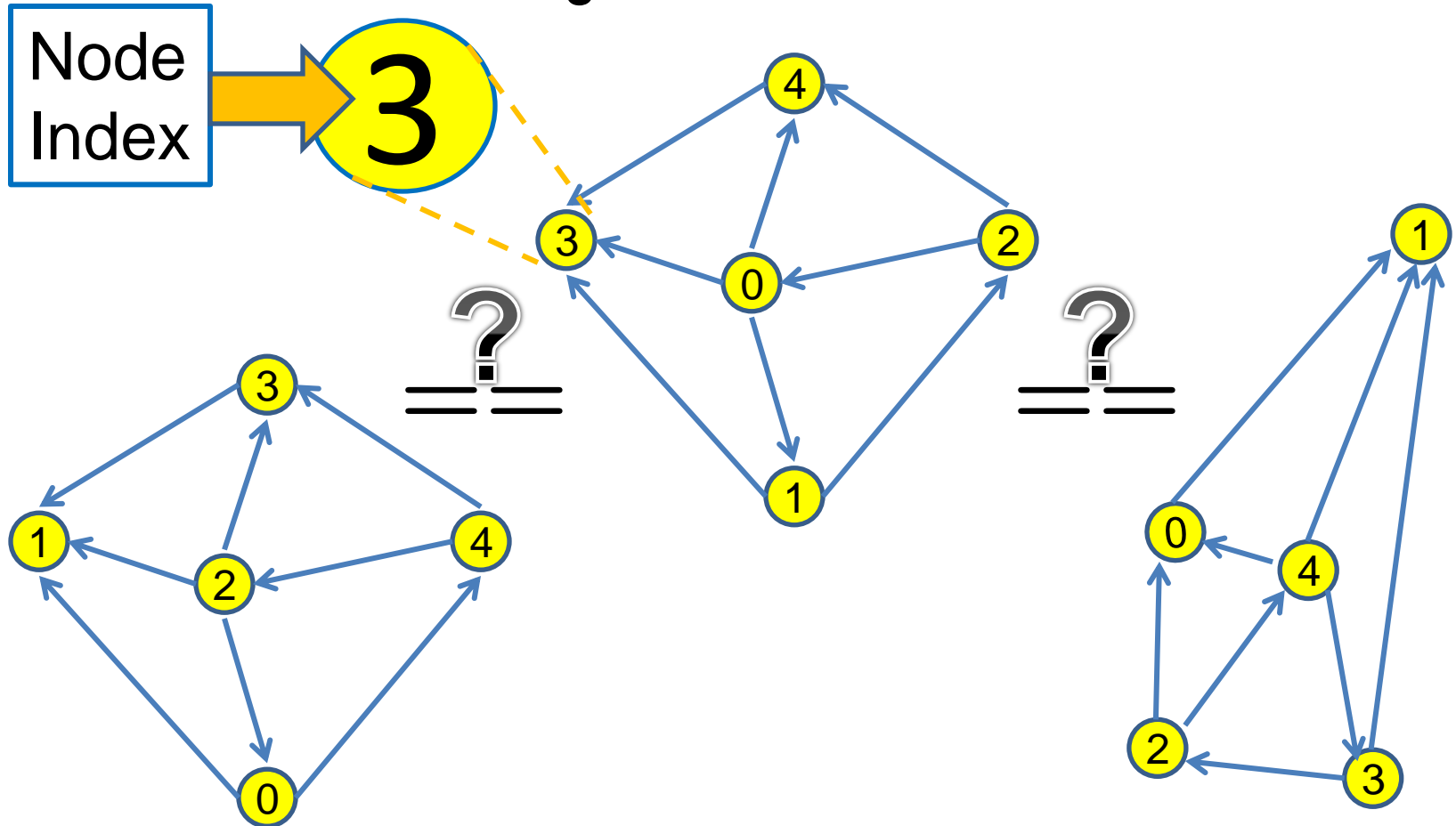
Selecting Salient Attributes



2. Understanding Value Semantics

Value-Semantic Properties

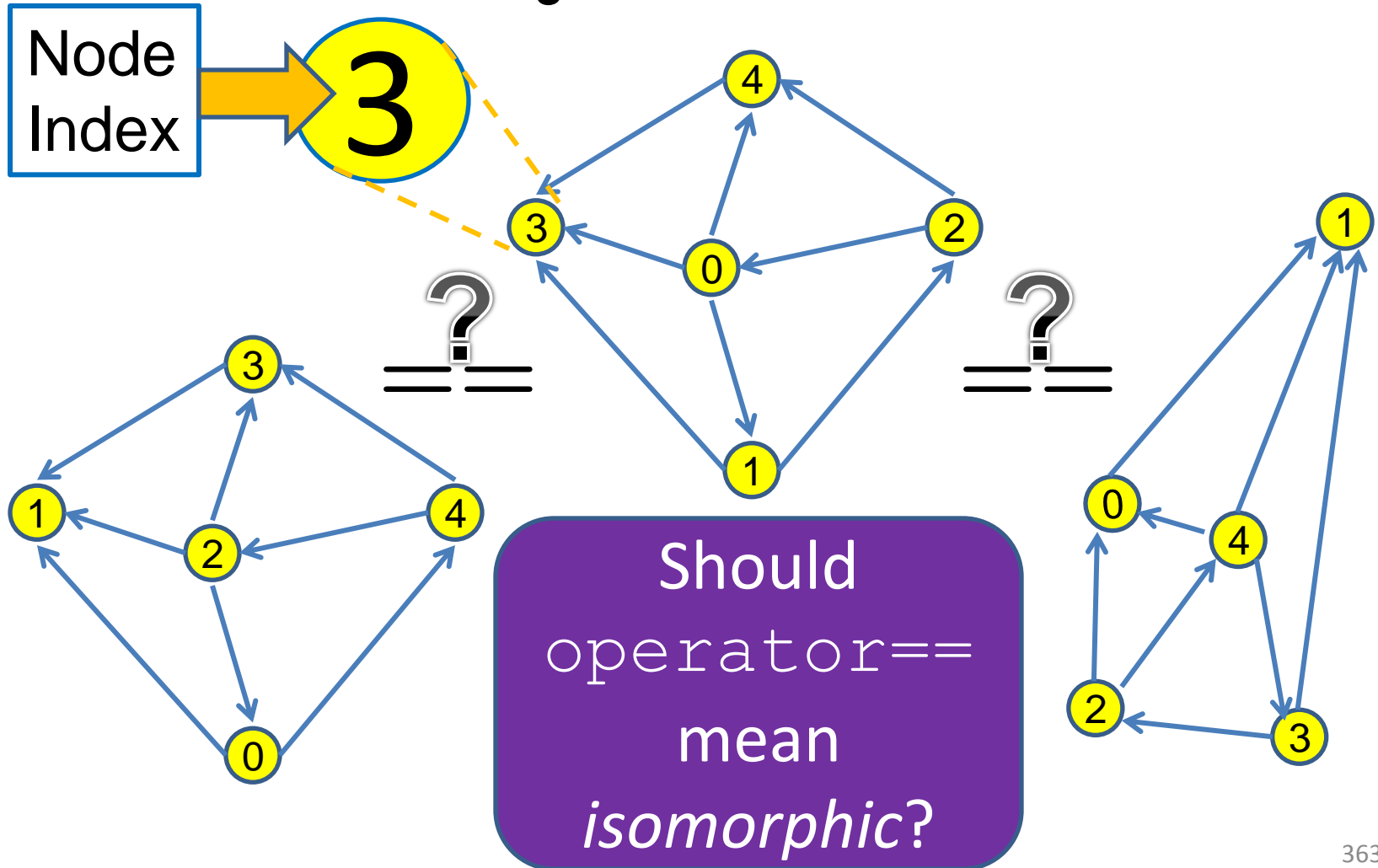
Selecting Salient Attributes



2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

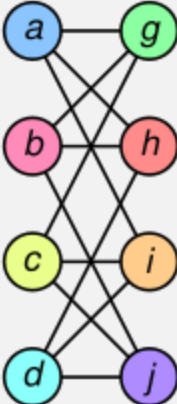
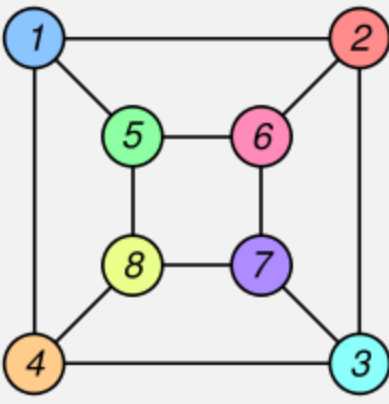


2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

In graph theory, an **isomorphism of graphs*** G and H is a bijection f between the vertex sets of G and H such that any two vertices u and v of G are adjacent in G if and only if $f(u)$ and $f(v)$ are adjacent in H .

Graph G	Graph H	An isomorphism between G and H
		$\begin{aligned} f(a) &= 1 \\ f(b) &= 6 \\ f(c) &= 8 \\ f(d) &= 3 \\ f(g) &= 5 \\ f(h) &= 2 \\ f(i) &= 4 \\ f(j) &= 7 \end{aligned}$

*http://en.wikipedia.org/wiki/Graph_isomorphism

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

How hard is it to determine

Graph Isomorphism?

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

How hard is it to determine

Graph Isomorphism?

Is known to be in NP *and* CO-NP.

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

How hard is it to determine

Graph Isomorphism?

Is known to be in NP *and* CO-NP.

Not known to be NP Complete.

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

How hard is it to determine

Graph Isomorphism?

Is known to be in NP *and* CO-NP.

Not known to be NP Complete.

Not known to be in P (Polynomial time).

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

How hard is it to determine

Graph Isomorphism?

Is known to be in NP and CO-NP.

Not known to be NP Complete.

Not known to be in P (Polynomial time).

It's Hard!

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

```
bool operator==(const Graph& lhs,
                const Graph& rhs);
// Two 'Graph' objects have the same
// value if they have the same number of
// nodes 'N' and there exists a renumbering
// of the nodes in 'rhs' such that, for
// each node-index 'i' '(0 <= i < N)',
// the nodes adjacent to node 'i' in 'lhs'
// have the same indices as those of the
// nodes adjacent to node 'i' in 'rhs'.
```

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

```
bool operator==(const Graph& lhs,
                const Graph& rhs);
// Two 'Graph' objects have the same
// value if they have the same number of
// nodes 'N' and there exists a renumbering
// of the nodes in 'rhs' such that, for
// each node-index 'i' '(0 <= i < N)',
// the nodes adjacent to node 'i' in 'lhs'
// have the same indices as those of the
// nodes adjacent to node 'i' in 'rhs'.
```

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

```
bool operator==(const Graph& lhs,  
                const Graph& rhs);  
// Two 'Graph' objects have the same  
// value if they have the same number of  
// nodes 'N' and, for each node-index 'i'  
// '(0 <= i < N)', the ordered sequence  
// of nodes adjacent to node 'i' in  
// 'lhs' has the same value as the one  
// for node 'i' in 'rhs'.
```

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

What are the salient attributes of `Graph`?

- ✓ Number of nodes.
- ✓ Specific nodes adjacent to each node.

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

What are the salient attributes of `Graph`?

- ✓ Number of nodes.
- ✓ Specific nodes adjacent to each node.

And, as a practical matter,

- ✓ *Numbering of the nodes.*

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

Or else we Must Omit
Equality Comparison
Operators for this Class!

✓ *Numbering of the nodes.*

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

Or else we Must Omit
Equality Comparison
Operators for this Class!

✓ *Numbering of the nodes.*

AND PERHAPS PROVIDE THIS
FUNCTIONALITY IN A UTILITY

2. Understanding Value Semantics

Discussion

Why would we ever omit valid value syntax when there is only one obvious notion of value?

2. Understanding Value Semantics

Discussion

Why would we ever
omit valid value
syntax when the

**When We Cannot
Do It Efficiently!**

2. Understanding Value Semantics

Discussion

Why would we ever
omit valid value
syntax when there

**When Doing So
Is “Off Message!”**

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

(Summary So Far)

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

(Summary So Far)

When selecting *salient* attributes, avoid subjective (domain-specific) interpretation:

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

(Summary So Far)

When selecting *salient* attributes, avoid subjective (domain-specific) interpretation:

➤ Fractions may be **equivalent**, but not **the same**.

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

(Summary So Far)

When selecting *salient* attributes, avoid subjective (domain-specific) interpretation:

- Fractions may be *equivalent*, but not *the same*.
- Graphs may be *isomorphic*, yet *distinct*.

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

(Summary So Far)

When selecting *salient* attributes, avoid subjective (domain-specific) interpretation:

- Fractions may be *equivalent*, but not *the same*.
- Graphs may be *isomorphic*, yet *distinct*.
- Triangles may be *similar* and still *differ*.

DON'T “EDITORIALIZE” EQUALITY

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

(Summary So Far)

Relegate any “subjective interpretations” of *equality* to **named functions!**

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

(Summary So Far)

Relegate any “subjective interpretations” of *equality* to *named functions* – ideally, in *higher-level* components:

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

(Summary So Far)

Relegate any “subjective interpretations” of *equality* to *named functions* – ideally, in *higher-level* components:

```
struct MyUtil {  
    static bool areEquivalent(const Rational& a)  
                               const Rational& b);  
    static bool areIsomorphic(const Graph& g1,  
                              const Graph& g2);  
    static bool areSimilar(const Triangle& x,  
                           const Triangle& y);  
};
```

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

(Summary So Far)

Relegate any “subjective interpretations” of *equality* to *named functions* – ideally, in *higher-level* components:

```
struct MyUtil {  
    static bool areEquivalent(const Rational& a)  
                               const Rational& b);  
    static bool areIsomorphic(const Graph& g1,  
                              const Graph& g2);  
    static bool areSimilar(const Triangle& x,  
                           const Triangle& y);  
};
```

2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

(Summary So Far)

Relegate any “subjective interpretations” of *equality* to *named functions* – ideally, in *higher-level* components:

```
struct MyUtil {  
    static bool areEquivalent(const Rational& a)  
                                const Rational& b);  
    static bool areIsomorphic(const Graph& g1,  
                                const Graph& g2);  
    static bool areSimilar(const Triangle& x,  
                                const Triangle& y);  
};
```


2. Understanding Value Semantics

Value-Semantic Properties

Selecting Salient Attributes

(Summary So Far)

Relegate any “subjective interpretations” of *equality* to named functions — ideally, in higher-level components:

```
struct MyUtil {  
    static bool areEquivalent(const Rational& a)  
                               const Rational& b);  
    static bool areIsomorphic(const Graphs  
                               const  
    static bool areSimilar(const Triangle& x,  
                             Triangle& y);  
};
```

Utility Class Category

2. Understanding Value Semantics

Value-Semantic Properties

A collateral benefit is Terminology:

Saying what we mean
facilitates understanding.

2. Understanding Value Semantics

Collateral Benefit: Terminology

“...objects are the same...”

“...objects are identical...”

“...objects are equal...”

“...objects are equivalent...”

“...create a copy of...”

2. Understanding Value Semantics

Collateral Benefit: Terminology

~~“...objects are the same...”~~

~~“...objects are identical...”~~

~~“...objects are equal...”~~

~~“...objects are equivalent...”~~

~~“...create a copy of...”~~

2. Understanding Value Semantics

Collateral Benefit: Terminology

BE PRECISE!

~~“...objects are the same...”~~

~~“...objects are identical...”~~

~~“...objects are equal...”~~

~~“...objects are equivalent...”~~

~~“...create a copy of...”~~

2. Understanding Value Semantics

Collateral Benefit: Terminology

BE PRECISE!

~~“...objects are the same...”~~

~~“...objects are identical...”~~

~~“...objects are equal...”~~

~~“...objects are equivalent...”~~

~~“...create a copy of...”~~

SAY EXACTLY *WHAT* MUST BE THE SAME!

2. Understanding Value Semantics

Collateral Benefit: Terminology

“...objects are the same...”

“...objects are identical...”

(identity)

2. Understanding Value Semantics

Collateral Benefit: Terminology

“...objects are the same...”

“...objects are identical...”

(identity)

“...(aliases) **refer to the same object...**”

2. Understanding Value Semantics

Collateral Benefit: Terminology

“...objects are the same...”
(value)

2. Understanding Value Semantics

Collateral Benefit: Terminology

“...objects are the same...”

(value)

“...(objects) **have the same value...**”

2. Understanding Value Semantics

Collateral Benefit: Terminology

“...objects are the same...”

(value)

“...(objects) **have the same value...**”

“...(objects) **refer to the same value...**”

2. Understanding Value Semantics

Collateral Benefit: Terminology

“...objects are the same...”

(value)

“...(objects) **have the same value...**”

“...(objects) **refer to the same value...**”

“...(objects) **represent the same value...**”

2. Understanding Value Semantics

Collateral Benefit: Terminology

“...objects are the same...”

“...objects are equal...”

(equality)

2. Understanding Value Semantics

Collateral Benefit: Terminology

“...objects are the same...”

“...objects are equal...”

(equality)

“... (objects) **compare equal**...”

2. Understanding Value Semantics

Collateral Benefit: Terminology

“...objects are the same...”

“...objects are equal...”

(equality)

“...(objects) **compare equal**...”

“...(homogeneous) `operator==` returns `true`...”

2. Understanding Value Semantics

Collateral Benefit: Terminology

“...objects are the same...”

“...objects are equal...”

(equality)

“...(objects) **compare equal**...”

“...(homogeneous) `operator==` returns `true`...”

For value-semantic objects:

2. Understanding Value Semantics

Collateral Benefit: Terminology

“...objects are the same...”

“...objects are equal...”

(equality)

“...(objects) **compare equal**...”

“...(homogeneous) `operator==` returns `true`...”

***For value-semantic objects:
Means have the same value!***

2. Understanding Value Semantics

Collateral Benefit: Terminology

“...objects are the same...”
(equivalent)

2. Understanding Value Semantics

Collateral Benefit: Terminology

“...objects are the same...”

(equivalent)

In separate *named* functions:

2. Understanding Value Semantics

Collateral Benefit: Terminology

“...objects are the same...”

(equivalent)

In separate named functions:

“...fractions are equivalent...”

2. Understanding Value Semantics

Collateral Benefit: Terminology

“...objects are the same...”

(equivalent)

In separate named functions:

“...fractions are equivalent...”

“...graphs are isomorphic...”

2. Understanding Value Semantics

Collateral Benefit: Terminology

“...objects are the same...”

(equivalent)

In separate named functions:

“...fractions are equivalent...”

“...graphs are isomorphic...”

“...triangles are similar...”

Outline

1. Introduction and Background

Components, Physical Design, and Class Categories

2. Understanding Value Semantics (and Syntax)

Most importantly, the Essential Property of Value

3. Two Important, Instructional Case Studies

Specifically, *Regular Expressions* and *Priority Queues*

4. Conclusion

What must be remembered when designing value types

Outline

1. Introduction and Background

Components, Physical Design, and Class Categories

2. Understanding Value Semantics (and Syntax)

Most importantly, the *Essential Property of Value*

3. Two Important, Instructional Case Studies

Specifically, *Regular Expressions* and *Priority Queues*

4. Conclusion

What must be remembered when designing value types

3. Two Important, Instructional Case Studies

Regular Expressions

Important Design Questions:

- What is a *Regular Expression*?
- Why create a separate class for it?
- Does/should it represent a value?
- How should its value be defined?
- Should such a class be *regular*?

3. Two Important, Instructional Case Studies

Regular Expressions

Important Design Questions:

- **What is a *Regular Expression*?**
- Why create a separate class for it?
- Does/should it represent a value?
- How should its value be defined?
- Should such a class be *regular*?

3. Two Important, Instructional Case Studies

Regular Expressions

What is a *Regular Expression*?

3. Two Important, Instructional Case Studies

Regular Expressions

What is a *Regular Expression*?

A Regular Expression describes a language that can be *accepted* by a Finite-State Machine (FSM).

3. Two Important, Instructional Case Studies

Regular Expressions

What is a *Regular Expression*?

A *Regular Expression* describes a language that can be *accepted* by a Finite-State Machine (FSM).

E.g.,

(1|0)+ describes binary numbers.

3. Two Important, Instructional Case Studies

Regular Expressions

Important Design Questions:

- What is a *Regular Expression*?
- **Why create a separate class for it?**
- Does/should it represent a value?
- How should its value be defined?
- Should such a class be *regular*?

3. Two Important, Instructional Case Studies

Regular Expressions

Why create a separate class for it?

3. Two Important, Instructional Case Studies

Regular Expressions

Why create a separate class for it?

A Regular-Expression class imbued with the value of a regular expression can be used to determine whether (or not) arbitrary string tokens are members of the language that the regular-expression value denotes.

3. Two Important, Instructional Case Studies

Regular Expressions

Why create a separate class for it?

```
class RegEx {  
    // ...  
public:  
    static bool isValid(const char *regEx);  
    RegEx();    // Empty language; accepts nothing.  
    RegEx(const char *regEx);  
    RegEx(const RegEx& other);  
    ~RegEx();  
    RegEx& operator=(const RegEx& rhs);  
    void setValue(const char *regEx);  
    int setValueIfValid(const char *regEx);  
    bool isMember(const char *token) const;  
};
```

3. Two Important, Instructional Case Studies

Regular Expressions

Why create a separate class for it?

```
class RegEx {  
    // ...  
public:  
    static bool isValid(const char *regEx);  
    RegEx(); // Empty language: Accepts nothing.  
    RegEx(const char *regEx);  
    RegEx(const RegEx& other);  
    ~RegEx();  
    RegEx& operator=(const RegEx& rhs);  
    void setValue(const char *regEx);  
    int setValueIfValid(const char *regEx);  
    bool isMember(const char *token) const;  
};
```



Class Methods

3. Two Important, Instructional Case Studies

Regular Expressions

Why create a separate class for it?

```
class RegEx {  
    // ...  
public:  
    static bool isValid(const char *regEx);  
    RegEx(); // Empty language: Accepts nothing.  
    RegEx(const char *regEx);  
    RegEx(const RegEx& other);  
    ~RegEx();  
    RegEx& operator=(const RegEx& rhs);  
    void setValue(const char *regEx);  
    int setValueIfValid(const char *regEx);  
    bool isMember(const char *token) const;  
};
```



Creators

3. Two Important, Instructional Case Studies

Regular Expressions

Why create a separate class for it?

```
class RegEx {  
    // ...  
public:  
    static bool isValid(const char *regEx);  
    RegEx(); // Empty language: Accepts nothing.  
    RegEx(const char *regEx);  
    RegEx(const RegEx& other);  
    ~RegEx();  
    RegEx& operator=(const RegEx& rhs);  
    void setValue(const char *regEx);  
    int setValueIfValid(const char *regEx);  
    bool isMember(const char *token) const;  
};
```



Creators

3. Two Important, Instructional Case Studies

Regular Expressions

Why create a separate class for it?

```
class RegEx {  
    // ...  
public:  
    static bool isValid(const char *regEx);  
    RegEx(); // Empty language: Accepts nothing.  
    RegEx(const char *regEx);  
    RegEx(const RegEx& other);  
    ~RegEx();  
    RegEx& operator=(const RegEx& rhs);  
    void setValue(const char *regEx);  
    int setValueIfValid(const char *regEx);  
    bool isMember(const char *token) const;  
};
```



Creators

3. Two Important, Instructional Case Studies

Regular Expressions

Why create a separate class for it?

```
class RegEx {  
    // ...  
public:  
    static bool isValid(const char *regEx);  
    RegEx(); // Empty language: Accepts nothing.  
    RegEx(const char *regEx);  
    RegEx(const RegEx& other);  
    ~RegEx();  
    RegEx& operator=(const RegEx& rhs);  
    void setValue(const char *regEx);  
    int setValueIfValid(const char *regEx);  
    bool isMember(const char *token) const;  
};
```



Creators

3. Two Important, Instructional Case Studies

Regular Expressions

Why create a separate class for it?

```
class RegEx {  
    // ...  
public:  
    static bool isValid(const char *regEx);  
    RegEx(); // Empty language: Accepts nothing.  
    RegEx(const char *regEx);  
    RegEx(const RegEx& other);  
    ~RegEx();  
    RegEx& operator=(const RegEx& rhs);  
    void setValue(const char *regEx);  
    int setValueIfValid(const char *regEx);  
    bool isMember(const char *token) const;  
};
```

Manipulators

Whatever the value is.

3. Two Important, Instructional Case Studies

Regular Expressions

Why create a separate class for it?

```
class RegEx {  
    // ...  
public:  
    static bool isValid(const char *regEx);  
    RegEx(); // Empty language: Accepts nothing.  
    RegEx(const char *regEx);  
    RegEx(const RegEx& other);  
    ~RegEx();  
    RegEx& operator=(const RegEx& rhs);  
    void setValue(const char *regEx);  
    int setValueIfValid(const char *regEx);  
    bool isMember(const char *token) const;  
};
```

Manipulators

What is the value?

3. Two Important, Instructional Case Studies

Regular Expressions

Why create a separate class for it?

```
class RegEx {  
    // ...  
public:  
    static bool isValid(const char *regEx);  
    RegEx(); // Empty language: Accepts nothing.  
    RegEx(const char *regEx);  
    RegEx(const RegEx& other);  
    ~RegEx();  
    RegEx& operator=(const RegEx& rhs);  
    void setValue(const char *regEx);  
    int setValueIfValid(const char *regEx);  
    bool isMember(const char *token) const;  
};
```

Manipulators

Why both?

3. Two Important, Instructional Case Studies


Regular Expressions

Why create a separate class for it?

```
class RegEx {  
    // ...  
public:  
    static bool isValid(const char *regEx);  
    RegEx(); // Empty language: Accepts nothing.  
    RegEx(const char *regEx);  
    RegEx(const RegEx& other);  
    ~RegEx();  
    RegEx& operator=(const RegEx& rhs);  
    void setValue(const char *regEx);  
    int setValueIfValid(const char *regEx);  
    bool isMember(const char *token) const;  
};
```



Accessors



a.k.a.
"accept"
or
"matching"

3. Two Important, Instructional Case Studies

Regular Expressions

Why create a separate class for it?

```
class RegEx {
```

```
    // ...
```

```
public:
```

Which Operations Are Salient?

```
    static bool isValid(const char *regEx);
```

```
    RegEx();    // Empty language; accepts nothing.
```

```
    RegEx(const char *regEx);
```

```
    RegEx(const RegEx& other);
```

```
    ~RegEx();
```

```
    RegEx& operator=(const RegEx& rhs);
```

```
    void setValue(const char *regEx);
```

```
    int setValueIfValid(const char *regEx);
```

```
    bool isMember(const char *token) const;
```

```
};
```

3. Two Important, Instructional Case Studies

Regular Expressions

Why create a separate class for it?

```
class RegEx {
```

```
    // ...
```

```
public:
```

Which Operations Are Salient?

```
    static bool isValid(const char *regEx);
```

```
    RegEx();    // Empty language; accepts nothing.
```

```
    RegEx(const char *regEx);
```

```
    RegEx(const RegEx& other);
```

```
    ~RegEx();
```

```
    RegEx& operator=(const RegEx& rhs);
```

```
    void setValue(const char *regEx);
```

```
    int setValueIfValid(const char *regEx);
```

```
    bool isMember(const char *token) const;
```

```
};
```

Just one!

3. Two Important, Instructional Case Studies

Regular Expressions

Why create a separate class for it?

```
class RegEx {
```

```
    // ...
```

```
public:
```

Which Operations Are Salient?

```
    static bool isValid(const char *regEx);
```

```
    RegEx();    // Empty language; accepts nothing.
```

```
    RegEx(const char *regEx);
```

```
    RegEx(const RegEx& other);
```

```
    ~RegEx();
```

```
    RegEx& operator=(const RegEx& rhs);
```

```
    void setValue(const char *regEx);
```

```
    int setValueIfValid(const char *regEx);
```

```
    bool isMember(const char *token) const;
```

```
};
```

Just one!

3. Two Important, Instructional Case Studies

Regular Expressions

Why create a separate class for it?

```
class RegEx {
```

```
    // ...
```

```
public:
```

Which Operations Are Salient?

```
    static bool isValid(const char *regEx);
```

```
    RegEx();    // Empty language; accepts nothing.
```

```
    RegEx(const char *regEx);
```

```
    RegEx(const RegEx& other);
```

```
    ~RegEx();
```

```
    RegEx& operator=(const RegEx& rhs);
```

```
    void setValue(const char *regEx);
```

```
    int setValueIfValid(const char *regEx);
```

```
    bool isMember(const char *token) const;
```

```
};
```

Let's think
about this!

3. Two Important, Instructional Case Studies

Regular Expressions

Important Design Questions:

- What is a *Regular Expression*?
- Why create a separate class for it?
- **Does/should it represent a value?**
- How should its value be defined?
- Should such a class be *regular*?

3. Two Important, Instructional Case Studies

Regular Expressions

Does/should it represent a value?

3. Two Important, Instructional Case Studies

Regular Expressions

Does/should it represent a value?

Is a `Regex` class a *value type*, or a *mechanism*?

3. Two Important, Instructional Case Studies

Regular Expressions

Does/should it represent a value?

Is a `Regex` class a *value type*, or a *mechanism*?

I.e., is there an obvious notion of what it means for two `Regex` objects to have the same value?

3. Two Important, Instructional Case Studies

Regular Expressions

Does/should it represent a value?

I claim, “yes!”

I.e., is there an obvious notion of what it means for two `Regex` objects to have the same value?

3. Two Important, Instructional Case Studies

Regular Expressions

Important Design Questions:

- What is a *Regular Expression*?
- Why create a separate class for it?
- Does/should it represent a value?
- **How should its value be defined?**
- Should such a class be *regular*?

3. Two Important, Instructional Case Studies

Regular Expressions

How should its value be defined?

1. The string used to create it.

3. Two Important, Instructional Case Studies

Regular Expressions

How should its value be defined?

1. The string used to create it.
- 2. The language it accepts.**

3. Two Important, Instructional Case Studies

Regular Expressions

How should its value be defined?

1. The string used to create it.
2. The language it accepts.

Note that there is no accessor to get the string used to initialize the value.

3. Two Important, Instructional Case Studies

Regular Expressions

How should its value be defined?

1. The string used to create it.
- 2. The language it accepts.**

IMO, the correct answer is 2. Why?

Note that there is no accessor to get the string used to initialize the value.

3. Two Important, Instructional Case Studies

Regular Expressions

How should its value be defined?

**Actually, there is no
such accessor, precisely
because we defined
value the way we did!**

3. Two Important, Instructional Case Studies

Regular Expressions

How should its value be defined?

1. The value of a RegEx object is defined by the value of the `value` property.
2. What makes a RegEx value special – i.e., distinct from that of the `(const char *)` used to create it – is the language value a RegEx object represents.

3. Two Important, Instructional Case Studies

Regular Expressions

How should its value be defined?

1. Had we provided
2. such an accessor,
it would not be
3. considered *salient*.

3. Two Important, Instructional Case Studies

Regular Expressions

Just like *capacity* for

`std::vector`

How

ed?

1.

2.

Th

Be

th

**Had we provided
such an accessor,
it would not be
considered *salient*.**

et

e.

3. Two Important, Instructional Case Studies

Regular Expressions

Or *iteration order* for

`std::unordered_map`

1.

2.

TH

Be

th

PERHAPS
“FINITE AUTOMATA”
WOULD HAVE BEEN
A BETTER NAME?

3. Two Important, Instructional Case Studies

Regular Expressions

Or *iteration order* for

`std::unordered_map`

1.

2.

TH

Be

tr

PERHAPS

“FINITE AUTOMATA”

“Language”??

3. Two Important, Instructional Case Studies

Regular Expressions

Important Design Questions:

- What is a *Regular Expression*?
- Why create a separate class for it?
- Does/should it represent a value?
- How should its value be defined?
- **Should such a class be *regular*?**

3. Two Important, Instructional Case Studies

Regular Expressions

Should such a class be regular?

I.e., Should our `RegEx` class support all of the value-semantic syntax of a *regular* class?

3. Two Important, Instructional Case Studies

Regular Expressions

Should such a class be regular?

I.e., Should our `RegEx` class support all of the value-semantic syntax of a *regular* class?

Question: How *expensive* would `operator==` be to implement?

3. Two Important, Instructional Case Studies

Regular Expressions

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

3. Two Important, Instructional Case Studies

Regular Expressions

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

In honor of this
very important question
would everyone
PLEASE STAND UP NOW!

3. Two Important, Instructional Case Studies

Regular Expressions

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

3. Two Important, Instructional Case Studies

Regular Expressions

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

- $O[1]$?

3. Two Important, Instructional Case Studies

Regular Expressions

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

- $O[1]$?

PLEASE SIT DOWN
as soon as I
have gone TOO FAR!

3. Two Important, Instructional Case Studies

Regular Expressions

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

- $O[\log N]$

3. Two Important, Instructional Case Studies

Regular Expressions

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

- $O[\log N]$

I.e., Please sit down
NOW if you can write
`operator==` for
`class RegEx` in $O[1]$!

3. Two Important, Instructional Case Studies

Regular Expressions

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

- $O[\log N]$

3. Two Important, Instructional Case Studies

Regular Expressions

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

- $O[\log N]$
- $O[\sqrt{N}]$

3. Two Important, Instructional Case Studies

Regular Expressions

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

- $O[\log N]$
- $O[\sqrt{N}]$
- $O[N]$

3. Two Important, Instructional Case Studies

Regular Expressions

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

- $O[\log N]$
- $O[\sqrt{N}]$
- $O[N]$
- $O[N * \log N]$

3. Two Important, Instructional Case Studies

Regular Expressions

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

- $O[\log N]$

-
-
-

Please sit down
NOW if you can write
`operator==` for
`class RegEx` in $O[N]!$

3. Two Important, Instructional Case Studies

Regular Expressions

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

- $O[\log N]$
- $O[\sqrt{N}]$
- $O[N]$
- $O[N * \log N]$

3. Two Important, Instructional Case Studies

Regular Expressions

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

- $O[\log N]$
- $O[\sqrt{N}]$
- $O[N]$
- $O[N * \log N]$
- $O[N * \sqrt{N}]$

3. Two Important, Instructional Case Studies

Regular Expressions

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

- $O[\log N]$
- $O[\sqrt{N}]$
- $O[N]$
- $O[N * \log N]$
- $O[N * \sqrt{N}]$
- $O[N^2]$

3. Two Important, Instructional Case Studies

Regular Expressions

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

- $O[\log N]$
- $O[\sqrt{N}]$
- $O[N]$
- $O[N * \log N]$
- $O[N * \sqrt{N}]$
- $O[N^2]$
- $O[N^2 * \log N]$

3. Two Important, Instructional Case Studies

Regular Expressions

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

- $O[\log N]$
- $O[\sqrt{N}]$
- $O[N]$
- $O[N * \log N]$
- $O[N * \sqrt{N}]$
- $O[N^2]$
- $O[N^2 * \log N]$
- Polynomial

3. Two Important, Instructional Case Studies

Regular Expressions

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

- $O[\log N]$
- $O[\sqrt{N}]$
- $O[N]$
- $O[N * \log N]$
- $O[N * \sqrt{N}]$
- $O[N^2]$
- $O[N^2 * \log N]$
- Polynomial
- NP

3. Two Important, Instructional Case Studies

Regular Expressions

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

- $O[\log N]$
- $O[\sqrt{N}]$
- $O[N]$
- $O[N * \log N]$
- $O[N * \sqrt{N}]$
- $O[N^2]$
- $O[N^2 * \log N]$
- Polynomial
- NP
- NP complete

3. Two Important, Instructional Case Studies

Regular Expressions

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

- $O[\log N]$
- $O[\sqrt{N}]$
- $O[N]$
- $O[N * \log N]$
- $O[N * \sqrt{N}]$
- $O[N^2]$
- $O[N^2 * \log N]$
- Polynomial
- NP
- NP Complete
- P-SPACE

3. Two Important, Instructional Case Studies

Regular Expressions

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

- $O[\log N]$
- $O[\sqrt{N}]$
- $O[N]$
- $O[N * \log N]$
- $O[N * \sqrt{N}]$
- $O[N^2]$
- $O[N^2 * \log N]$
- Polynomial
- NP
- NP Complete
- P-SPACE
- P-SPACE Complete

3. Two Important, Instructional Case Studies

Regular Expressions

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

- $O[\log N]$
- $O[\sqrt{N}]$
- $O[N]$
- $O[N * \log N]$
- $O[N * \sqrt{N}]$
- $O[N^2]$
- $O[N^2 * \log N]$
- Polynomial
- NP
- NP Complete
- P-SPACE
- P-SPACE Complete
- Undecidable

3. Two Important, Instructional Case Studies

Regular Expressions

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

- $O[\log N]$
- $O[\sqrt{N}]$
- $O[N]$
- $O[N * \log N]$
- $O[N * \sqrt{N}]$
- $O[N^2]$
- $O[N^2 * \log N]$
- Polynomial
- NP
- NP Complete
- P-SPACE
- **P-SPACE Complete**
- Undecidable

If you just
sat down
you were right!

3. Two Important, Instructional Case Studies

Regular Expressions

P-Space Complete

Over an alphabet Σ , given one DFA having states $S=\{si\}$ (of which $A\subseteq S$ are accepting) and transition function $\delta:S\times\Sigma\rightarrow S$, and another DFA having states $T=\{tj\}$ (of which $B\subseteq T$ are accepting) and transition function $\zeta:T\times\Sigma\rightarrow T$, one can "easily" construct a DFA with states $U=S\times T$ (Cartesian product) and transition function $\eta((si, tj), \sigma) = (\delta(si, \sigma), \zeta(tj, \sigma))$, where $\sigma \in \Sigma$. Then the two original DFAs are equivalent iff the only states reachable in this Cartesian-product DFA are a subset of $(A\times B)\cup((S\setminus A)\times(T\setminus B))$ — i.e., it's impossible to reach a state that is accepting in one of the original DFAs, but not in the other. Once one has translated the regular expressions to DFAs, the naive **time complexity is $O(|\Sigma|^{|S| \cdot |T|})$** , and the **space complexity is $O(|S| \cdot |T| \cdot |\Sigma|)$** .

3. Two Important, Instructional Case Studies

Regular Expressions

Should such a

Question: How *expensive* would it be?

Should we avoid value types
where equality comparison
is expensive?

- $O[\log N]$
- $O[\sqrt{N}]$

**Clearly No
Equality-Comparison
Operators!**

- P-SPACE
- **P-SPACE Complete**
- Undecidable

3. Two Important, Instructional Case Studies

Regular Expressions

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

**Copy Construction
and Assignment
Aren't a Problem.**

- P-SPACE
- **P-SPACE Complete**
- Undecidable

3. Two Important, Instructional Case Studies

Regular Expressions

Discussion?

3. Two Important, Instructional Case Studies

Priority Queues

Important Design Questions:

- What is a *Priority Queue*?
- Why create a separate class for it?
- Does/should it represent a value?
- How should its value be defined?
- Should such a class be *regular*?

3. Two Important, Instructional Case Studies

Priority Queues

Important Design Questions:

- **What is a *Priority Queue*?**
- Why create a separate class for it?
- Does/should it represent a value?
- How should its value be defined?
- Should such a class be *regular*?

3. Two Important, Instructional Case Studies

Priority Queues

What is a *Priority Queue*?

3. Two Important, Instructional Case Studies

Priority Queues

What is a *Priority Queue*?

A *priority queue* is a (generic) container that provides constant-time access to its **top** priority element – defined by a user-supplied *priority* function (or *functor*) – as well as supporting logarithmic-time **pushes** and **pops** of queue-element values.

3. Two Important, Instructional Case Studies

Priority Queues

What is a *Priority Queue*?

A *priority queue* (generic) container that
provides access to its **top**
priority element – defined by a user-
supplied *priority* function (or *functor*) – as
well as supporting logarithmic-time **pushes**
and **pops** of queue-element values.

Salient
Operations

3. Two Important, Instructional Case Studies

Priority Queues

What is a *Priority Queue*?

Example Queue Element:

```
class LabeledPoint {
    std::string d_label;
    int         d_x;
    int         d_y;
public:

    // ... (Regular Type)

    const std::string& label() const { return d_label };
    int                x()      const { return d_x; };
    int                y()      const { return d_y; };
};

bool operator==(const LabeledPoint& lhs,
                const LabeledPoint& rhs) {
    return lhs.label() == rhs.label()
        && lhs.x()      == rhs.x()
        && lhs.y()      == rhs.y();
}
```

(Unconstrained Attribute Class)

3. Two Important, Instructional Case Studies

Priority Queues

What is a *Priority Queue*?

Example Queue Element:

```
class LabeledPoint {  
    std::string d_label;  
    int         d_x;  
    int         d_y;  
public:
```

// ... (Regular Type)

```
    const std::string& label() const { return d_label };  
    int               x()      const { return d_x; };  
    int               y()      const { return d_y; };  
};
```

```
bool operator==(const LabeledPoint& lhs,  
                const LabeledPoint& rhs) {  
    return lhs.label() == rhs.label()  
        && lhs.x()      == rhs.x()  
        && lhs.y()      == rhs.y();  
}
```

Example Comparison Function:

```
bool less(const LabeledPoint& a,  
          const LabeledPoint& b) {  
    return abs(a.x()) + abs(a.y())  
           < abs(b.x()) + abs(b.y());  
} (a.k.a. "Manhattan Distance")
```

(Unconstrained Attribute Class)

3. Two Important, Instructional Case Studies

Priority Queues

What is a *Priority Queue*?

Example Queue Element:

```
class LabeledPoint {  
    std::string d_label;  
    int          d_x;  
    int          d_y;  
public:
```

// ... **(Regular Type)**

```
    const std::string& label() const { return d_label };  
    int               x()      const { return d_x;   };  
    int               y()      const { return d_y;   };  
};
```

```
bool operator==(const LabeledPoint& lhs,  
                const LabeledPoint& rhs) {  
    return lhs.label() == rhs.label()  
        && lhs.x()     == rhs.x()  
        && lhs.y()     == rhs.y();  
}
```

Example Comparison Function:

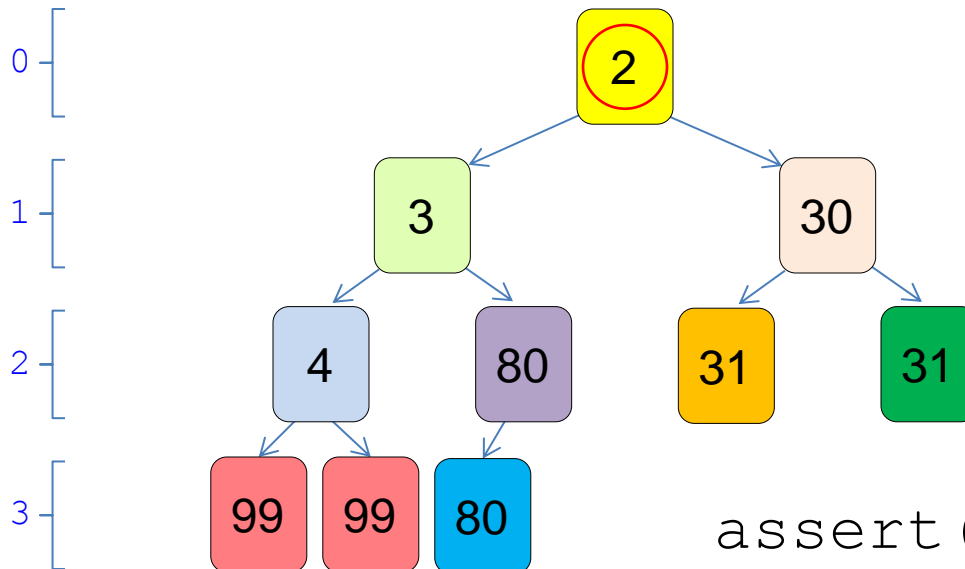
```
bool less(const LabeledPoint& a,  
          const LabeledPoint& b) {  
    return abs(a.x()) + abs(a.y())  
           < abs(b.x()) + abs(b.y());  
} (a.k.a. "Manhattan Distance")
```

(Unconstrained Attribute Class)

3. Two Important, Instructional Case Studies

Priority Queues

What is a *Priority Queue*?

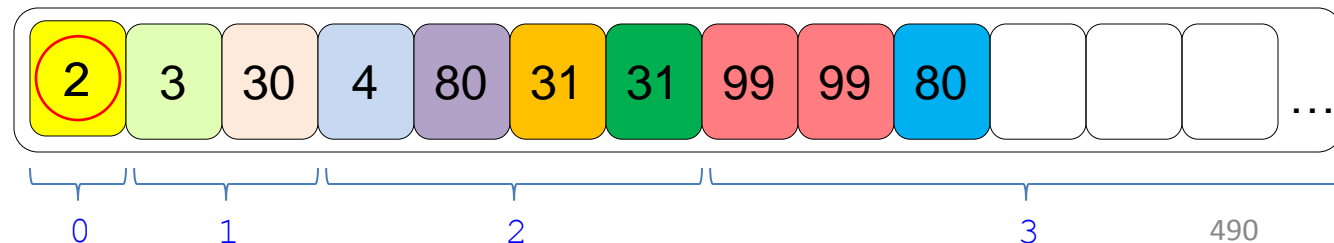


Each element is labeled with its calculated priority.

Each distinct color represents an element having a distinct value.

```
assert (q.top() == 2);
```

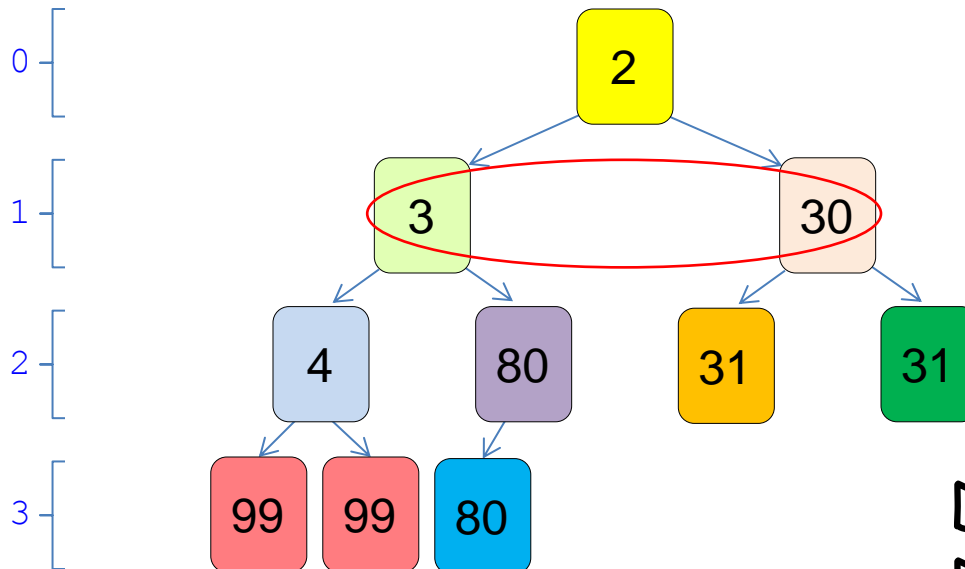
Array-Based Heap:



3. Two Important, Instructional Case Studies

Priority Queues

What is a *Priority Queue*?

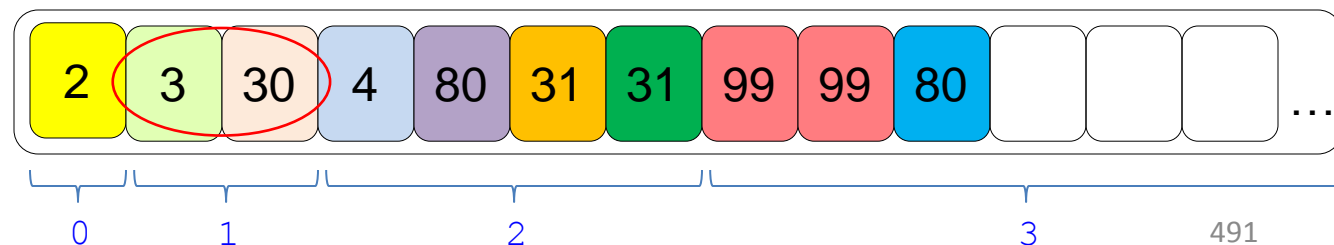


Each element is labeled with its calculated priority.

Each distinct color represents an element having a distinct value.

Different Priorities,
Different Values

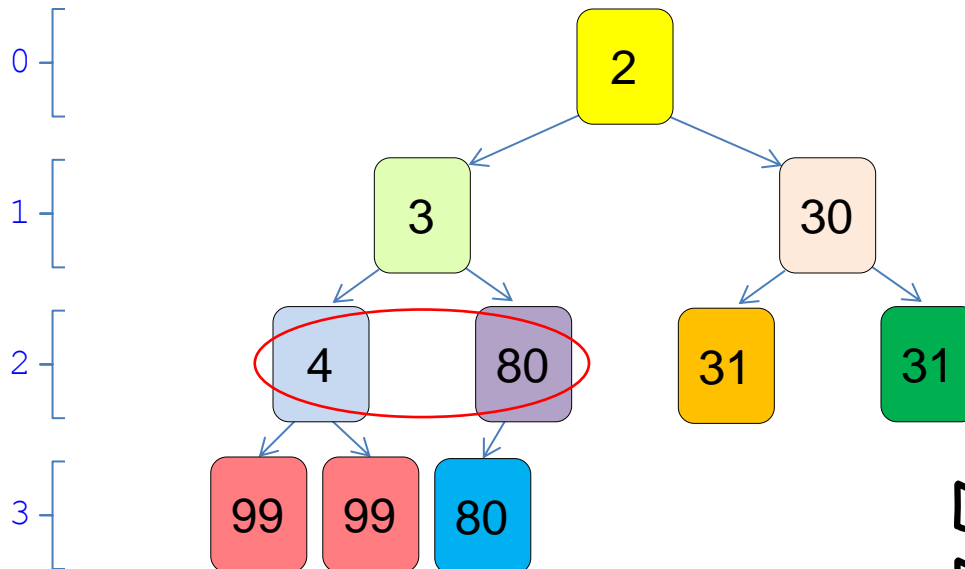
Array-Based Heap:



3. Two Important, Instructional Case Studies

Priority Queues

What is a *Priority Queue*?

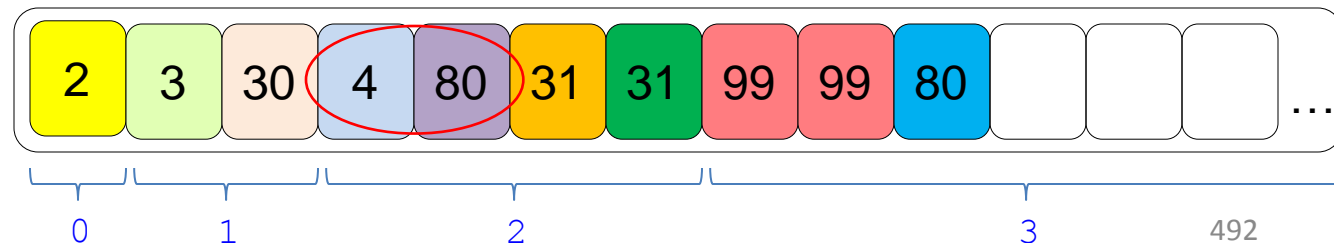


Each element is labeled with its calculated priority.

Each distinct color represents an element having a distinct value.

Different Priorities,
Different Values

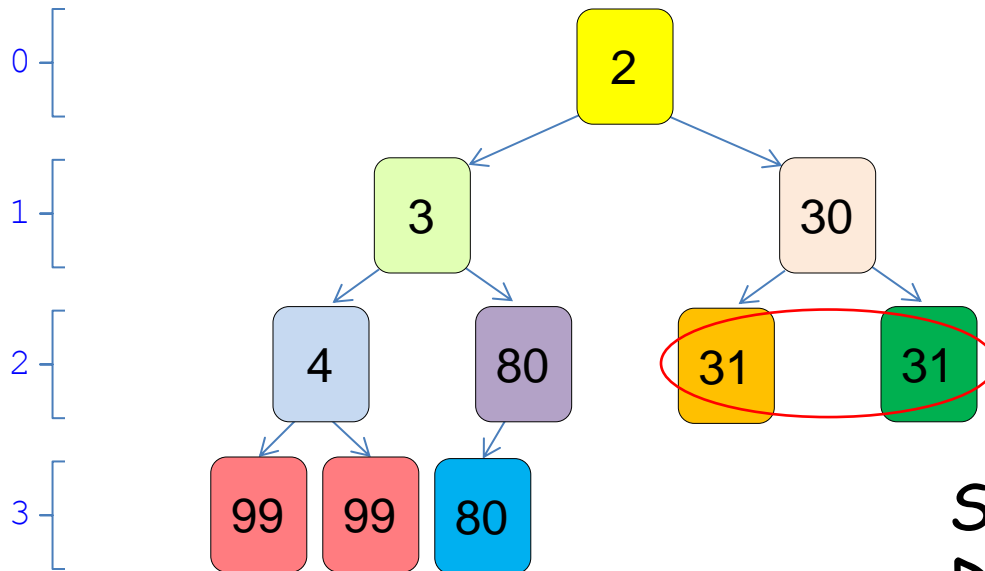
Array-Based Heap:



3. Two Important, Instructional Case Studies

Priority Queues

What is a *Priority Queue*?

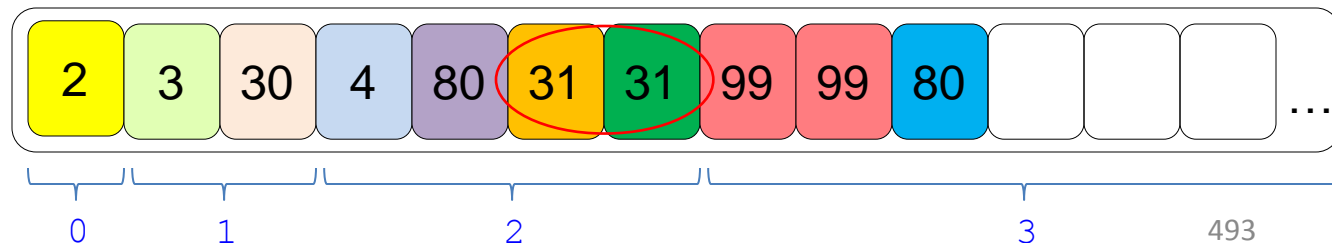


Each element is labeled with its calculated priority.

Each distinct color represents an element having a distinct value.

Same Priority,
Different Values

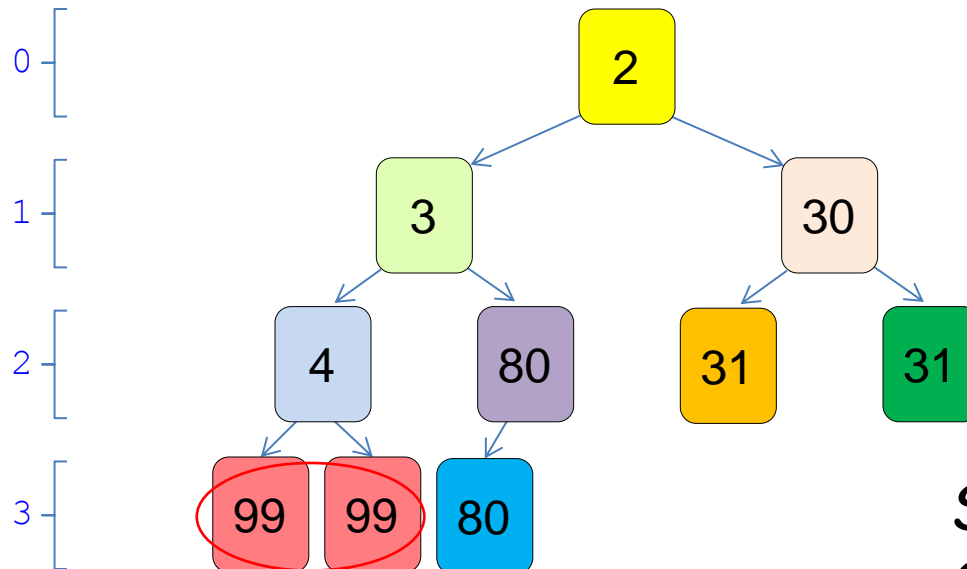
Array-Based Heap:



3. Two Important, Instructional Case Studies

Priority Queues

What is a *Priority Queue*?

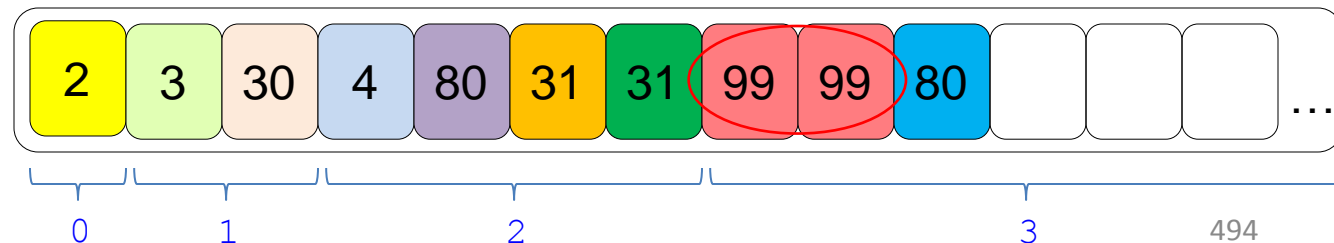


Each element is labeled with its calculated priority.

Each distinct color represents an element having a distinct value.

Same Priority,
Same Value

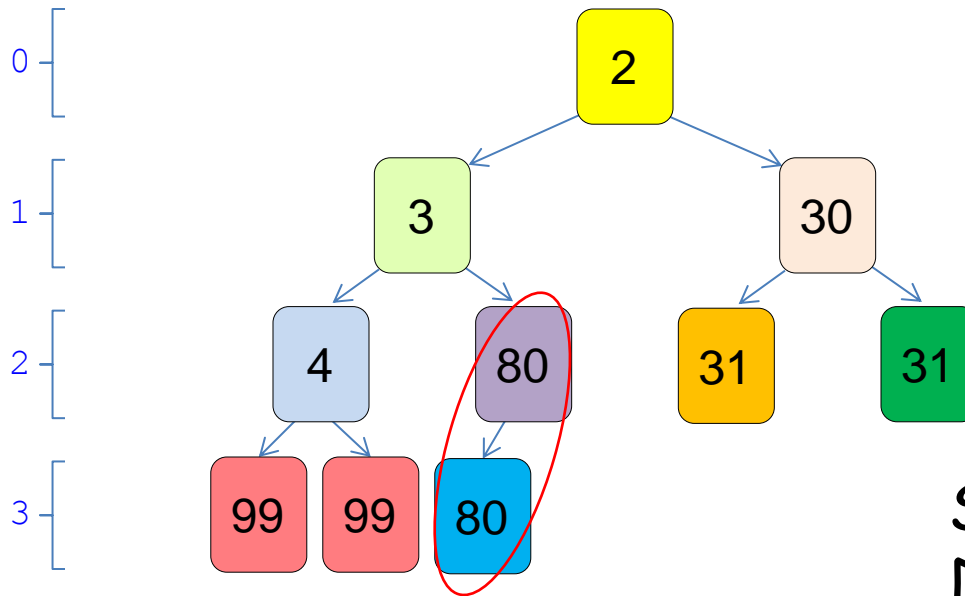
Array-Based Heap:



3. Two Important, Instructional Case Studies

Priority Queues

What is a *Priority Queue*?

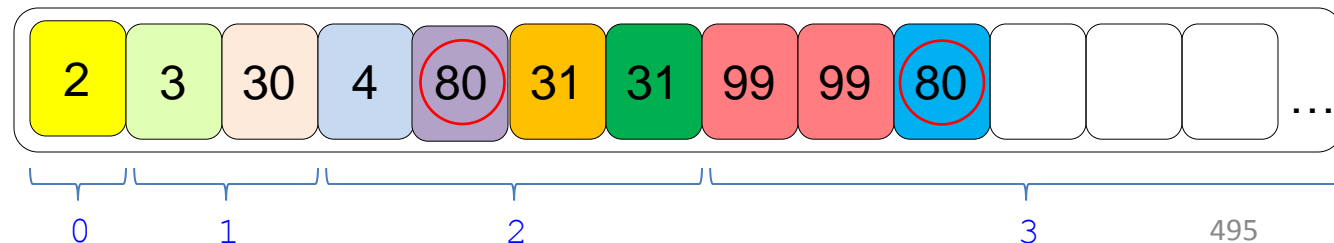


Each element is labeled with its calculated priority.

Each distinct color represents an element having a distinct value.

Same Priority,
Different Values

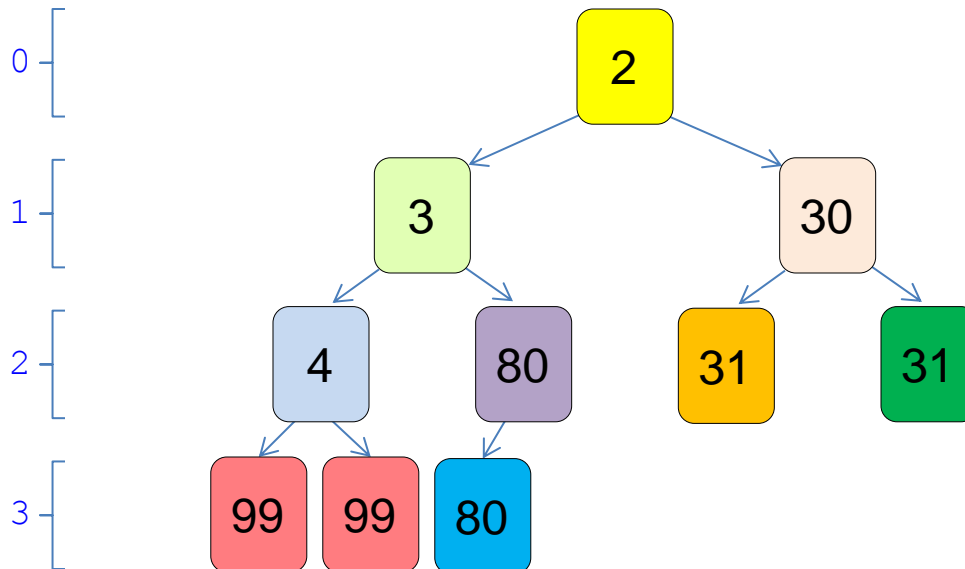
Array-Based Heap:



3. Two Important, Instructional Case Studies

Priority Queues

What is a *Priority Queue*?

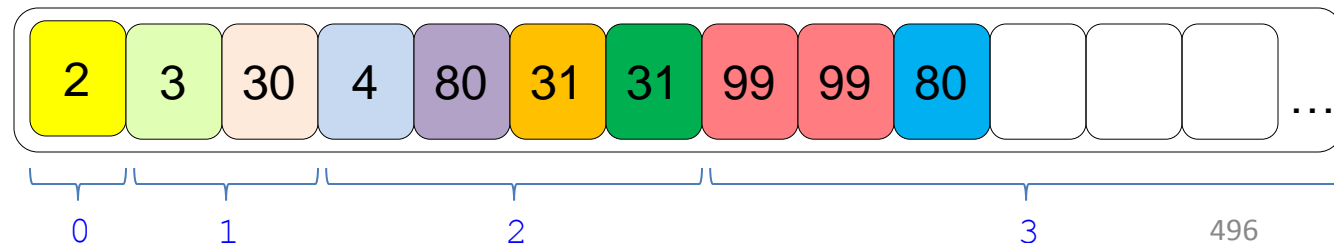


Each element is labeled with its calculated priority.

Each distinct color represents an element having a distinct value.

`q.push (2) ;`

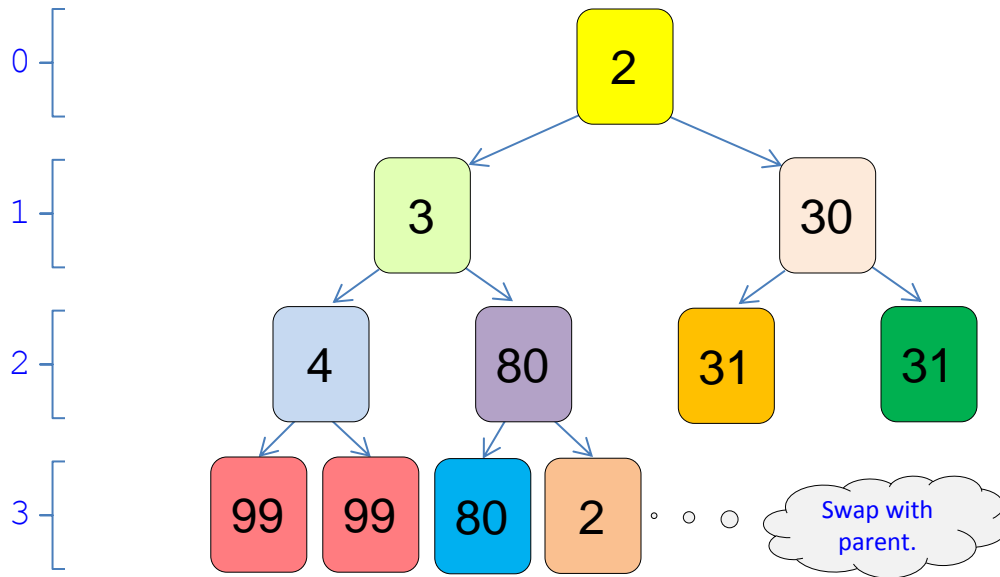
Array-Based Heap:



3. Two Important, Instructional Case Studies

Priority Queues

What is a *Priority Queue*?

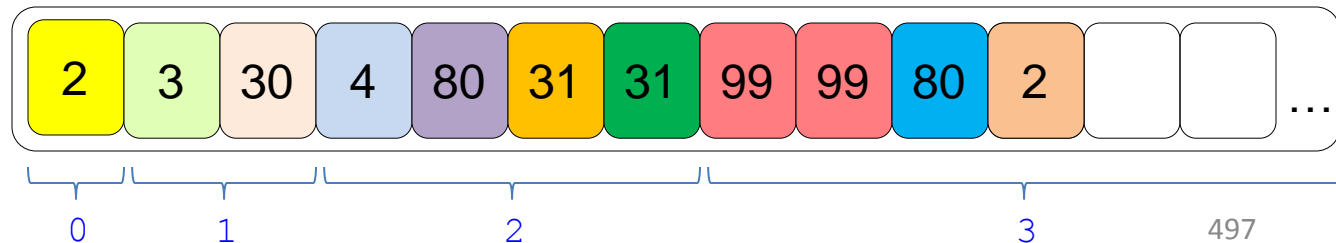


Each element is labeled with its calculated priority.

Each distinct color represents an element having a distinct value.

`q.push (2) ;`

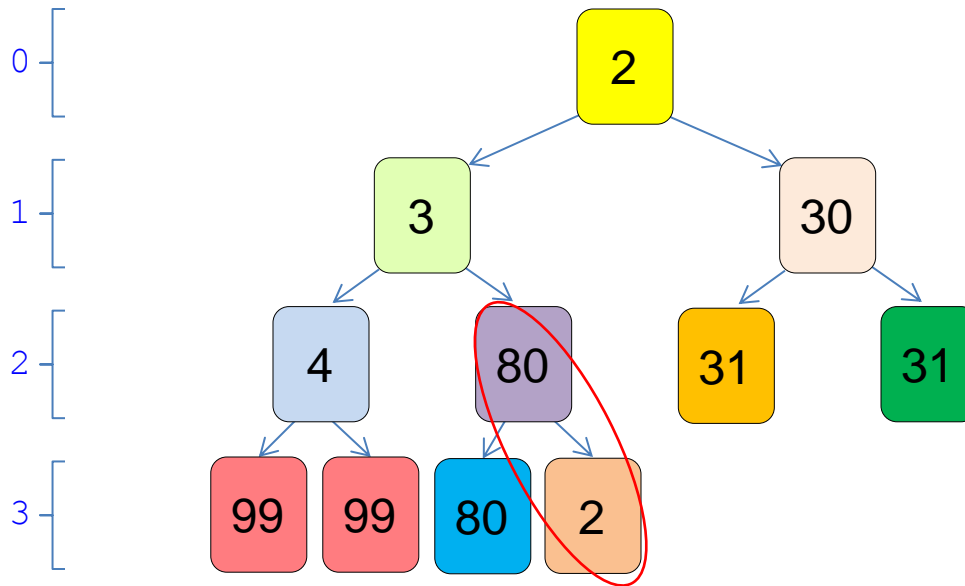
Array-Based Heap:



3. Two Important, Instructional Case Studies

Priority Queues

What is a *Priority Queue*?

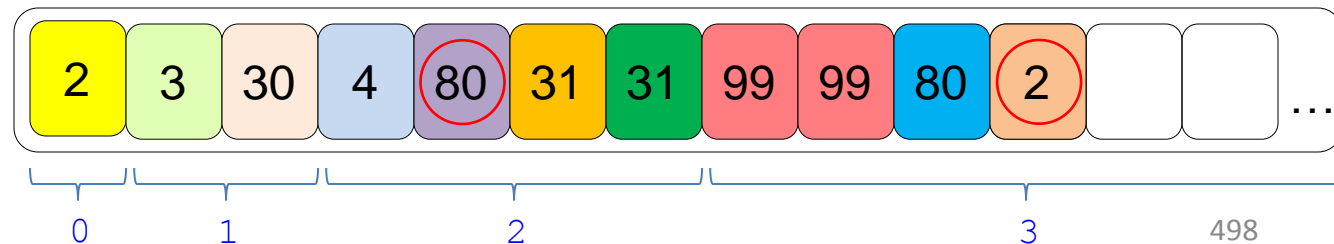


Each element is labeled with its calculated priority.

Each distinct color represents an element having a distinct value.

`q.push (2) ;`

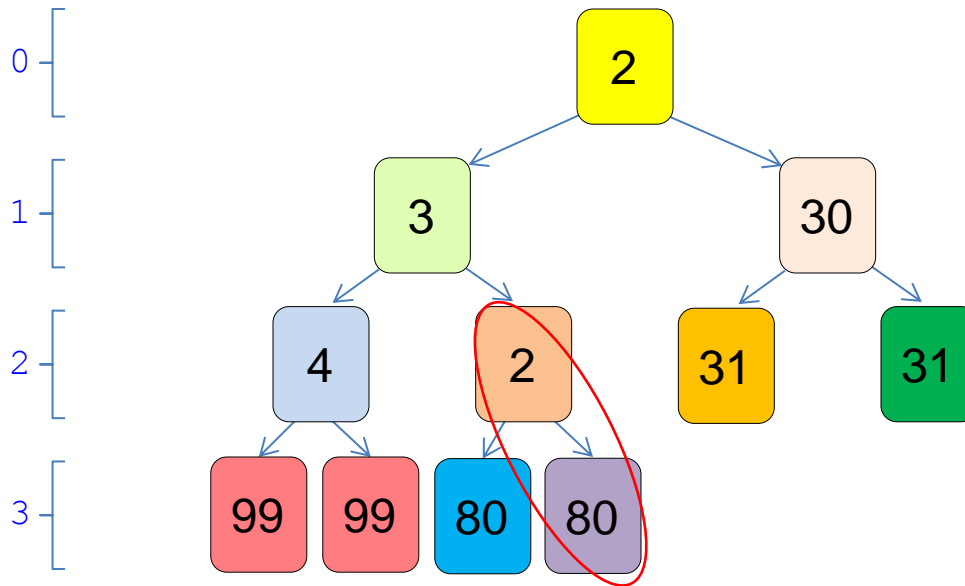
Array-Based Heap:



3. Two Important, Instructional Case Studies

Priority Queues

What is a *Priority Queue*?

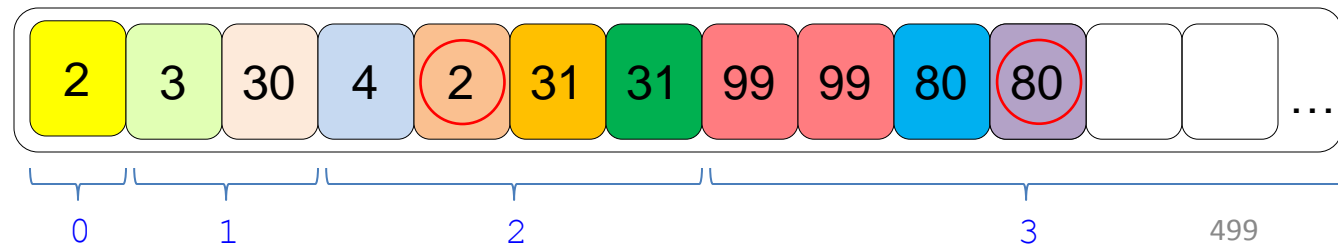


Each element is labeled with its calculated priority.

Each distinct color represents an element having a distinct value.

`q.push (2) ;`

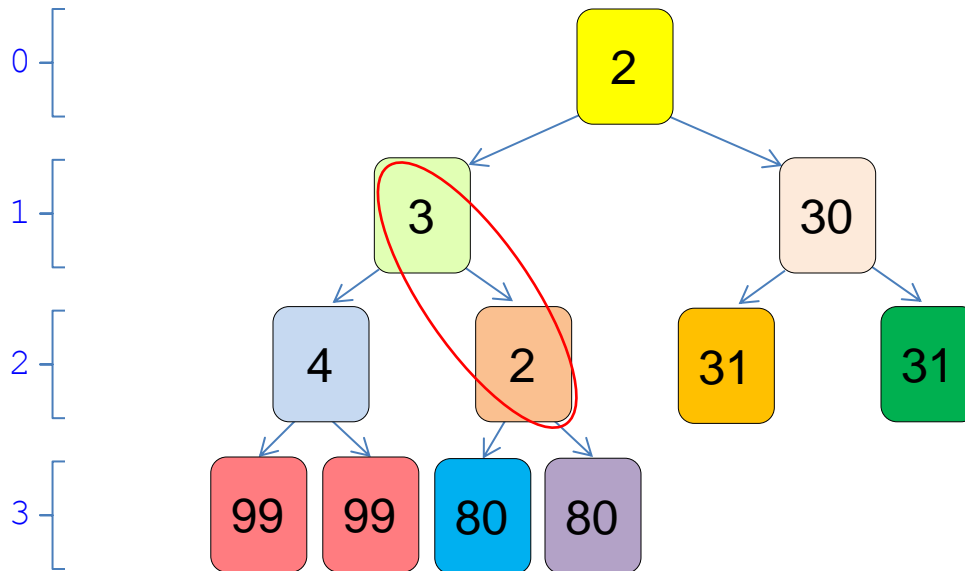
Array-Based Heap:



3. Two Important, Instructional Case Studies

Priority Queues

What is a *Priority Queue*?

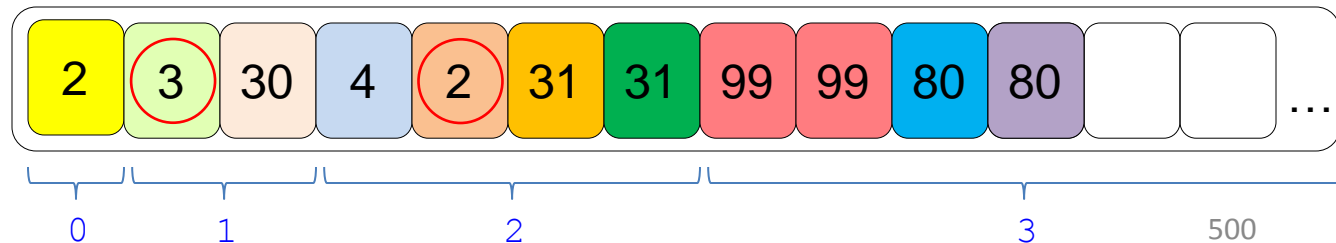


Each element is labeled with its calculated priority.

Each distinct color represents an element having a distinct value.

`q.push (2) ;`

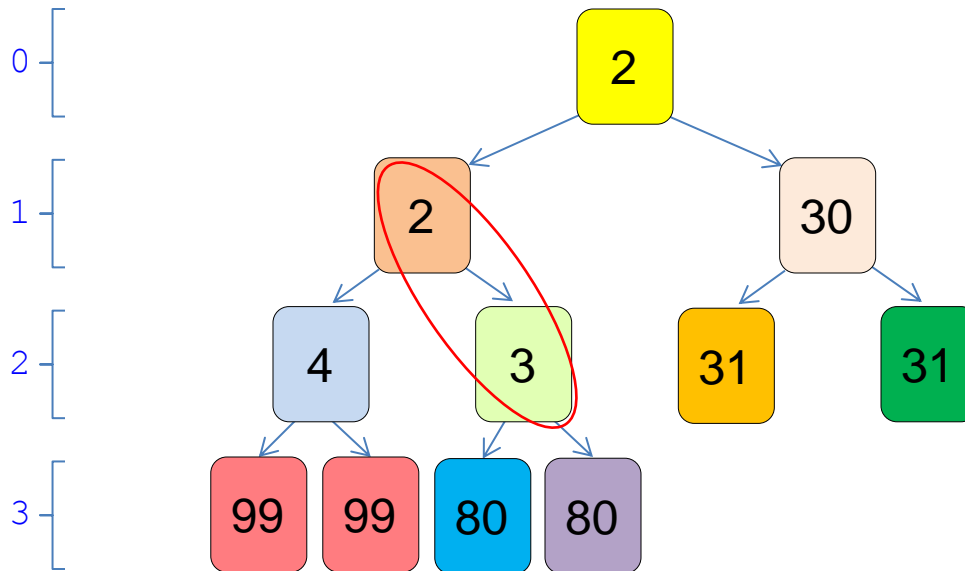
Array-Based Heap:



3. Two Important, Instructional Case Studies

Priority Queues

What is a *Priority Queue*?

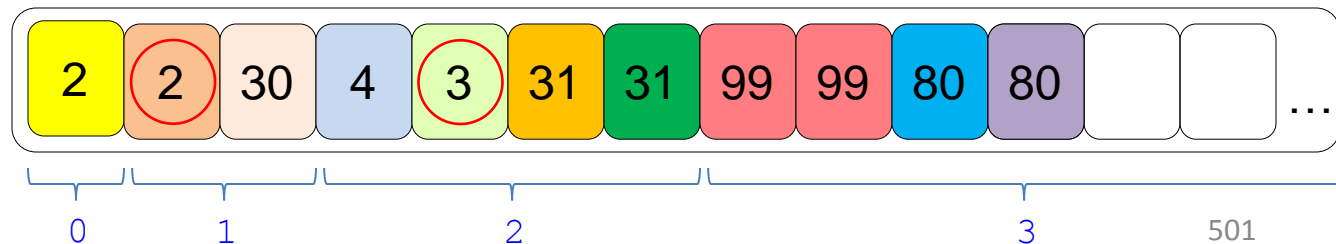


Each element is labeled with its calculated priority.

Each distinct color represents an element having a distinct value.

`q.push (2) ;`

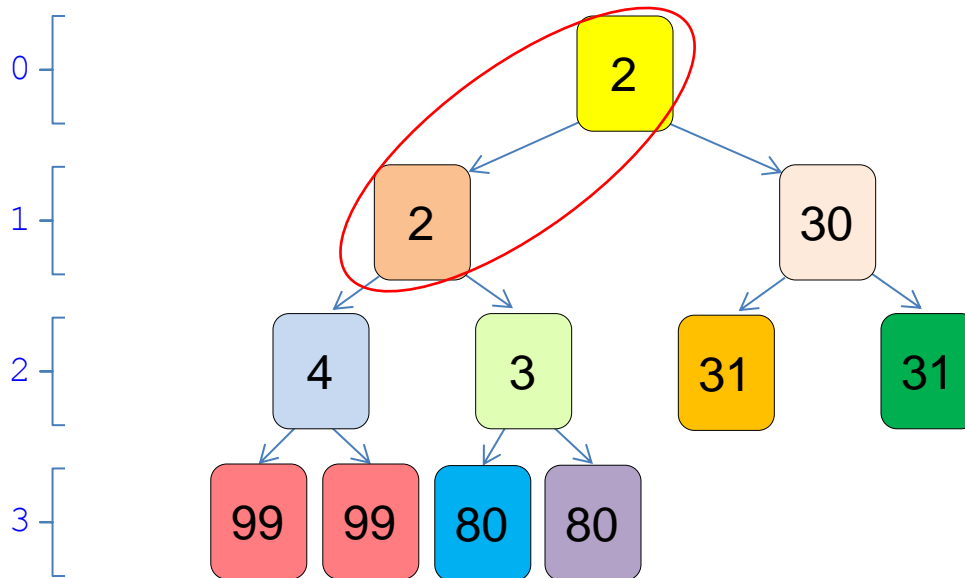
Array-Based Heap:



3. Two Important, Instructional Case Studies

Priority Queues

What is a *Priority Queue*?

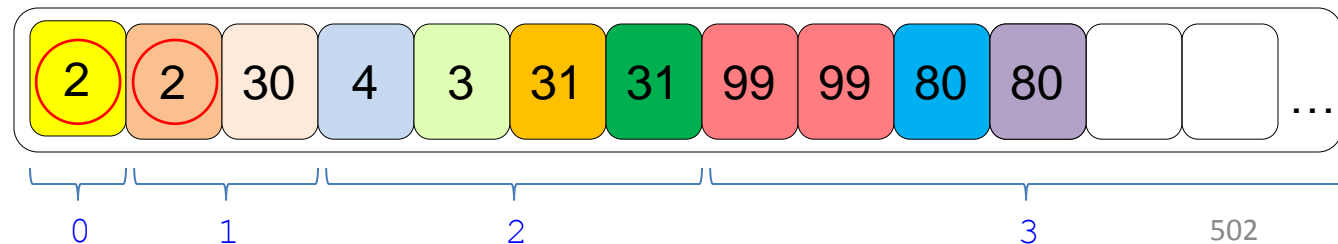


Each element is labeled with its calculated priority.

Each distinct color represents an element having a distinct value.

`q.push (2) ;`

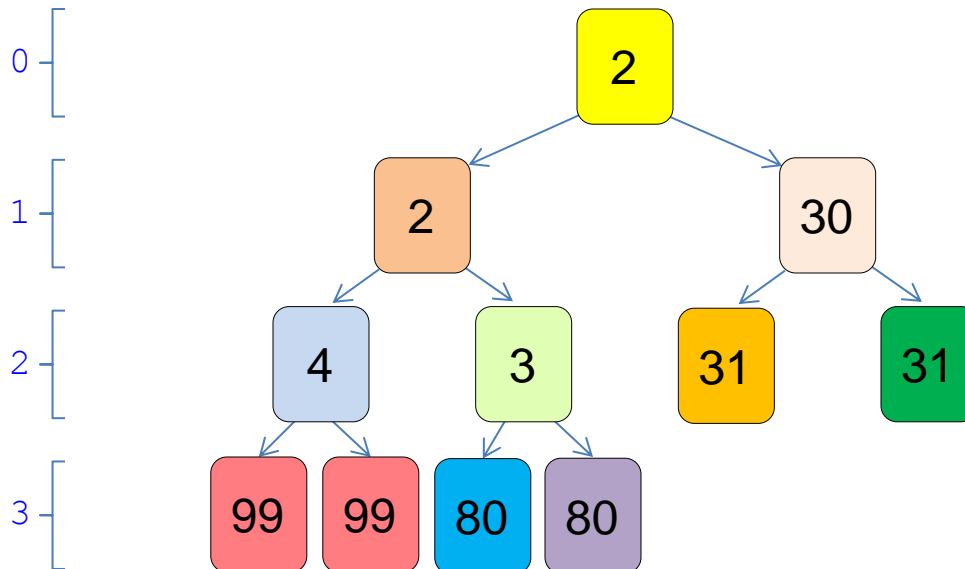
Array-Based Heap:



3. Two Important, Instructional Case Studies

Priority Queues

What is a *Priority Queue*?

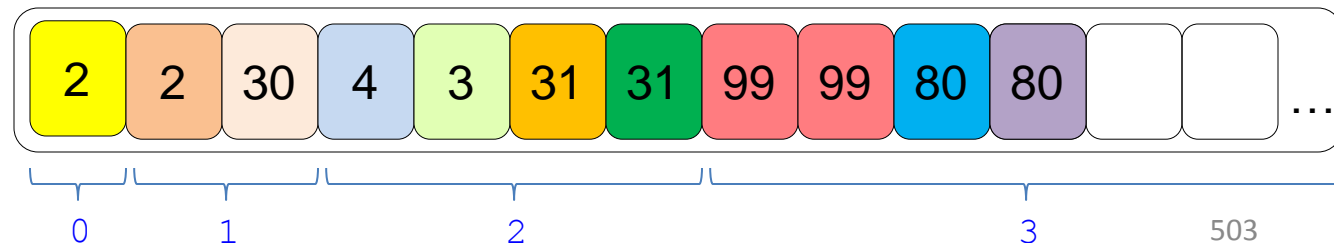


Each element is labeled with its calculated priority.

Each distinct color represents an element having a distinct value.

`q.push (2) ;`

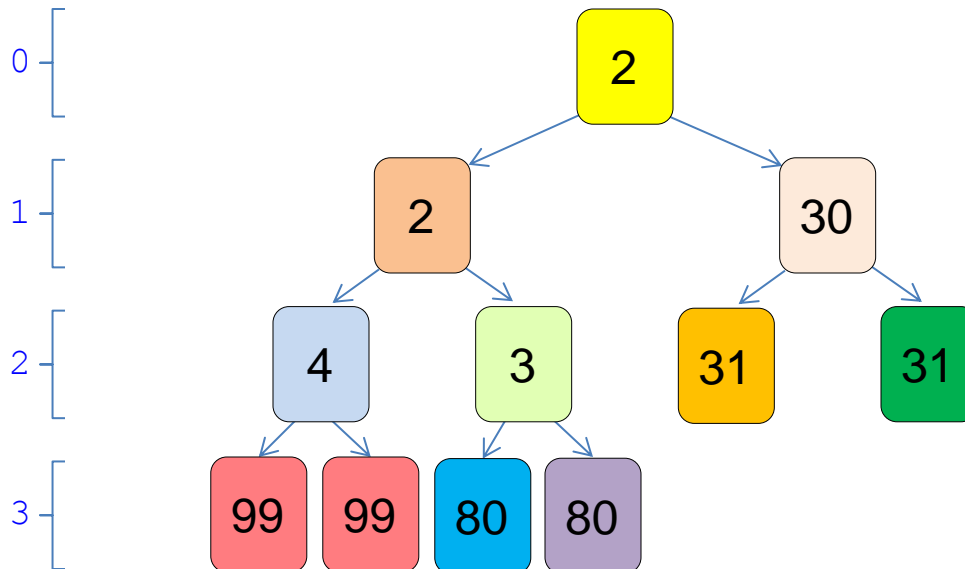
Array-Based Heap:



3. Two Important, Instructional Case Studies

Priority Queues

What is a *Priority Queue*?

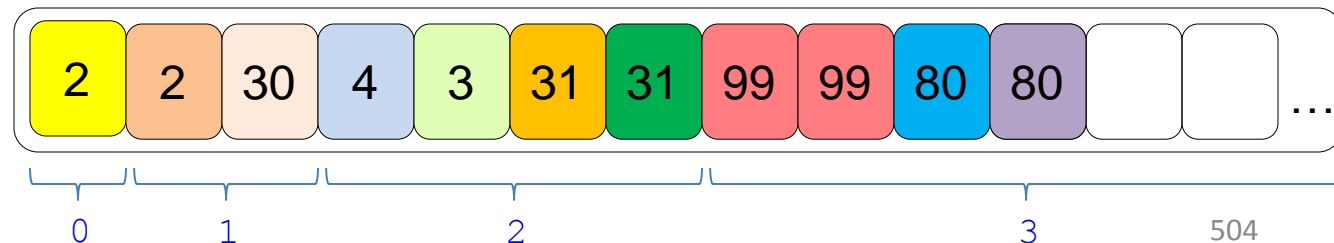


Each element is labeled with its calculated priority.

Each distinct color represents an element having a distinct value.

`q.pop()` ;

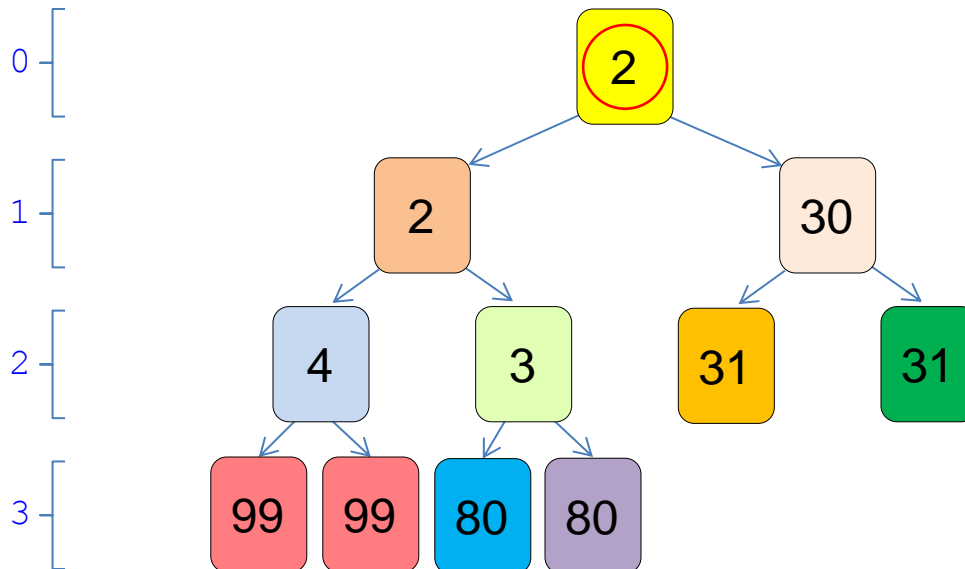
Array-Based Heap:



3. Two Important, Instructional Case Studies

Priority Queues

What is a *Priority Queue*?

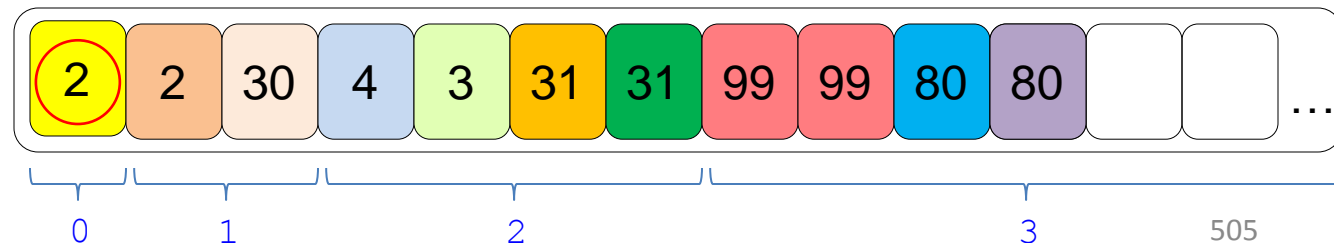


Each element is labeled with its calculated priority.

Each distinct color represents an element having a distinct value.

`q.pop()` ;

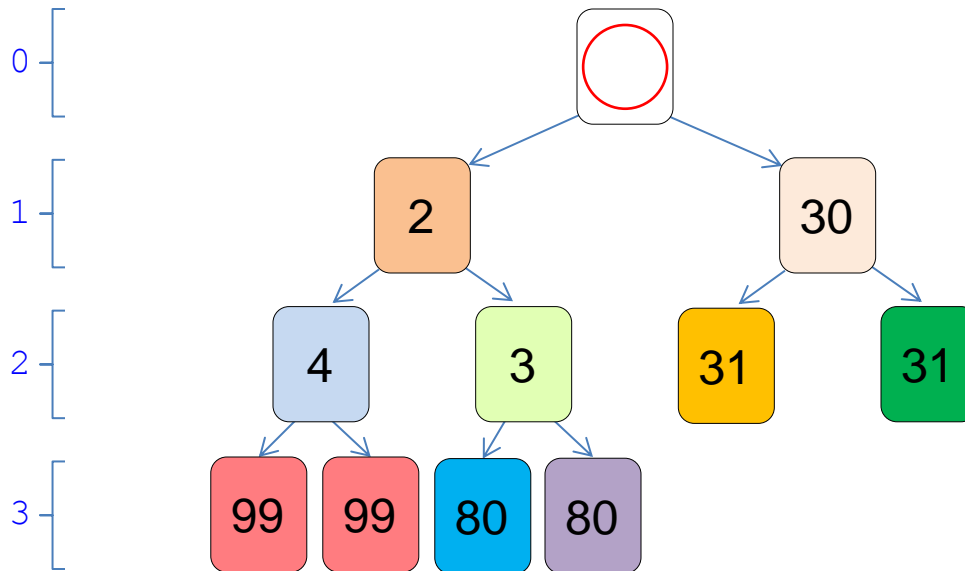
Array-Based Heap:



3. Two Important, Instructional Case Studies

Priority Queues

What is a *Priority Queue*?

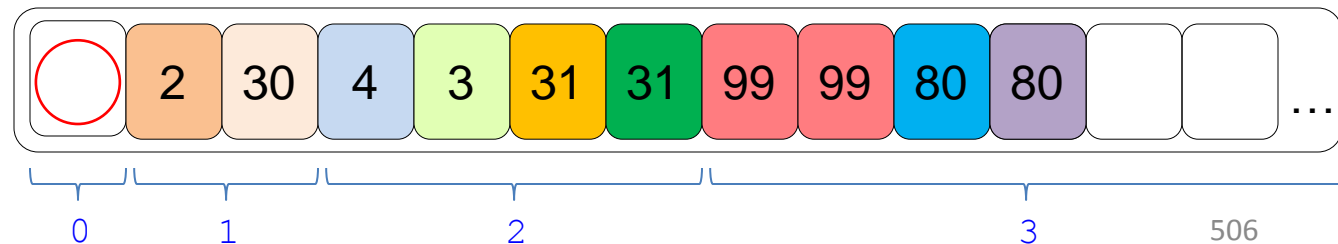


Each element is labeled with its calculated priority.

Each distinct color represents an element having a distinct value.

`q.pop()` ;

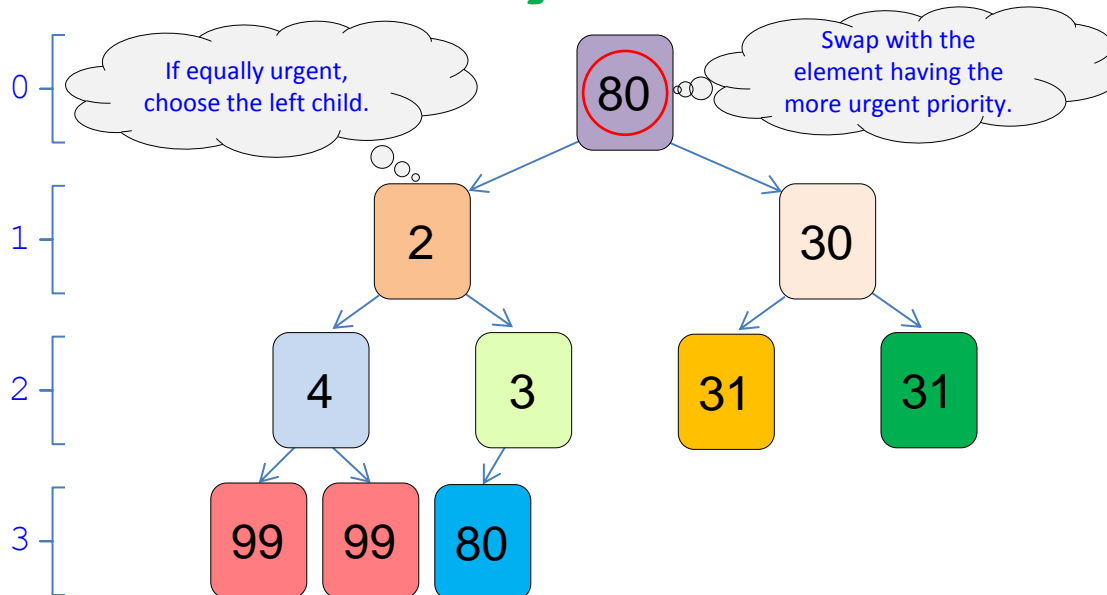
Array-Based Heap:



3. Two Important, Instructional Case Studies

Priority Queues

What is a *Priority Queue*?

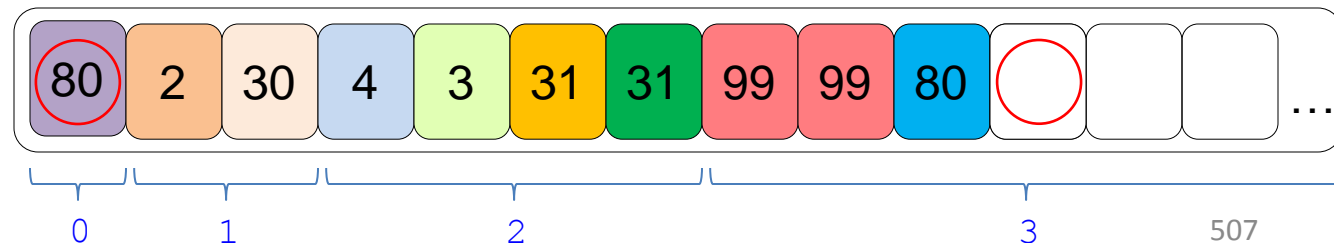


Each element is labeled with its calculated priority.

Each distinct color represents an element having a distinct value.

`q.pop()` ;

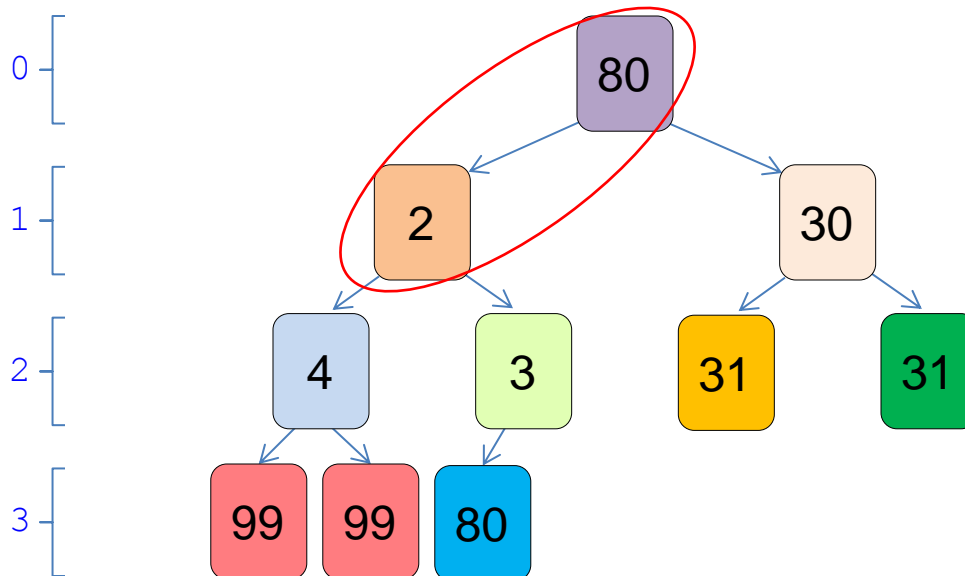
Array-Based Heap:



3. Two Important, Instructional Case Studies

Priority Queues

What is a *Priority Queue*?

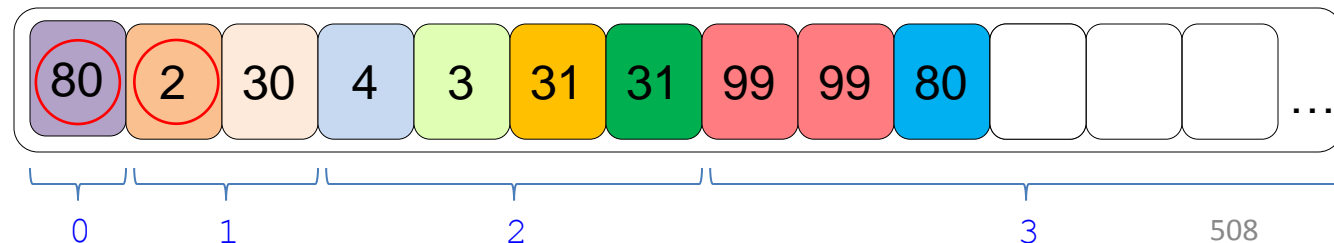


Each element is labeled with its calculated priority.

Each distinct color represents an element having a distinct value.

`q.pop()` ;

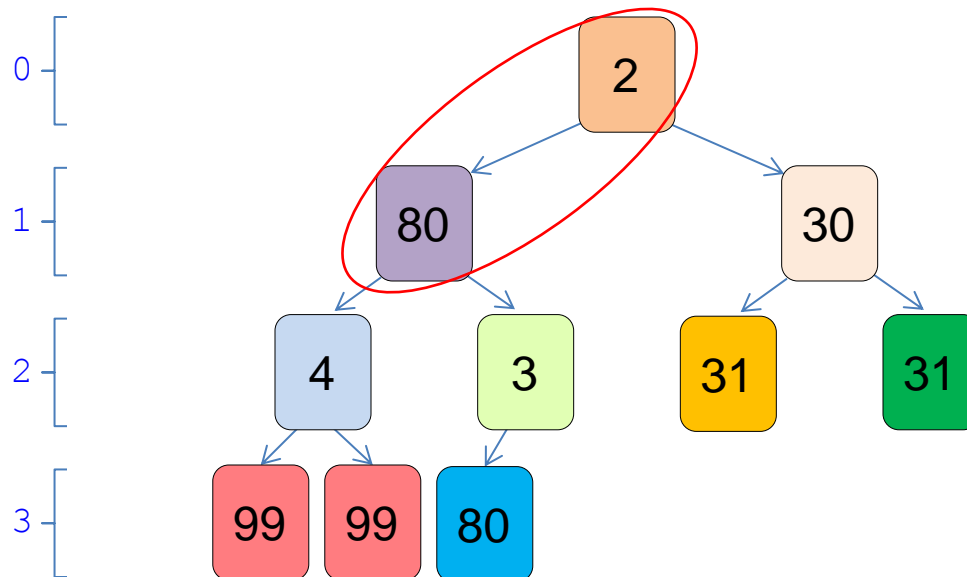
Array-Based Heap:



3. Two Important, Instructional Case Studies

Priority Queues

What is a *Priority Queue*?

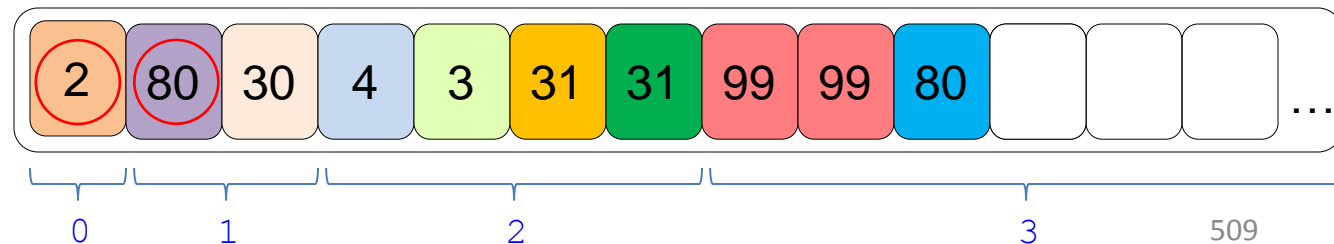


Each element is labeled with its calculated priority.

Each distinct color represents an element having a distinct value.

```
q.pop();
```

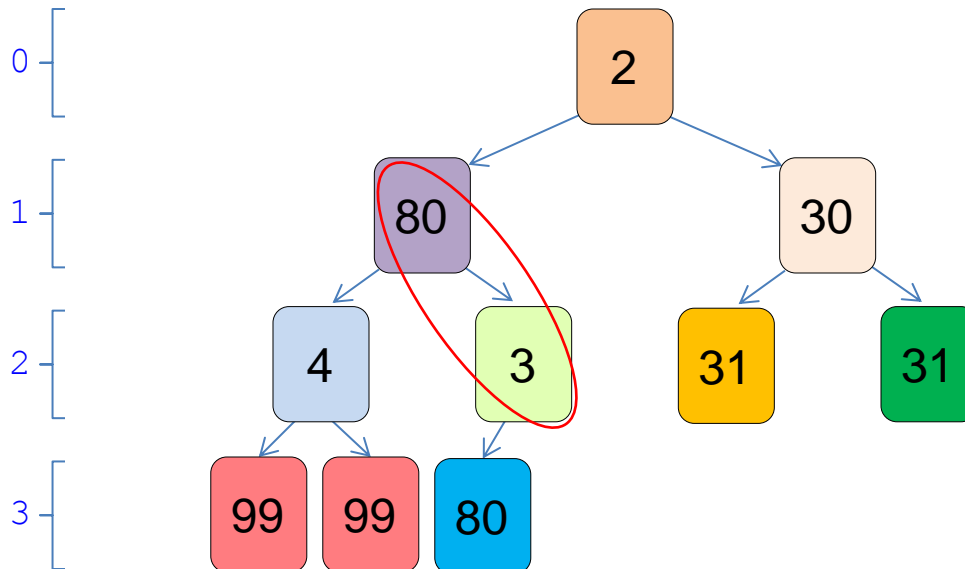
Array-Based Heap:



3. Two Important, Instructional Case Studies

Priority Queues

What is a *Priority Queue*?

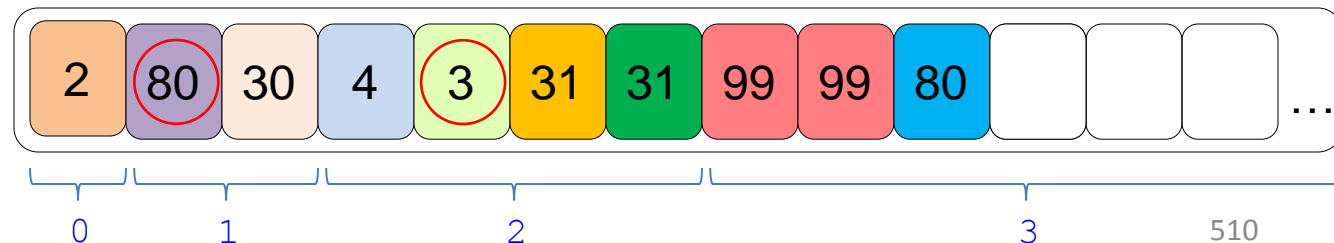


Each element is labeled with its calculated priority.

Each distinct color represents an element having a distinct value.

`q.pop()` ;

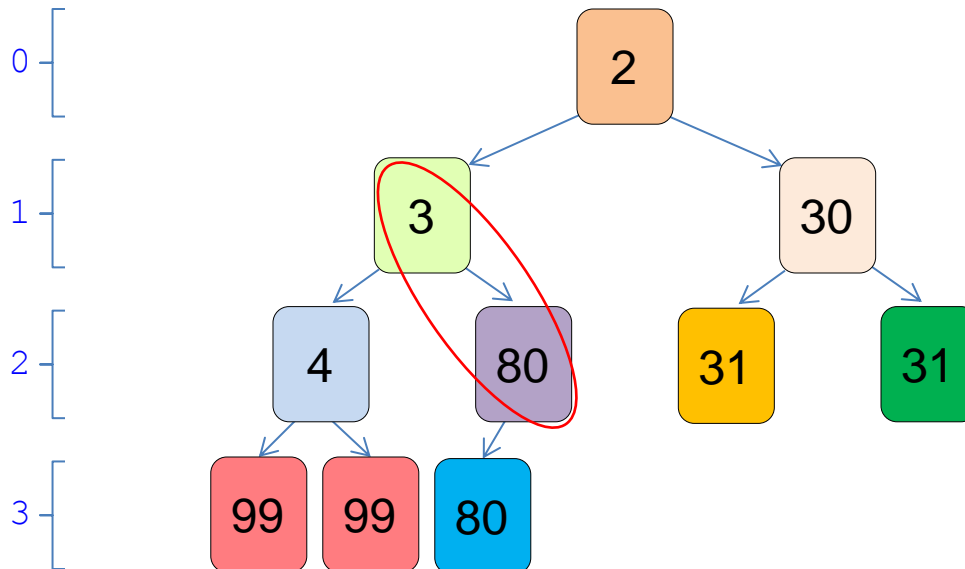
Array-Based Heap:



3. Two Important, Instructional Case Studies

Priority Queues

What is a *Priority Queue*?

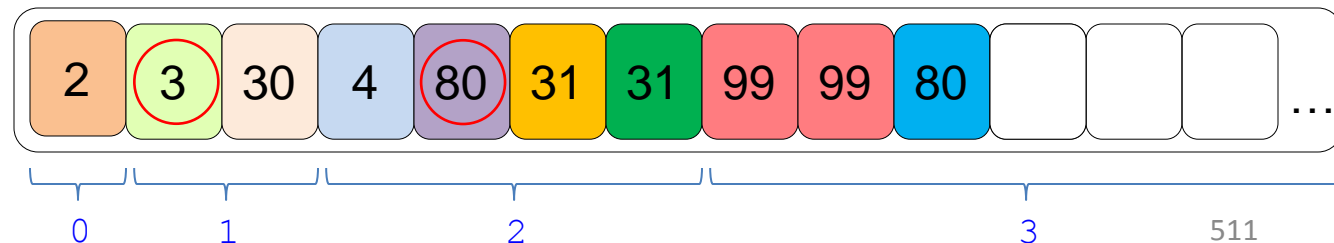


Each element is labeled with its calculated priority.

Each distinct color represents an element having a distinct value.

`q.pop()` ;

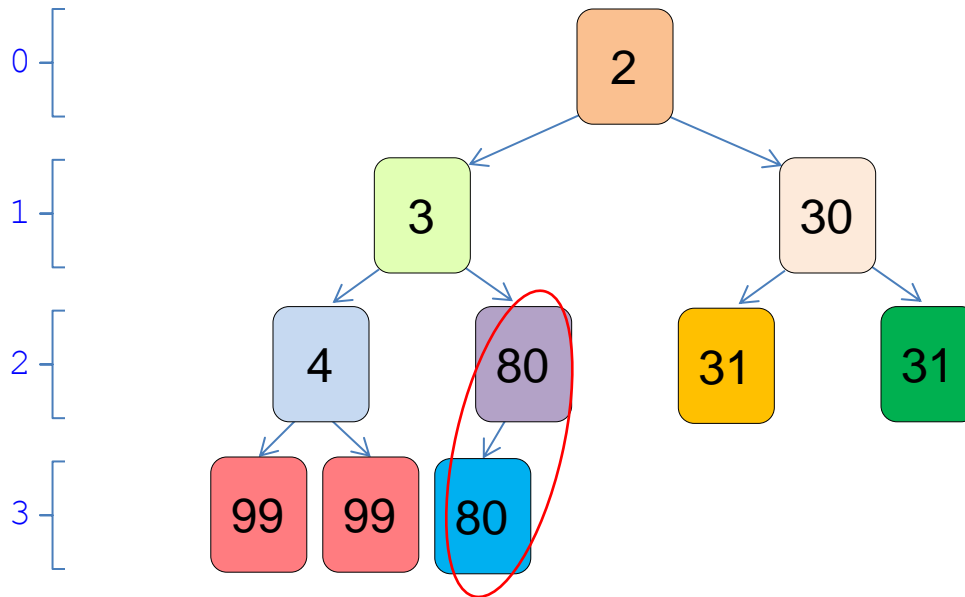
Array-Based Heap:



3. Two Important, Instructional Case Studies

Priority Queues

What is a *Priority Queue*?

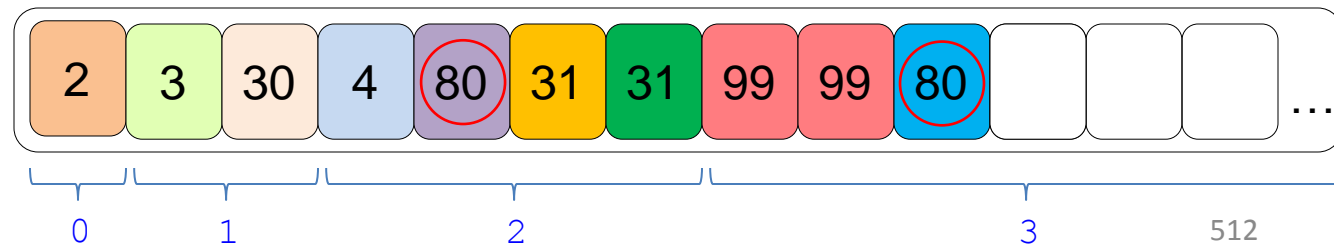


Each element is labeled with its calculated priority.

Each distinct color represents an element having a distinct value.

`q.pop()` ;

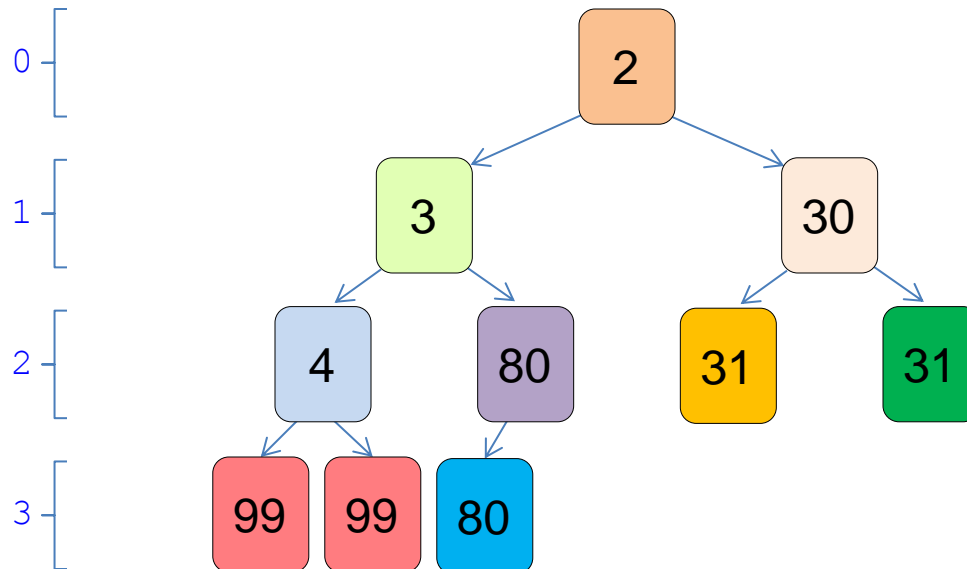
Array-Based Heap:



3. Two Important, Instructional Case Studies

Priority Queues

What is a *Priority Queue*?

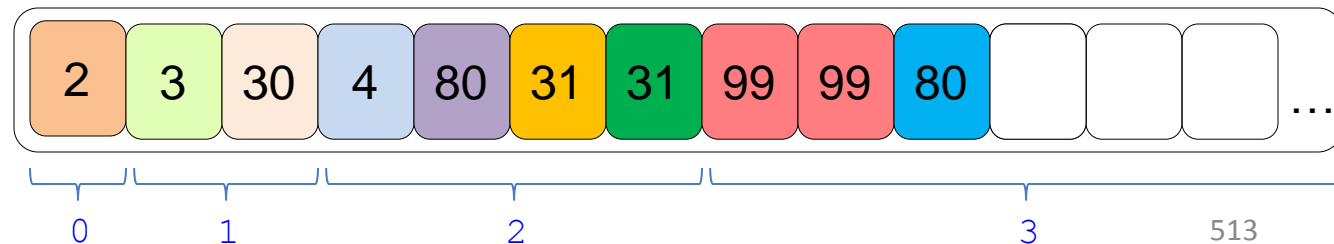


Each element is labeled with its calculated priority.

Each distinct color represents an element having a distinct value.

```
q.pop();
```

Array-Based Heap:



3. Two Important, Instructional Case Studies

Priority Queues

Important Design Questions:

- What is a *Priority Queue*?
- **Why create a separate class for it?**
- Does/should it represent a value?
- How should its value be defined?
- Should such a class be *regular*?

3. Two Important, Instructional Case Studies

Priority Queues

Why create a separate class for it?

3. Two Important, Instructional Case Studies

Priority Queues

Why create a separate class for it?

A Priority Queue is a useful data structure for dispensing value-semantic (as well as other types of) objects according to a user-specified priority order.

3. Two Important, Instructional Case Studies

Priority Queues

Important Design Questions:

- What is a *Priority Queue*?
- Why create a separate class for it?
- **Does/should it represent a value?**
- How should its value be defined?
- Should such a class be *regular*?

3. Two Important, Instructional Case Studies

Priority Queues

Does/should it represent a value?

3. Two Important, Instructional Case Studies

Priority Queues

Does/should it represent a value?

Is a `PriorityQueue` class a *value type*, or a *mechanism*?

3. Two Important, Instructional Case Studies

Priority Queues

Does/should it represent a value?

Is a `PriorityQueue` class a *value type*, or a *mechanism*?

I.e., is there an obvious notion of what it means for two `PriorityQueue` objects to have the same value?

3. Two Important, Instructional Case Studies

Priority Queues

Does/should it represent a value?

I claim, “yes!”

I.e., is there an obvious notion of what it means for two `PriorityQueue` objects to have the same value?

3. Two Important, Instructional Case Studies

Priority Queues

Does/should it represent a value?

I claim, “yes!”

I.e., is the queue of what it means for objects to be in the queue?

Assuming, of course, that the queue-element type is also value semantic.

3. Two Important, Instructional Case Studies

Priority Queues

Important Design Questions:

- What is a *Priority Queue*?
- Why create a separate class for it?
- Does/should it represent a value?
- **How should its value be defined?**
- Should such a class be *regular*?

3. Two Important, Instructional Case Studies

Priority Queues

How should its value be defined?

3. Two Important, Instructional Case Studies

Priority Queues

How should its value be defined?



3. Two Important, Instructional Case Studies

Priority Queues

How should its value be defined?



3. Two Important, Instructional Case Studies

Priority Queues

How should its value be defined?

Two objects of class `PriorityQueue` have the same value iff there does not exist a *distinguishing sequence* among all of its *salient* operations:

1. `top`
2. `push`
3. `pop`

3. Two Important, Instructional Case Studies

Priority Queues

Important Design Questions:

- What is a *Priority Queue*?
- Why create a separate class for it?
- Does/should it represent a value?
- How should its value be defined?
- **Should such a class be *regular*?**

3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

I.e., should our `PriorityQueue` class support all of the value-semantic syntax of a *regular* class?

3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

I.e., should our `PriorityQueue` class support all of the value-semantic syntax of a *regular* class?

Question: How *expensive* would `operator==` be to implement?

3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

Moreover, how on earth would we determine whether two arbitrary `PriorityQueue` objects do or do not have a *distinguishing sequence* of *salient* operations??

3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

Necessary:

3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

Necessary:

- Same number of elements.

3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

Necessary:

- Same number of elements.
- Same numbers of respective element values.

3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

Necessary:

- Same number of elements.
- Same numbers of respective element values.

Sufficient:

3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

Necessary:

- Same number of elements.
- Same numbers of respective element values.

Sufficient:

- Same underlying linear heap order.

3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

Necessary:

- Same number of elements.
- Same numbers of respective element values.

Sufficient:

- Same underlying linear heap order.

BUT IS THIS NECESSARY OR NOT??

3. Two Important, Instructional Case Studies

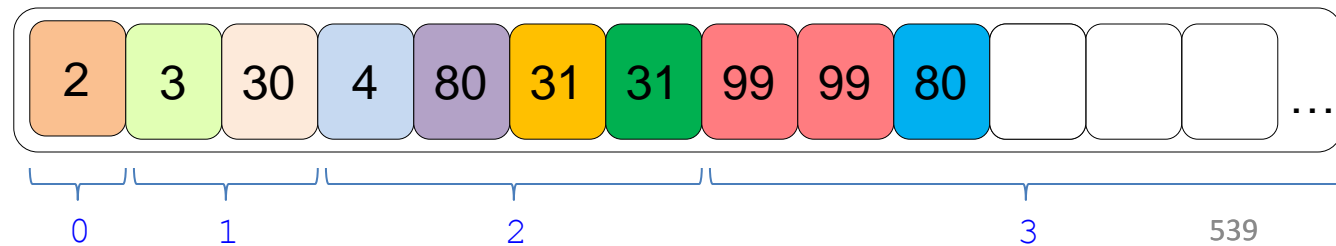
Priority Queues

Should such a class be regular?

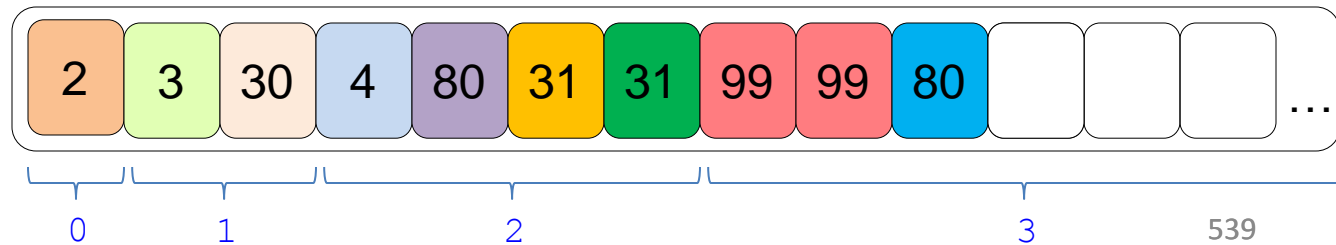
Question: How *expensive* would `operator==` be to implement?

For example, both of these linear heaps pop in the same order:

Array-Based Heap 1:



Array-Based Heap 2:



3. Two Important, Instructional Case Studies

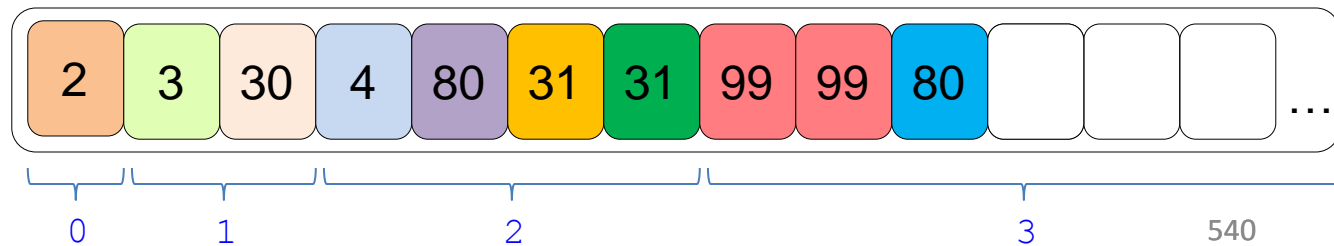
Priority Queues

Should such a class be regular?

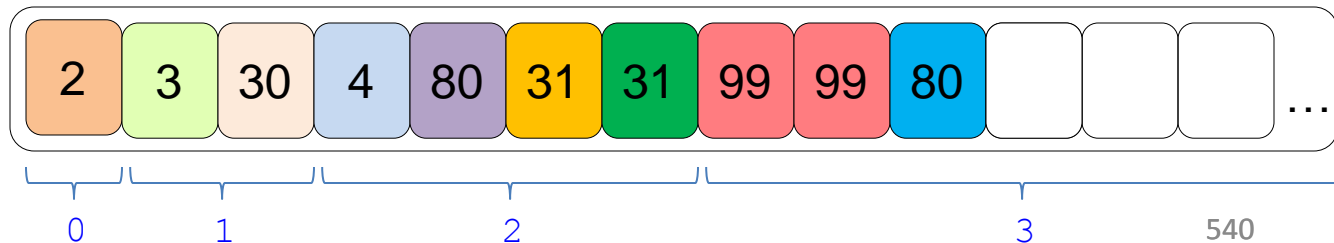
Question: How *expensive* would `operator==` be to implement?

For example, both of these linear heaps pop in the same order (**of course!**):

Array-Based Heap 1:



Array-Based Heap 2:



3. Two Important, Instructional Case Studies

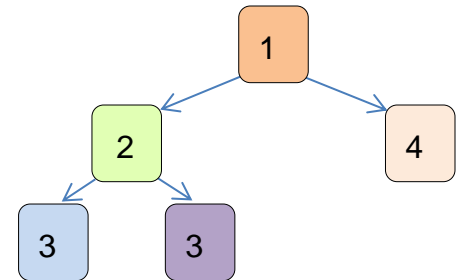
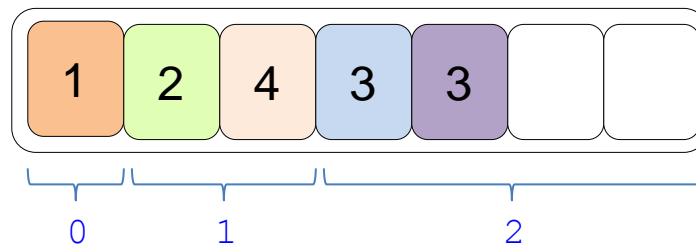
Priority Queues

Should such a class be regular?

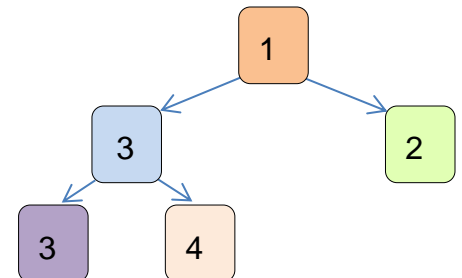
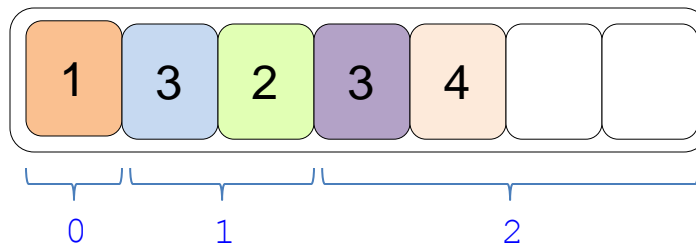
Question: How *expensive* would `operator==` be to implement?

But so do these:

Array-Based Heap 1:



Array-Based Heap 2:



3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

As it turns out, we can distinguish these two values with appropriate **pushes**, **tops**, and **pops**.

3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

As it turns out, we can distinguish these two values with appropriate **pushes**, **tops**, and **pops**.

But can we always do that?

3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

As it turns out, we can distinguish these two values with appropriate **pushes**, **tops**, and **pops**.

But can we always do that?

If we aren't sure, should we implement `operator==` for this class anyway?

3. Two Important, Instructional Case Studies

Priority Queues

Should we

Qu

What if we know that more than 99.99% (but less than 100%) of the time we can distinguish the values of two `PriorityQueue` objects that do not have the same linear heap orderings?

top

But then we always do that?

If we aren't sure, should we implement `operator==` for this class anyway?

3. Two Important, Instructional Case Studies

Priority Queues

Should we

What if we know that
99.99% (b

I say No!

Perhaps make it a
named function.

If we aren't sure, should we implement
`operator==` for this class anyway?

3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

Suppose it were true that, for any pair of priority queues, where the linear heap order is not the same, there exists a distinguishing sequence of salient operations that distinguishes them:

What is the complexity of `operator==`?

3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

Suppose it were true that for any pair of priority queues, there exists a linear heap order isomorphism. There exists a distinguishing sequence of salient operations that distinguishes them:

What is the complexity of `operator==`?

3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

Until quite recently, that linear order is
necessary was just a conjecture.

3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

Until quite recently, that linear order is
necessary was just a conjecture.

I finally have a simple constructive proof.

3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

Until quite recently, that linear order is necessary was just a conjecture.

I finally have a simple constructive proof.

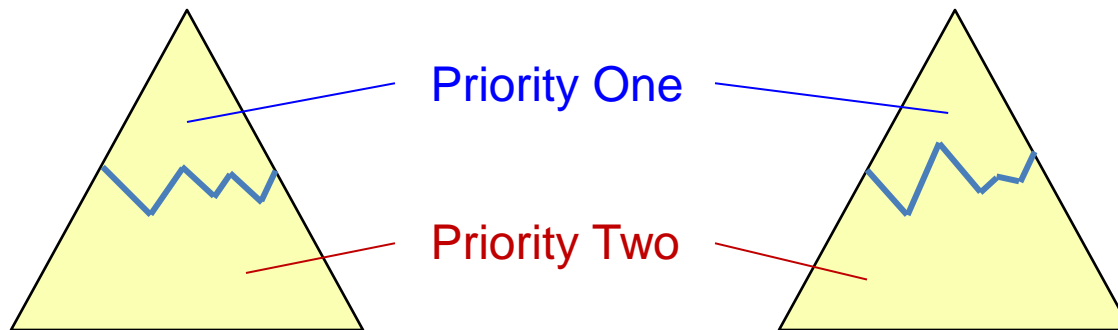
Here is a very quick sketch:

3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

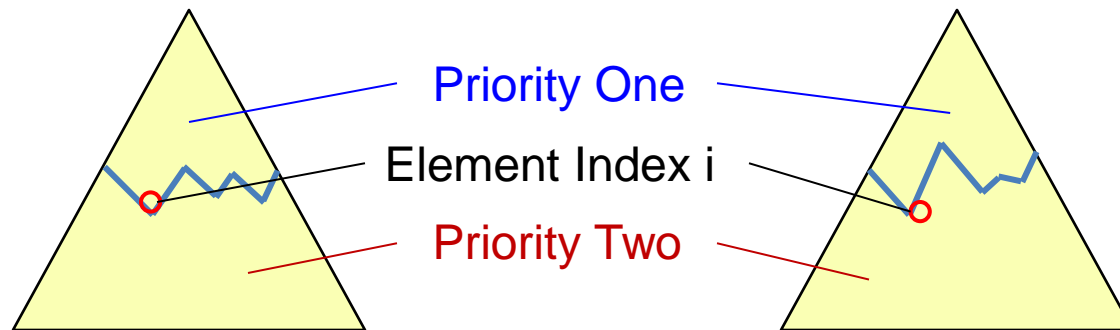


3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?



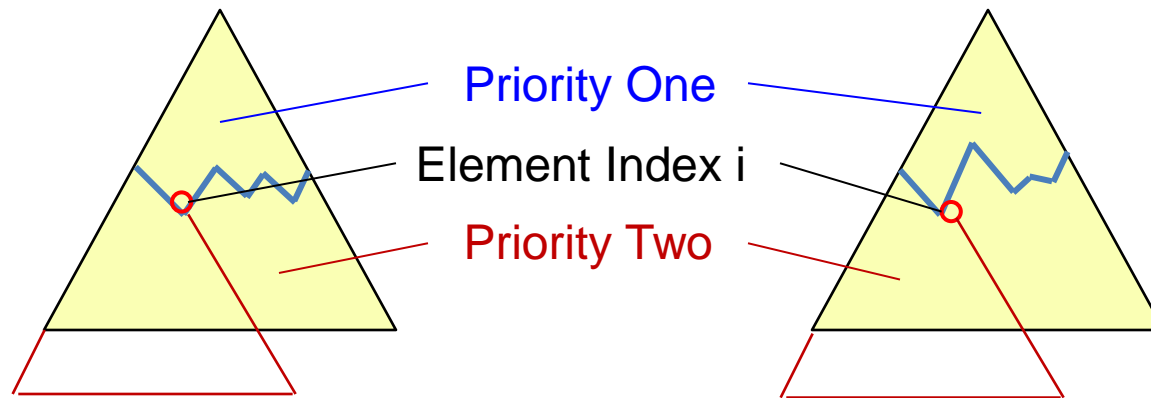
Highest-Index Element Having Distinct Priorities

3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?



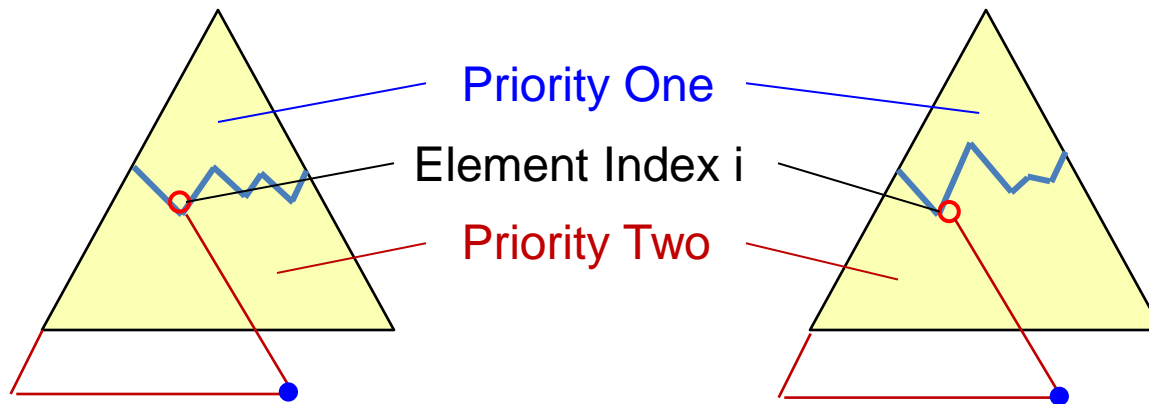
Push Arbitrary Priority-Two Values

3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?



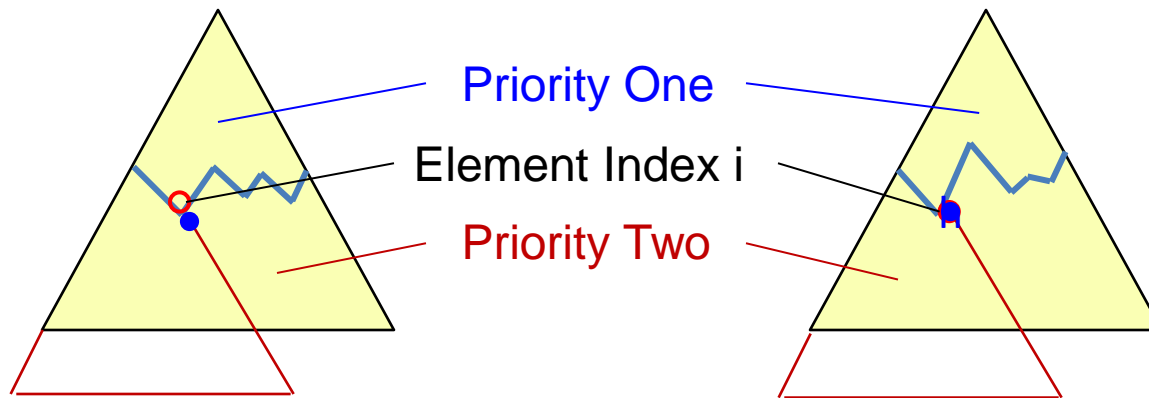
Push a Priority-One Value

3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?



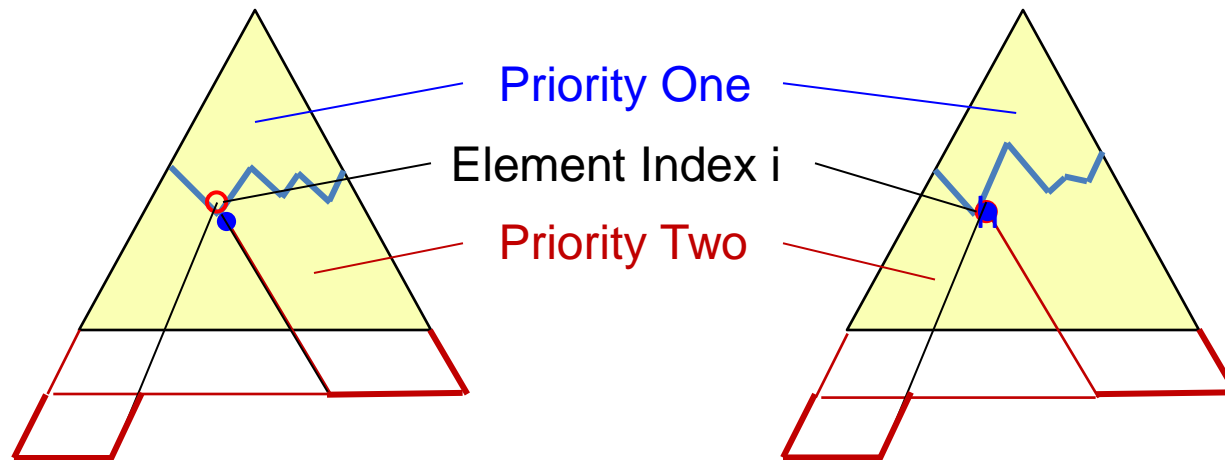
Push a Priority-One Value

3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?



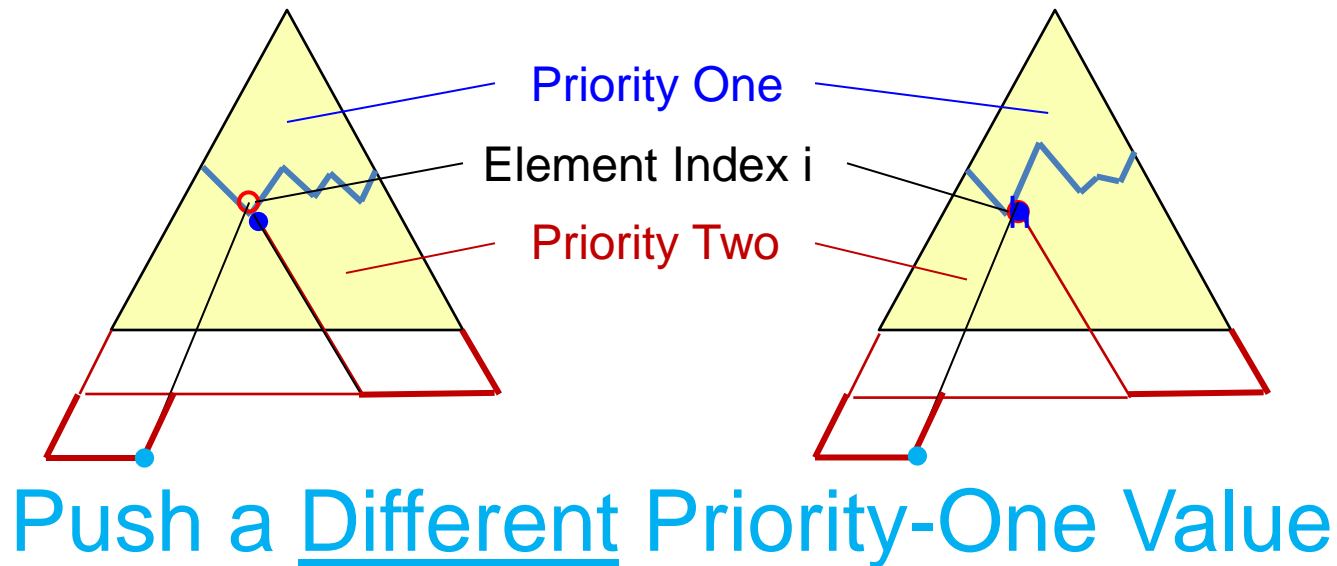
Push Arbitrary Priority-Two values

3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

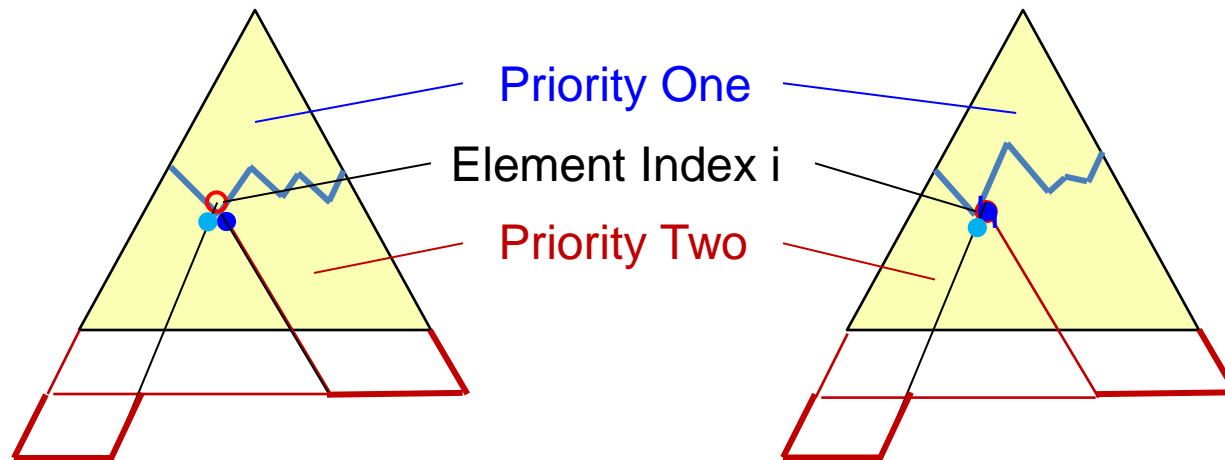


3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?



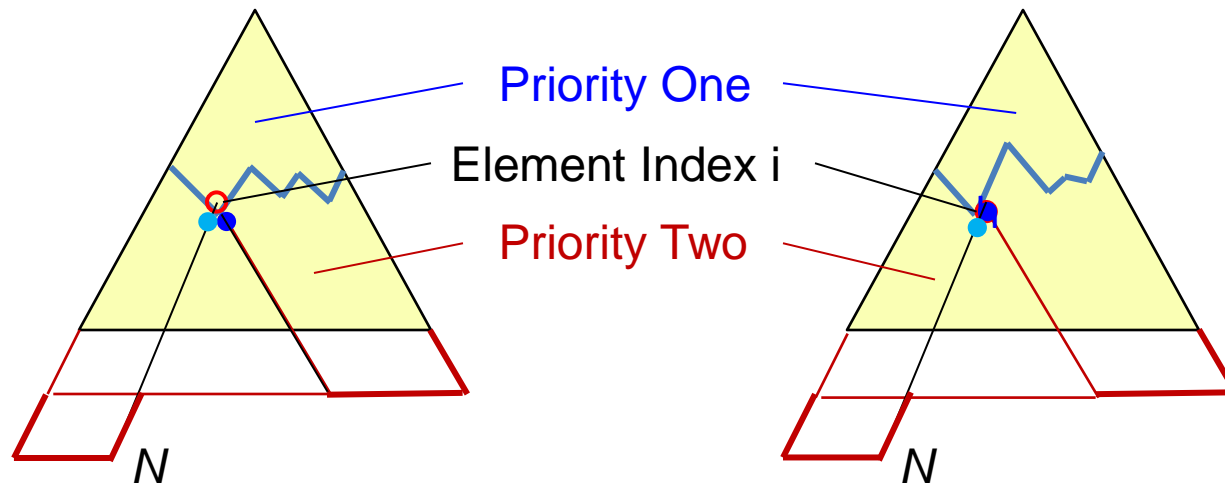
Push a Different Priority-One Value

3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?



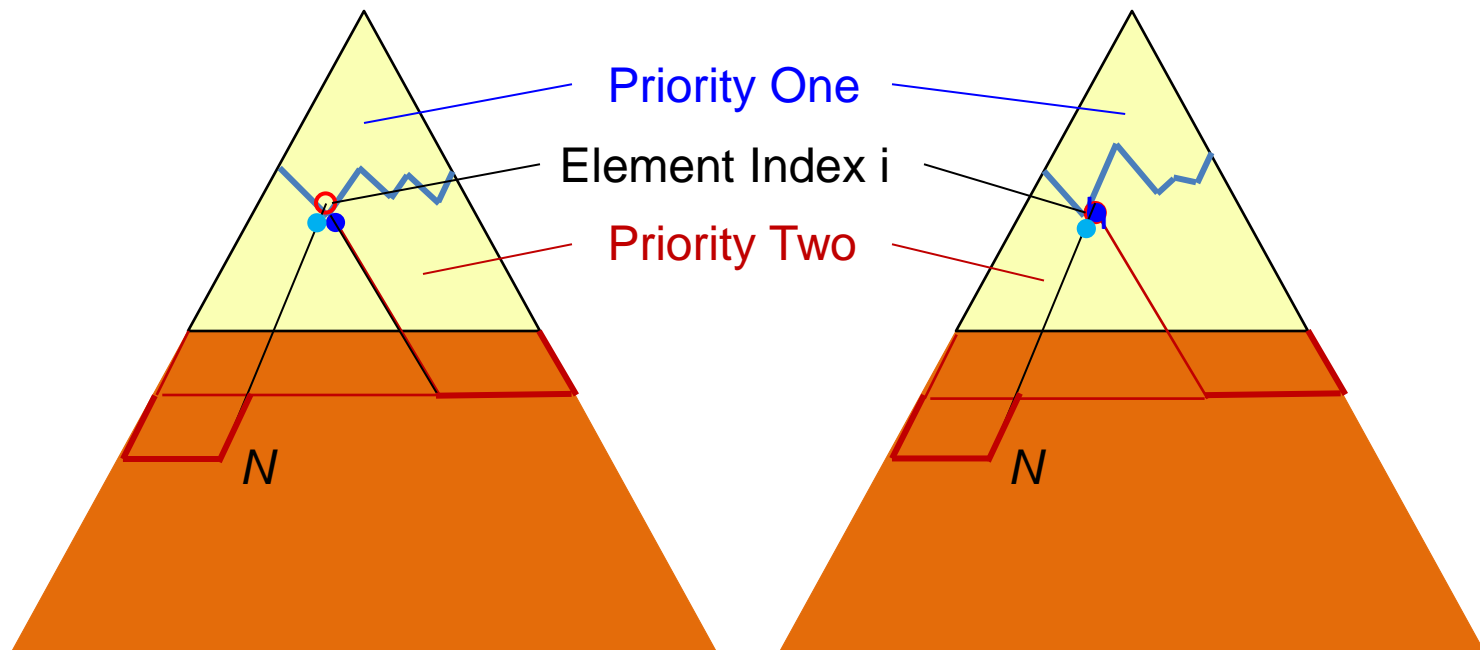
Push *N* Arbitrary Priority-Two Values

3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?



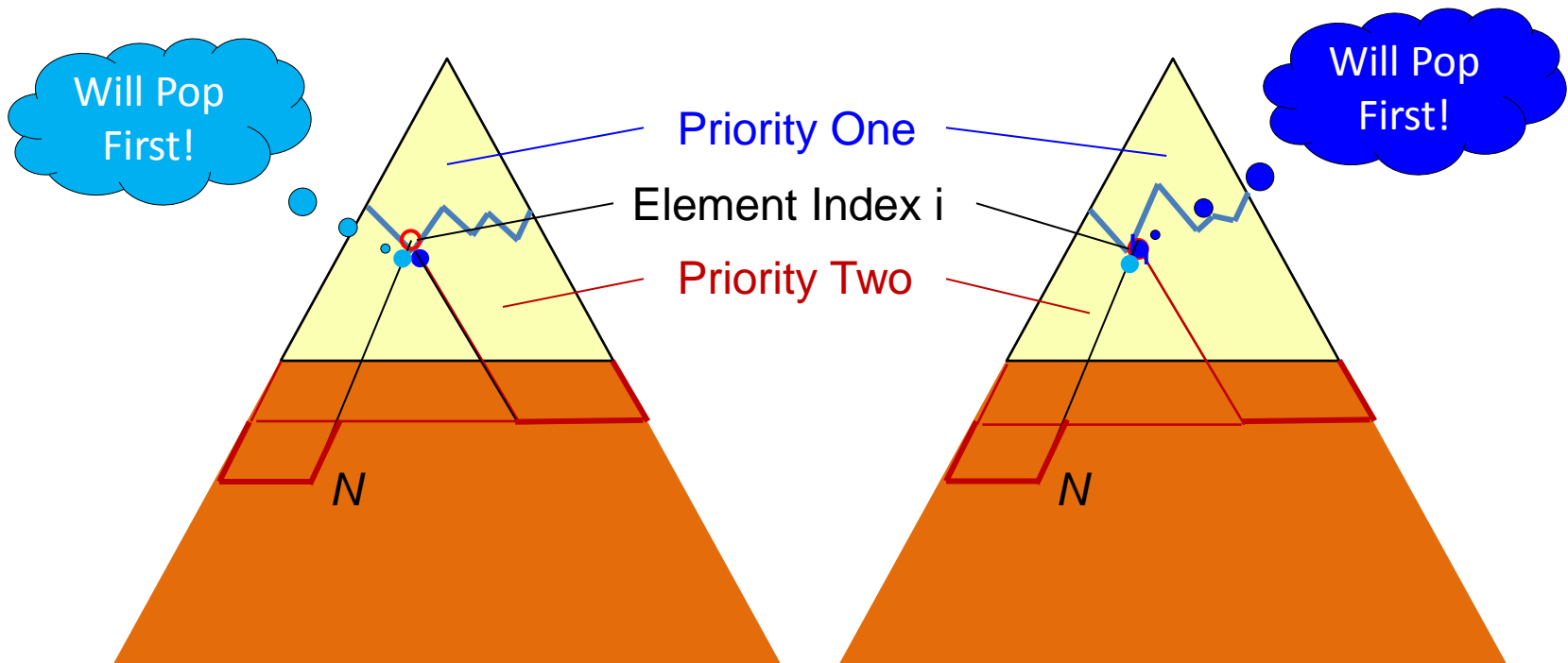
Push N Arbitrary Priority-Two Values

3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?



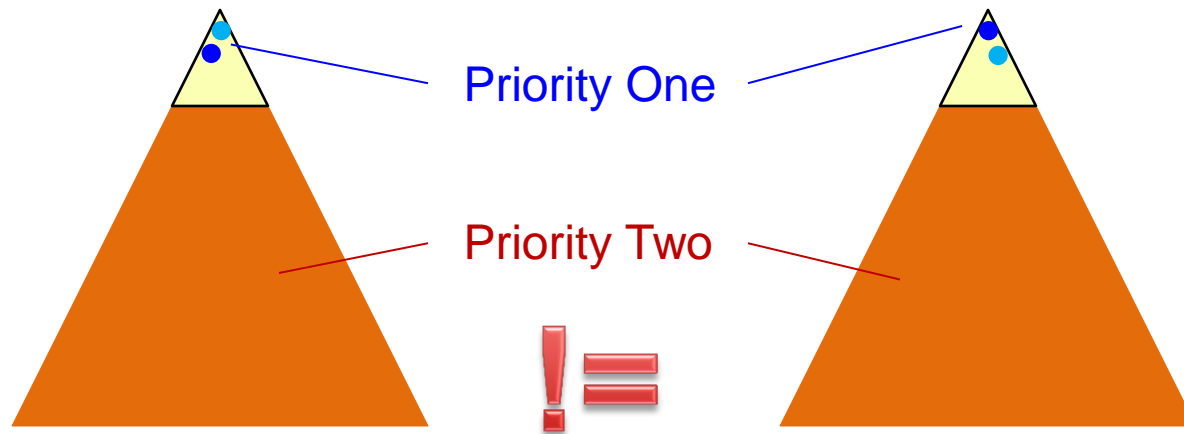
Pop N Elements

3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?



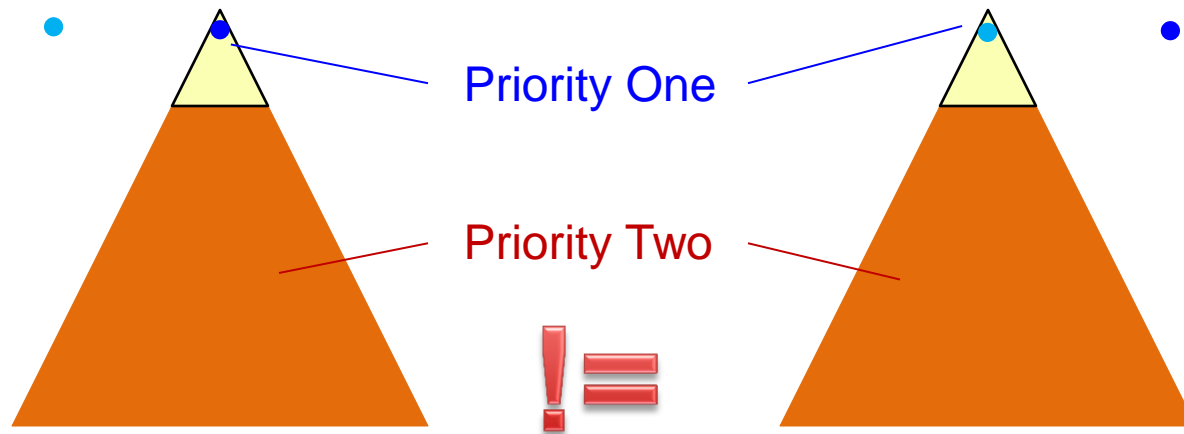
After almost N_{pop} operations
the tops are not the same!

3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?



After one more `pop` operation
the element values are not the same!

3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?



3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

YES IT SHOULD!

3. Two Important, Instructional Case Studies

Priority Queues

Should such a class be regular?

Question: How *expensive* would `operator==` be to implement?

YES IT SHOULD!
O[N] !!!

3. Two Important, Instructional Case Studies

Priority Queues

Discussion?

Outline

1. Introduction and Background

Components, Physical Design, and Class Categories

2. Understanding Value Semantics (and Syntax)

Most importantly, the Essential property of Value

3. Two Important, Instructional Case Studies

Specifically, *Regular Expressions* and *Priority Queues*

4. Conclusion

What must be remembered when designing value types

Outline

1. Introduction and Background

Components, Physical Design, and Class Categories

2. Understanding Value Semantics (and Syntax)

Most importantly, the *Essential property of Value*

3. Two Important, Instructional Case Studies

Specifically, *Regular Expressions* and *Priority Queues*

4. Conclusion

What must be remembered when designing value types

4. Conclusion

What to Remember about VSTs

4. Conclusion

What to Remember about VSTs

So what are the take-aways?

4. Conclusion

What to Remember about VSTs

So what are the take-aways?

- Some types naturally represent a *value*.

4. Conclusion

What to Remember about VSTs

So what are the take-aways?

- Some types naturally represent a *value*.
- Ideally, each value type will have *regular* syntax.

4. Conclusion

What to Remember about VSTs

So what are the take-aways?

- Some types naturally represent a *value*.
- Ideally, each value type will have *regular* syntax.
- Moreover, all operations on value types should follow proper *value semantics*:

4. Conclusion

What to Remember about VSTs

So what are the take-aways?

- Some types naturally represent a *value*.
- Ideally, each value type will have *regular* syntax.
- Moreover, all operations on value types should follow proper *value semantics*:
 - Value derives only from autonomous object state, but not all object state need contribute to value.

4. Conclusion

What to Remember about VSTs

So what are the take-aways?

- Some types naturally represent a *value*.
- Ideally, each value type will have *regular* syntax.
- Moreover, all operations on value types should follow proper *value semantics*:
 - Value derives only from autonomous object state, but not all object state need contribute to value.
 - Adhere to the Essential Property of Value.

4. Conclusion

What to Remember about VSTs

So what are the take-aways?

- Some types naturally represent a *value*.
- Ideally, each value type will have *regular* syntax.
- Moreover, all operations on value types should follow proper *value semantics*:
 - Value derives only from autonomous object state, but not all object state need contribute to value.
 - Adhere to the Essential Property of Value.
 - Behave as if each value has a canonical internal representation.

4. Conclusion

What to Remember about VSTs

- Two objects of a given value-semantic type have the same value iff there does not exist a *distinguishing sequence* among all of its *salient* operations.

Value is in a class's DNA

4. Conclusion

What to Remember about VSTs

The **key** take-away:

4. Conclusion

What to Remember about VSTs

The **key** take-away:

What makes a value-type *proper*
has essentially **nothing** to do with
syntax...

4. Conclusion

What to Remember about VSTs

The **key** take-away:

What makes a value-type *proper* has essentially **nothing** to do with ***syntax***; it has **everything** to do with ***semantics***:

4. Conclusion

What to Remember about VSTs

The **key** take-away:

What makes a value-type *proper* has essentially nothing to do with *syntax*; it has everything to do with *semantics*: A class that respects the **Essential Property of Value** is value-semantic...

4. Conclusion

What to Remember about VSTs

The **key** take-away:

What makes a value-type *proper* has essentially nothing to do with *syntax*; it has everything to do with *semantics*: A class that respects the **Essential Property of Value** is value-semantic; **otherwise, it is not!**

For More Information

- Find our open-source distribution at:
<http://www.openbloomberg.com/bde>
- Moderator: kpffleming@bloomberg.net
- How to contribute? *See our site.*
- All comments and criticisms welcome...
- I can be reached at jlakos@bloomberg.net

The End